

Types of wires & cables

The wires used for internal wiring of building may be divided into different groups.

(i) Conductor used (copper & aluminium)

(ii) Numbers of cores

(i) single core

(ii) Twine core

(3) Voltage rating (250V, 440V)

~~250V~~ (650V to 1100V)

(4) Types of insulation used

(i) Vix (vulcanised Indian rubber)

(ii) Tough rubber
or Caf

(i) (240 / 420 / 650V / 1100)

(iii) lead sheathed cables they are available for 240-440V grades that provide good protection

(iv) PVC (220 to 440 / 600 - 1100V grades)

harder than rubber better than insulator

(v) Weather proof cable $\therefore$ they are used for outdoor wiring and

industrial used for (200/250, 680/1100)

used for house volt & lines

- (vi) Multi strand cables ÷ these are more flexible and durable having healthy sheathing capacity skin effect is better in case of higher frequency

Components of LT switch gear:
(low tension voltage)

1 ϕ 3 ϕ

220V, 440V, 11kV, 33kV, 66kV, 110kV (AC)

- (i) fuse ÷ function of fuses is to carry the normal working current safely without heating.

- (ii) SFU ÷ switch fuse unit
(i) double pole $\rightarrow$ 1 ϕ controlling 1
(ii) triple pole $\rightarrow$ 3 ϕ 3 wire controlling

Iron clad switch

- (iii) protection device $\rightarrow$ PVC

- (iv) ELCB ÷ Earth leakage circuit breaker

- (v) ~~valley~~ + valving operator earth breaker

Wires and Cables

* The wires used for internal wiring of buildings may be divided into different groups

(i) Conductor used

(i) CU Conductor cables

(ii) Aluminium Conductor cables

(ii) Number of Cores used

(i) Single core cables

(ii) Twin core cables

(iii) Three core cables

(iii) Voltage grading

(i) 250/440 volt cables

(ii) 650/1100 volt cables

(iv) Type of insulation used :-

(i) (VIR) insulated cables (vulcanized indian rubber) available in 240/415 V & 650/1100 V grades.

(v) Tough Rubber sheathed (TRS) or
Cable Type sheathed (CTS) cables.

Electrical Installation

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* wire ÷ A wire is made of a single conductor used for carrying electrical current.

* Cable ÷ A cable is a group of multiple conductors inside a common sheathing. Used for carrying electrical current.

Different between wires & Cable

Wire	Cable
i) wire is made of a single conductor.	i) Cable is made of multiple conductor.
ii) wire is used to carry electricity to bear (tension) mechanical loads.	ii) Cable is used for ^{signal} power transmission for telecommunication signal or to carry electricity.
iii) Ex ⇒ copper wire, Al wire.	Ex ⇒ HDMI cable, USB cable
iii) Ex ⇒ type ÷ solid standard	iii) multi conductor optical fiber cable

* Types of wires and cables

- i) Conductor material used
 - ii) number of cores used
 - iii) voltage grading
 - iv) type of insulation used
- a) (VIR) Vulcanized Indian Rubber cable (VIR)
 - b) Tough Rubber Sheathed (TRS)
 - c) Polyvinyl chloride cable (PVC)
 - d) Weather proof cables
 - e) Lead sheathed cables

- (f) flexible cords and cables
- (g) Multi-strand cable
- (h) XLPE cables

(i) Conductor used: (i) Copper Conductor cable
(ii) Aluminium Conductor cable

(ii) No. of cores used: (i) single core cable
(ii) Twin core cable
(iii) Three core cable

(iii) Voltage grading: (i) 250V/440V cable
(ii) 650/1100V cable

(iv) Types of insulation used:

(a) VIR: Vulcanized Indian rubber cable available in 240V/415V & 650V/1100V grades.

(b) TRS: Tough rubber sheathed: available in
→ 250V/440 & 650V/110V grades
→ cheaper in cost or lighter in weight & easier in installation and weather proof cable it used in wet condition.

(c) PVC cable: polyvinyl chloride cables - available in 250V/440V & 650V/1100V grades.
→ Used in cabling - capping bottom
→ harder than rubber, better insulating quality & flexibility.

- (d) Weather proof cables : weather proof cables available in 240/415 V & 650V/110V grades. used for outdoor wiring, industrial supply, power supply.
- (e) Lead Sheathed Cable : Lead Sheathed cables available in 240V/415V grades used for good protection against moisture & protection against mechanical injury.
- (f) flexible cords & cables : flexible cords and cables used for house hold appliances. Not used in fixed wiring.
- (g) Multi strand cables : Multi-strand cables are more flexible & durable. Surface area of multi strand cable is more so heating radiating capacity is more.
- (h) XLPE Cables : XLPE Cables built of insulation made of polymers. Higher current rating, longer service life.



Define Switchgear : The apparatus used for switching, controlling, protecting the electrical circuit and equipment is known as switchgear. from overload & short circuit

Call of Switch

- LV switchgear $\rightarrow$ 1000 V to 1500 V
- MV switchgear $\rightarrow$ 3.3 kV to 33 kV
- HV switchgear $\rightarrow$ above 36 kV

* LT Switchgear $\rightarrow$ Low tension switchgear
Voltage

* Various Components of LT Switchgear

- (i) fuse
- (ii) switch fuse unit (sfu)
- (iii) Miniature circuit breaker (MCB)
- (iv) Earth leakage circuit breaker (ELCB)
- (v) Moulded case circuit breaker (MCCB)

(i) fuse $\div$ A fuse is an electrical safety device which is used in electrical circuit for protecting electrical equipment against overloads or short circuit. It based on the principle of heating effect of electric current.

(ii) (sfu)

Switch fuse unit $\div$ Switch fuse unit is the combination of one switch and one fuse unit. Sfu protect the circuit against excessive current, Sfu is also known as iron clad switch.

Types of sfu (i) Double pole Iron clad

(ii) Triple pole Iron clad

(iii) Triple pole with neutral link iron clad

(i) Double pole iron clad $\div$ 1ϕ 2 wire circuit

(ii) Triple pole iron clad $\div$ 3ϕ , three wire circuit

(iii) Triple pole with neutral iron clad $\div$ 3ϕ , 4 wires
(with neutral wire)

(MCB)

(iii) Miniature Circuit Breaker: A Miniature Circuit Breaker is an automatically operated electrical switch which is used to protect low voltage electrical circuits from excessive current and overload or short circuit.

MCB are available with different current rating 1, 2, 2.5, 3, 4, 5, 6, 7, 7.5, 10, 16, 20, 25, 32, 35, 40, 63, 100, 125, 160 A and voltage rating (240/415 V) ac and upto 220V DC

uses: It is used to protect devices such as Air Conditioners, refrigerators, & Computers. (ELCB)

(iv) Earth Leakage Circuit Breaker: Earth Leakage Circuit Breaker is an electrical device that protect against earth leakage.

If any current leaks from any electrical wire due to insulation failure then ELCB detects that earth leakage and makes the power supply off. otherwise it harmful if anyone touches the insulation.

There are two types of earth leakage circuit breaker

(i) voltage ELCB (ii) Current ELCB

(i) voltage ELCB: A voltage ELCB is a voltage operated circuit breaker that contains relay coil which connected to the metallic body and at the other end is connected to ground wire. 3rd wire

(b) Current ELCB: Current ELCB is a current operated circuit breaker it applies on 3 phase and 3 wires, its work is to break circuit.
both ELCB works on circuit break.

(MCCB)
*v) Moulded Case Circuit Breaker: MCCB is an automatic ^{operated} electrical device which is used to protect the electrical equipment or circuits and devices from overload, short-circuit and earth fault. MCCB is much larger than MCB. ~~MCCB is available in 32 A up to 8000 A and voltage range 220V to 11 kV.~~ MCCB rating can be changed as per requirement it is the biggest advantage of MCCB.

* what is earthing? why it is provided?

ans) Earthing is the process of connecting metallic body of electrical equipment to earth for transferring the immediate ~~dis~~charge of the electrical energy directly to the earth by the help of low resistance wire, is known as the electrical earthing.

Earthing is provided

(i) To avoid electric shock

(ii) To avoid risk of fire

(iii) To ~~avoid~~ provide the humans from electric shock.

(iv) To protect equipments from excessive flow of current.

* Methods of earthing are:

- (i) wire or strip earthing
- (ii) Rod earthing (1m)
- (iii) Pipe earthing (8ft)
- (iv) plate earthing (1.5m)

* Batteries, Types, characteristics

* Battery: A battery is the collection of more than one cells to create the flow of electrons within a circuit. Battery is the primary power source for any gadget used in smartphone, laptop, watch, remote. In the batteries chemical energy is converted into electrical energy.

* Types of batteries

- (i) Primary Batteries
- (ii) Secondary Batteries

(i) primary Batteries: primary batteries are that batteries which cannot be ~~recharge~~ recharged. primary batteries are made of electrochemical cells whose electrochemical reaction cannot be reversed. primary battery used where low amount of power requires. it cannot be recharge so that it is expensive. Examples: Uses $\rightarrow$ Remote, watch
Dry Cell, alkaline batteries

Advantages:

- (i) Small in size
- (ii) low internal resistance
- (iii) long life capacity
- (iv) Higher efficiency

* Define ampere hour efficiency of battery
→ Ampere hour efficiency is the ratio of output and input ampere hour of the cell.

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* Secondary Batteries: Secondary batteries are that batteries which can be recharged. Secondary batteries are made of electrochemical cells whose electrochemical reaction can be reversed. It is also too expensive.

Ex ⇒ Lithium ion batteries
Nickel, Cadmium

* Types of primary battery.

- (i) Alkaline battery
- (ii) Silver oxide battery

(i) Alkaline battery: These are the most common type of primary batteries. They have a long life and they can provide reliable power to devices such as flashlights, remote and toys. Chemical composition → Zinc with manganese dioxide and potassium hydroxide electrolyte.

(ii) Silver oxide battery: These are the most common types of primary batteries used in small electronic devices such as calculators, watches. They have a long life and provide stable voltage output.

* Types of Secondary battery

- (i) Lithium-ion battery
- (ii) Lead acid battery

* Explain any two types of battery

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(i) Lithium-ion battery : Lithium-ion battery is the most commonly rechargeable battery used for electronic devices such as smartphone, laptops. They are lightweight and high energy density.

Anode $\rightarrow$ Graphite

Cathode $\rightarrow$ Lithium metal oxide

Electrolyte $\rightarrow$ aq. solution dissolved with lithium salts

Voltage $\rightarrow$ 3.7 - 3.85 V

used in $\rightarrow$ smartphones, laptops

(ii) Lead acid battery : These are the commonly used in cars and other vehicles and backup power supplies, It has high energy density. It can provide a lot of power for short periods of time.

Anode $\rightarrow$ Lead metal

Cathode $\rightarrow$ Lead dioxide

Electrolyte $\rightarrow$ H_2SO_4

Voltage $\rightarrow$ 2V

used in $\rightarrow$ cars, vehicles.

Q1) What are important characteristics for a battery?

- ① Capacity $\div$ Capacity refers to the amount of energy of a battery that can store and it is measured in ampere-hours (Ah).
- ② Voltage $\div$ Voltage is the electrical potential difference between two points in a circuit and it determines how much energy a battery can deliver to a device.
- ③ Charge time $\div$ This is the amount of time it takes for a battery to fully recharge and it's important for devices that need to be charged quickly.
- ④ Cycle life $\div$ Cycle life refers to the number of times a battery can be charged and discharged before its capacity begins to degrade.
- ⑤ Cost $\div$ Finally the cost of a battery is an important consideration as it can vary widely depending on the technology, capacity and other features.
- ⑥ Power $\div$ Power is the rate at which a battery can deliver energy to a device. It is measured in watts (W).

(*) Briefly discuss different methods of charging battery.

ans $\Rightarrow$ Two methods of charging battery.

- i) Constant current method
- ii) Constant voltage method

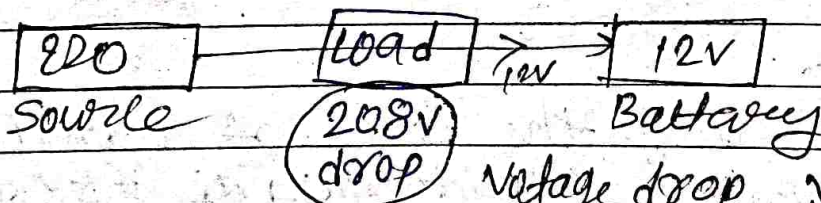
① Constant current method $\div$

① DC source voltage is ^{more} greater than battery voltage

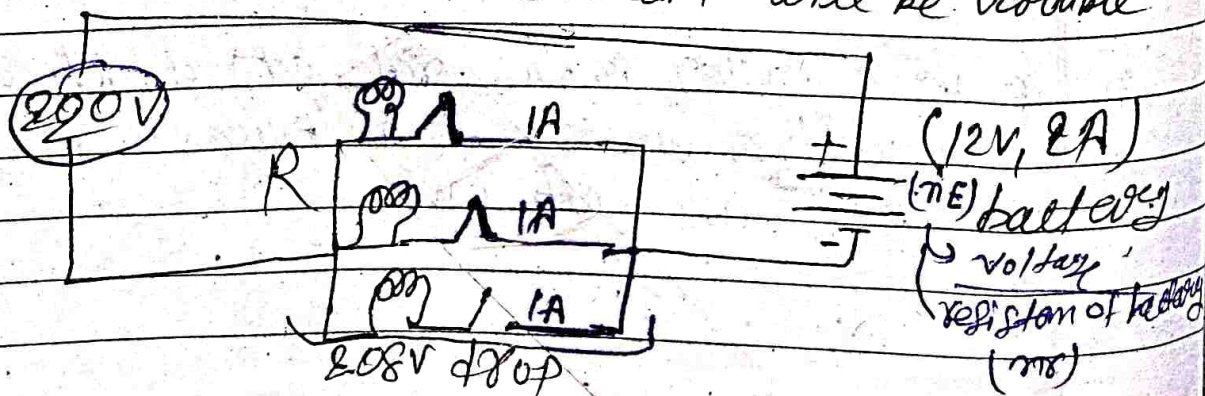
DC Source (↑↑↑)
(220V)

battery
(6, 8, 10, 12, 20)

ii) Current should be constant till discharging to charging the battery.
Constant current



So there voltage drop so
current drop hence
there current will be variable



$$V = IR$$

$$I = \frac{V_{total}}{R_{total}}$$

$$I = \frac{V - nE}{R + nr}$$

$$R = \frac{V - nE}{I} - nr$$

② Constant voltage method

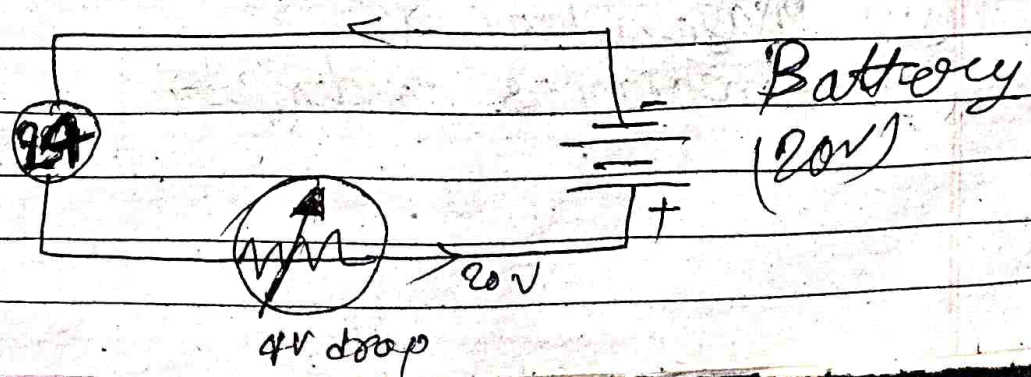
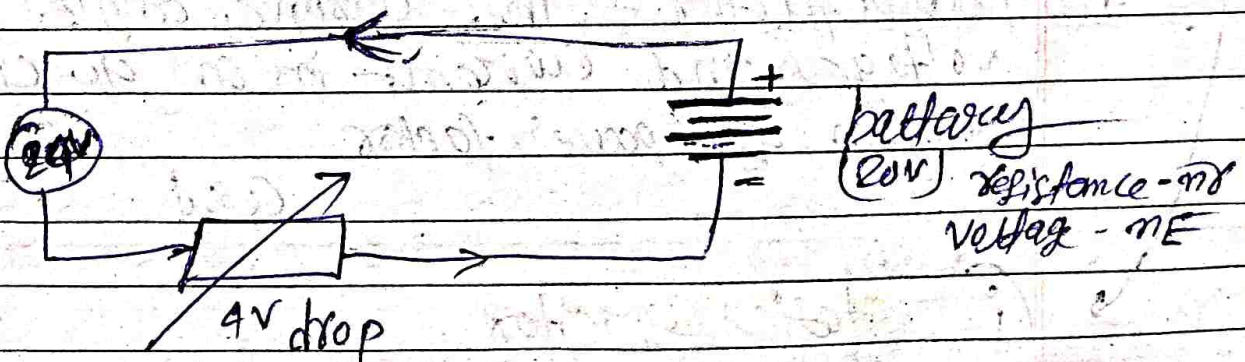
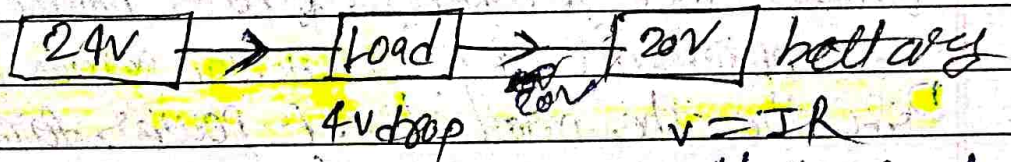
① DC source voltage is little greater than battery.

DC source
(24V)

Battery
(8, 10, 12, 20V)

② Voltage should be constant till discharging to charging the battery.
Constant Voltage

DC source



what are electrical measuring instruments
what are different types of electric measuring instruments.

ans →

- i
- ii
- iii
- iv
- v
- vi
- vii

Ammeter → It finds current in a conductor

Voltmeter → It finds voltage in a conductor

Multimeter → It can find both V & I at once

Wattmeter → It finds power in a wire

Ohmmeter → It finds resistance in a wire

Galvanometer

Digital multimeter

Electrical measuring tools are a device which is used to measure the magnitude of an electric current, voltage, resistance, power.

* Enlist two methods for power factor improvement. What are power factor its significance

* Describe the methods of power factor improvement

* Power factor ÷ The cosine angle between voltage and current in an AC circuit is known as power factor

$\cos \phi$



* Significance of power factor

- i
- ii
- iii

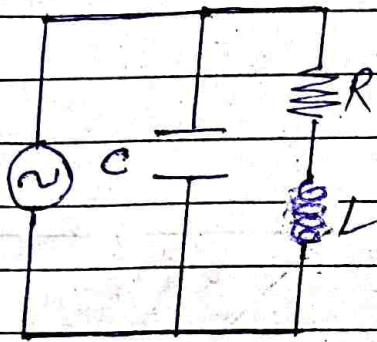
less electricity cost

less heat

long life of the electrical system

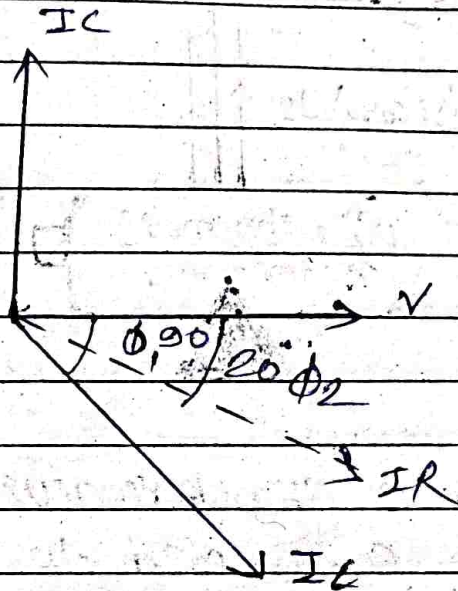
(PYQ) Describe methods of power factor improvement.

(1) Static Capacitor :-



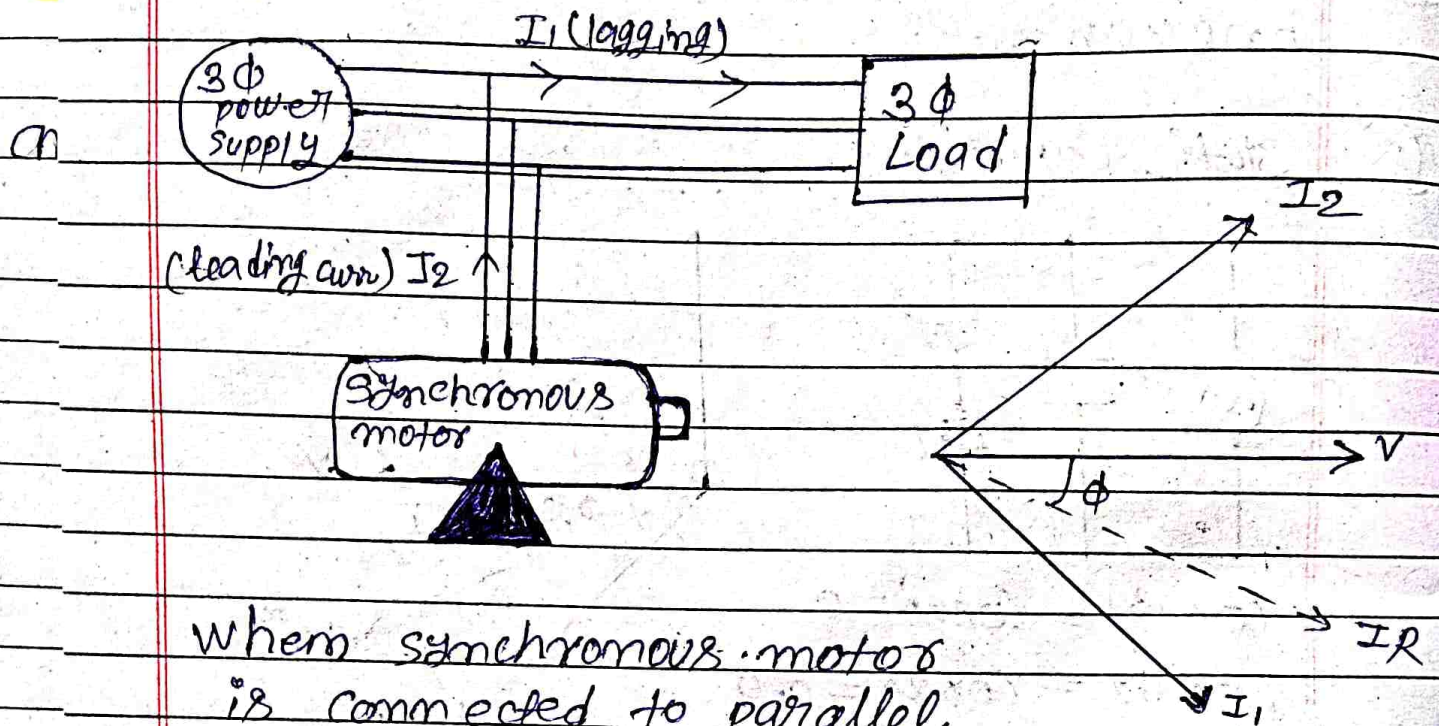
$$\cos \phi_1 = \cos 90^\circ = 0$$

$$\cos \phi_2 = \cos 20^\circ = 0.9$$



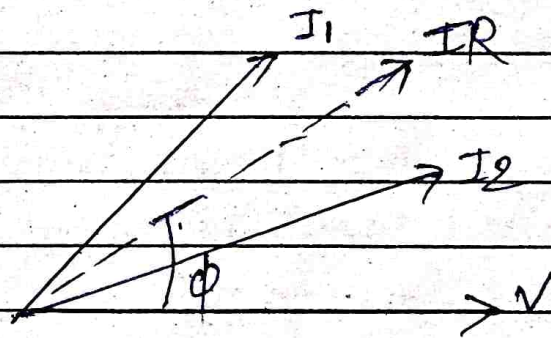
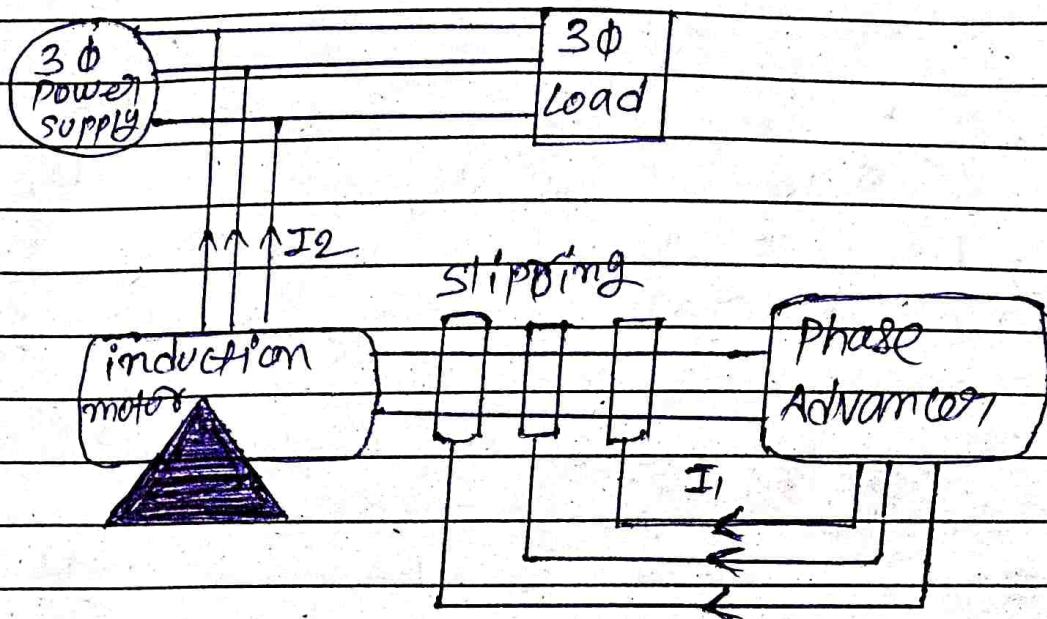
Here static capacitors are connected parallel with power supply, this static capacitor provides leading current and delivers reactive power to the inductive load thereby power factor is improved in system.

(2) Synchronous condenser :



When synchronous motor is connected to parallel with power supply, it provides leading current or reactive power to system thereby power factor improved in the system.

③ Phase advancer :-



Phase advancer is a device used in induction motor to improve their power factor. They are installed in the rotor circuit of the motor and provide additional excitation current to the rotor winding ~~and reduce reactive power~~ and improve the power factor. R

I_2

(PYQ)

Give concept of work and energy.

Ans $\Rightarrow$ Work $\rightarrow$ The concept of work is referred to the amount of energy that is transformed when a ~~force~~ force is applied over ~~distance~~ on an object to move ~~from one place to another place~~ from ~~one place to another place~~ is called work.

Energy $\div$ Energy refers to the ability of a system to perform work is called energy.

(PYQ)

Give Analogy between Electric and Magnetic circuits.

(1) Just as electric circuits have components like resistors, capacitors, inductors, that affect the flow of current.

Just like that

Magnetic circuits have components like magnetic cores, air gaps, coils that affects the flow of magnetic flux.

(2)

Just as electric circuits can be used to perform tasks like ~~transmitting~~ transmitting power or processing signals.

Just like that

Magnetic circuits ~~can~~ can be used to perform tasks like storing energy or controlling motion.

(Q.10) Explain how rotating magnetic field is produced? Give expression for its magnitude.

Ans $\Rightarrow$ A rotating magnetic field is produced when a set of coils carrying an alternative current is arranged in a specific way such that the magnetic fields generated by each coil combine together to create a rotating magnetic field.

$$B = B_m \sin(\omega t)$$

$$B = B_m \sin(2\pi f t)$$

where B is the magnitude of the magnetic field and B_m is the maximum magnitude of the magnetic field, ω is the angular frequency that is equal to two times of frequency and t is time.

DC ↓

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* diff b/w Node & Junction

node

Junction

- | | |
|--|---|
| <p>(i) node is a point in network where two or more circuits are joined.</p> | <p>Junction is a point where two or more three or more than three circuits are joined.</p> |
| <p>(ii) every junction can be a node.</p> | <p>(ii) every node cannot be a junction.</p> |
| <p>(iii) EX ⇒ A</p> | <p>EX ⇒ B</p> |

~~Define the concept of voltage and current~~

* Define the term phase splitting

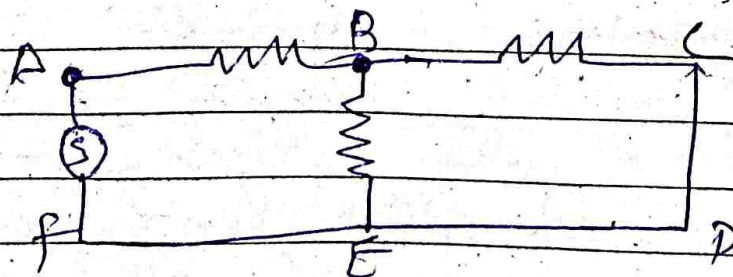
→ A device by which a single phase current is split into two or more currents differing in phase which is used to starting a single-phase inductor motor.

* diff b/w mesh and loop with example

mesh

loop

- | | |
|---|---|
| <p>(i) The loop which cannot be further divided is called mesh.</p> | <p>loop is the closed path of network is called loop.</p> |
| <p>(ii) mesh cannot exist in loop.</p> | <p>loop cannot exist in mesh mesh.</p> |
| <p>(iii) EX ⇒ ABCEFA</p> | <p>EX ⇒ ABCDEFA</p> |



DC circuits

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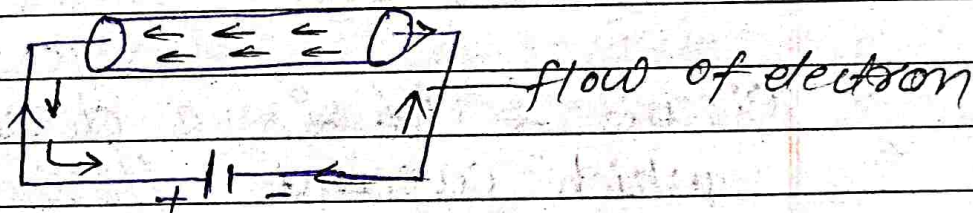
* Electricity ÷ The flow of electrons in a closed circuit to do work called electricity.

* Electric current ÷ The continuous movement of free electron in an electric circuit from -ve terminal of the cell to the +ve terminal through external circuit.

$$\text{Current} = \frac{q}{t} \Rightarrow \boxed{I = \frac{q}{t}} \text{ Amperes}$$

or

It is the rate of flow of electron or charge flowing per sec. is called electric current.



* Electric potential ÷ The capacity of a charged body to do work called electric potential.

$$V = \frac{\text{work done}}{\text{charge}} \Rightarrow \boxed{V = \frac{W}{Q}} \text{ volt}$$

(*) Ohm's law ÷ Keeping the physical condition & temperature of conductor as constant, current flowing between any two points of a conductor is directly proportional to potential difference across temperature.

$$I \propto V \Rightarrow \frac{V}{I} = \text{constant}$$
$$\boxed{V = IR}$$

* Limitation of ohm's law

- (i) This law is not applicable to non linear element such as electric arc, powdered carbon, th. etc.
- (ii) this law is not applicable to unilateral networks such as electronic tubes & diode.

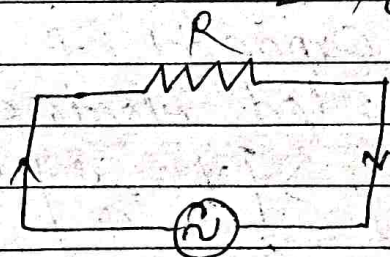
* Electric power $\div$ The rate at which work is done in an electrical circuit

$$P = \frac{\text{work done}}{\text{Time}} \quad P = \frac{VI}{t} \quad [P = VI] \text{ watt}$$

$$[P = \frac{W}{t}] \quad W = VQ \Rightarrow W = VIt$$

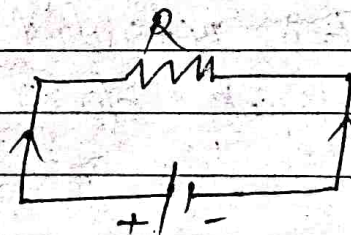
* circuit $\div$ It is a closed path through which current flow

2 types



AC

$f = 50 \text{ Hz}$



DC

V & I constant

* linear element $\div$ Linear elements are the elements that show a linear relationship between voltage and current $\Rightarrow$ Resistor, inductor

$\rightarrow$ The circuit containing only linear resistors are called linear circuits.

* Non linear element $\div$ Non-elements are those that do not show a linear relation between voltage and current.

Ex $\Rightarrow$ ~~gas~~ gas diode, electric arc, inductor

$\rightarrow$ The circuit containing non linear element are called non linear circuit.

Ex $\Rightarrow$ Transistor etc

* Unilateral circuit $\div$ An electric circuit whose characteristic properties change with the direction of its operation.

Ex $\Rightarrow$ diode

* unilateral circuit $\div$ unilateral circuit are those circuit which allows the current to flow only ~~in~~ in one direction

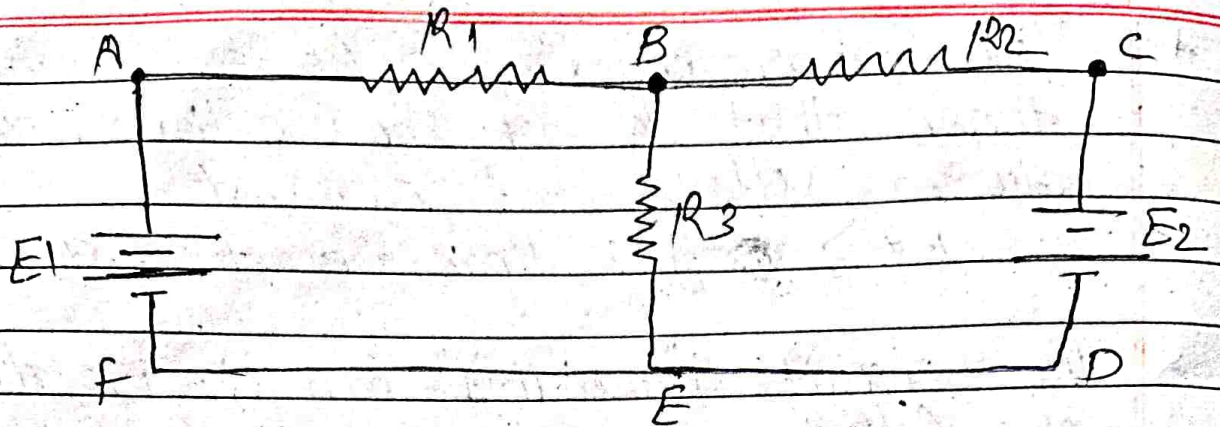
Ex diode

* bilateral circuit $\div$ bilateral circuit are those circuit which allows the current flow in both direction.

* active element $\div$ Those element which supplies energy to circuit is called active element.

$\Rightarrow$ Network having active element is called active network Ex $\Rightarrow$ DC or AC source

* Passive element $\div$ Those element which receives energy are called passive element.



* **Node** ÷ A node is a point in network where two or more circuit are joined
Ex = A, B, C, D

* **Junction** ÷ A junction is a point in the network where 3 or more element joined
eg, B

* **Loop** ÷ the closed path of network is called loop. → ABEFA

* **Mesh** ÷ The loop which can't be further divided is called mesh.
Ex → ABEFA, BCDEB

electric

* **Resistance** ÷ Resistance is a measure of opposition of current flow in an electrical circuit.
 $R = \frac{\rho l}{A}$ Ohm → unit
factors depend (i) length of wire
(ii) area of wire
(iii) ρ or ρ

$$P = \frac{V^2}{R}$$

$$H = I^2 R t$$

* **Inductance** ÷ It is the property of a material by the virtue of which a change in electric current through it induces emf in conductor.

$$V = L \frac{di}{dt} \quad i^0 = \frac{1}{L} \int V dt + i^0$$

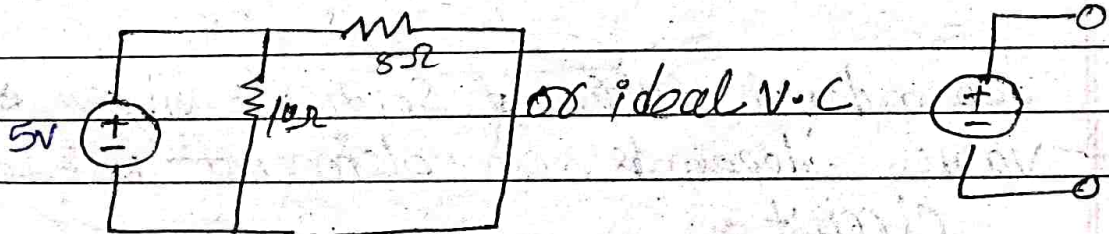
* Capacitance ÷ The capability of an element to store electric charges within it.

$$C = \frac{Q}{V} \quad U = \frac{1}{2} CV^2$$

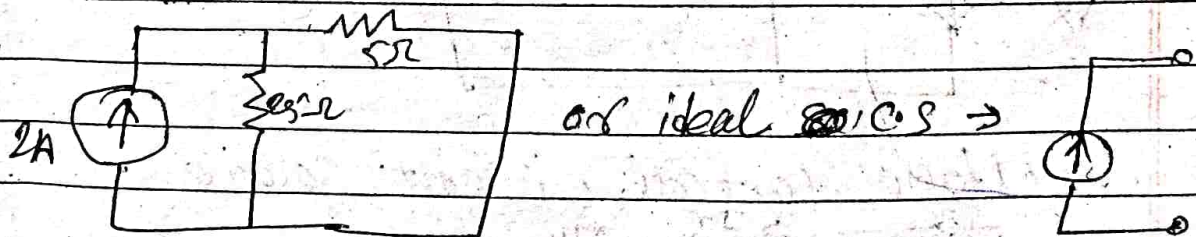
* Voltage and current sources / Energy source

(1) Independent Sources

(i) independent voltage source ÷ whose voltage value does not depend on element present in the circuit.



(ii) Independent current source ÷ whose current value does not depend on element present in circuit.



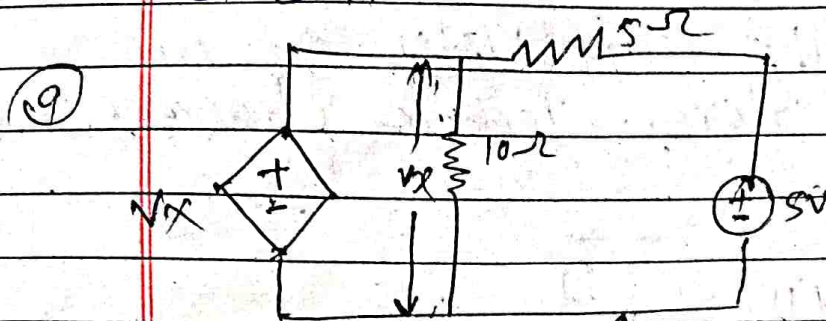
(2) Dependent sources

(i) dependent voltage sources

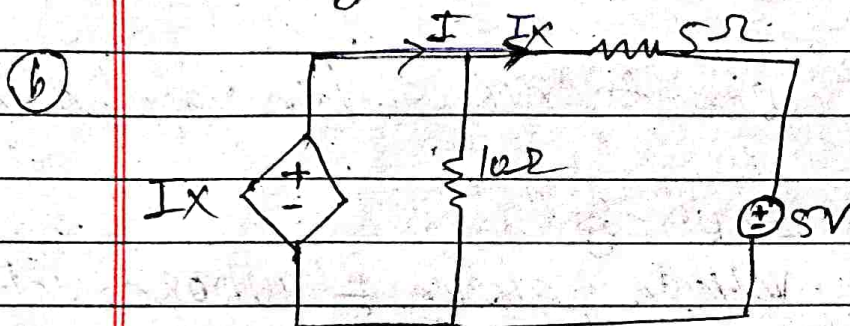
(ii) dependent current sources

dependent voltage sources voltage control voltage source
current control voltage source

- (i) dependent voltage source: whose voltage value depends on element present in circuit.

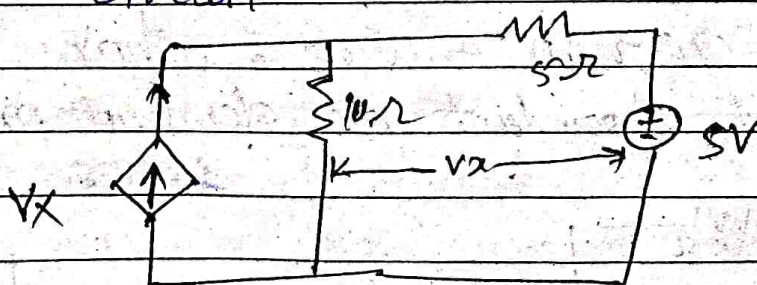


Voltage Control Voltage Source

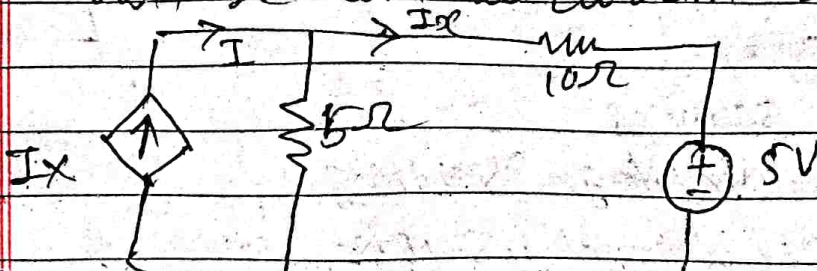


Current Control voltage source

- (ii) dependent current source: whose ~~voltage~~ current value depends on element present in circuit.

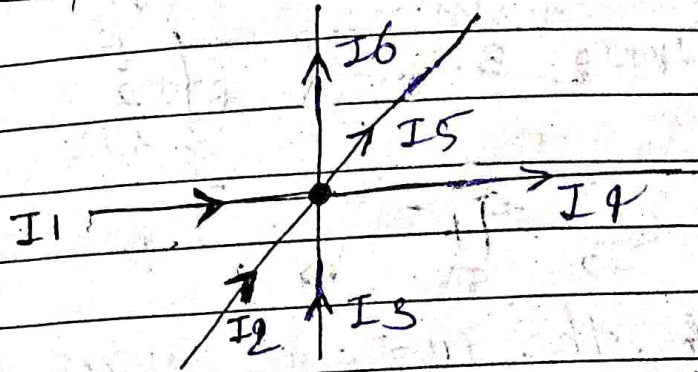


(a) Voltage Control current source



(b) Current Control current source

* **Kirchhoff current law** ÷ The algebraic sum of all current meeting at a junction or a point is ~~zero~~ equal to zero.



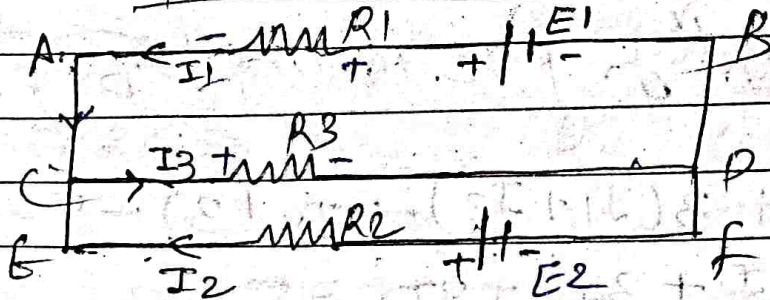
$$I_1 + I_2 + I_3 - (I_4 + I_5 + I_6) = 0$$

$$\sum I = 0$$

* **Kirchhoff's voltage law** ÷ It states that the algebraic sum of all the voltage and Emf in a closed loop is equal to zero.

$$\sum E + \sum V = 0$$

$$\sum E + \sum IR = 0$$



Apply KVL rule in mesh ~~ACDBA~~ ACDBA

$$I_1 R_1 + I_3 R_3 - E_1 = 0$$

$$I_1 R_1 + I_3 R_3 = E_1$$

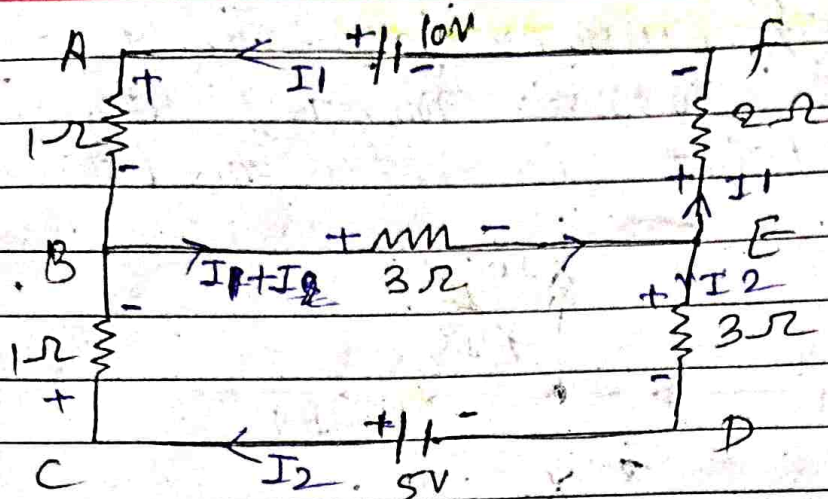
Apply KVL in mesh CEFC

$$I_2 R_2 + I_3 R_3 - E_2 = 0$$

$$I_2 R_2 + I_3 R_3 = E_2$$

Numerical on KVL

*



Calculate the current in each branch.

Apply KVL in first mesh ABEFA

$$I_1 \times 1\Omega + 3\Omega(I_1 + I_2) + 2\Omega(I_1) - 10V = 0$$

$$I_1 + 3I_1 + 3I_2 + 2I_1 = 10$$

$$6I_1 + 3I_2 = 10 \quad \text{--- (A)}$$

again apply KVL in mesh BCDEB

$$I_2 + 3(I_1 + I_2) + I_2(3) - 5 = 0$$

$$I_2 + 3I_1 + 3I_2 + 3I_2 = 5$$

$$3I_1 + 7I_2 = 5 \quad \text{--- (B) } \times 2$$

Solving eq A and B

$$6I_1 + 3I_2 = 10$$

$$6I_1 + 14I_2 = 10$$

$$-11I_2 = 0$$

$$I_2 = 0$$

put in (A)

$$6I_1 + 3(0) = 10$$

$$I_1 = \frac{10 \times 5}{6 \times 3}$$

$$I_1 = \frac{5}{3}$$

$$I_2 = I_1 + I_2$$

$$I_2 = 5/3$$

* Network $\div$ A network is Collection of interconnected components (resistor, capacitor)

Network Theorem

- (i) Superposition Theorem
- (ii) Norton Theorem
- (iii) Thevenin Theorem

* Superposition Theorem $\div$

* Current division Method $\div$

$$I_x = I_T \times \frac{\text{Res's of opp branch}}{\left(\text{Res's of opp branch} + \text{Res's of current branch} \right)}$$

* Voltage division Method

$$V_x = \frac{R_x}{R_T} \times V(\text{input})$$

$$R_S = R_1 + R_2 + R_3$$

$$R_P = \frac{R_1 \cdot R_2}{R_1 + R_2}$$

* Superposition theorem : If a number of voltage and current source are acting in a linear network then the resulting current in each branch is the algebraic sum of all the currents that would be produced in it, and other source will be replaced by open and ~~else~~ short-circuit.

Procedure :

(i) Consider one source at a time & other source are removed.

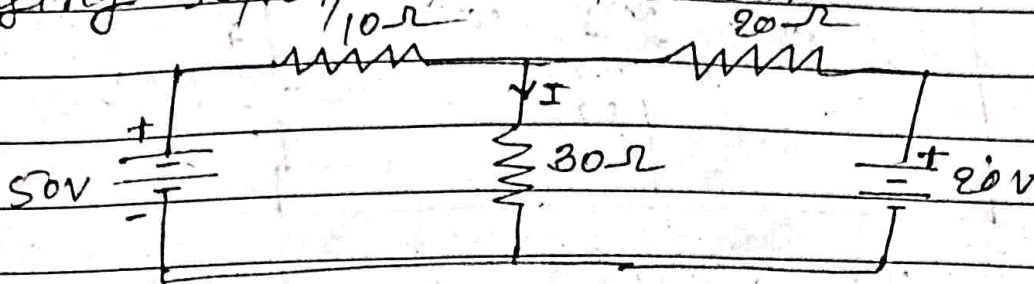
Note : voltage source $\rightarrow$ short circuit
current source $\rightarrow$ open circuit

(ii) Current is calculated in each require branch due to single source.

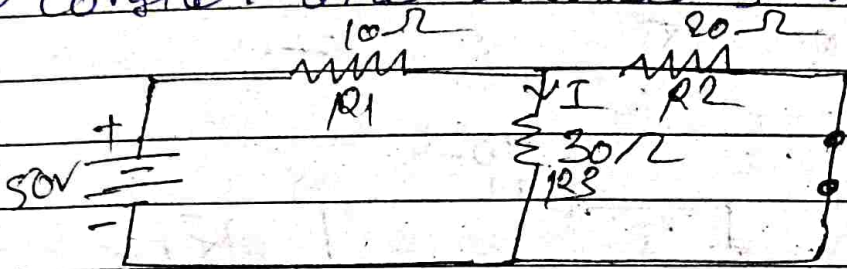
(iii) Repeat this process for other source at a time.

(iv) finally calculate the algebraic sum of all the currents ~~in a required branch~~ that produced in each branch.
~~by the help of current division rule~~

* find current I for the circuit shown by using superposition theorem.

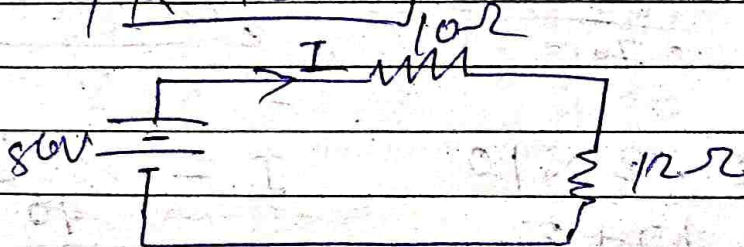


Step - 1 $\rightarrow$ consider one source 50V at a time



$$R = \frac{R_2 \times R_3}{R_2 + R_3} = R = \frac{20 \times 30}{50} = \frac{600}{50} = 12$$

$$\boxed{R = 12 \Omega}$$



$$R_B = 10 + 12 = 22 \Omega$$

$$R_{\text{Total}} = 22 \Omega$$

from ohm law $\boxed{V = IR}$

$$I = \frac{V}{R} \quad I_T = \frac{50}{22} \quad I_T = \frac{25}{11}$$

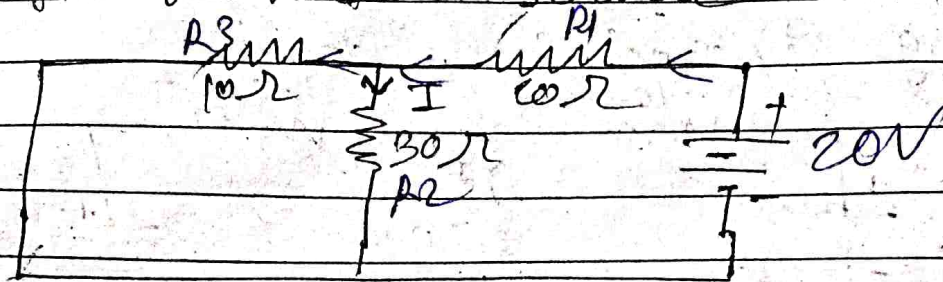
$$\boxed{I_T = 2.27 \text{ A}}$$

$\therefore$ from current division method

$I_1 = I_T \times \frac{\text{opp. of current (resis of opp. branch)}}{\text{opp. resi + res of cur branch}}$

$$I_1 = \frac{2.27 \times 20}{20 + 30} \Rightarrow I_1 = 0.908 \text{ A}$$

Config'd by another source 20V

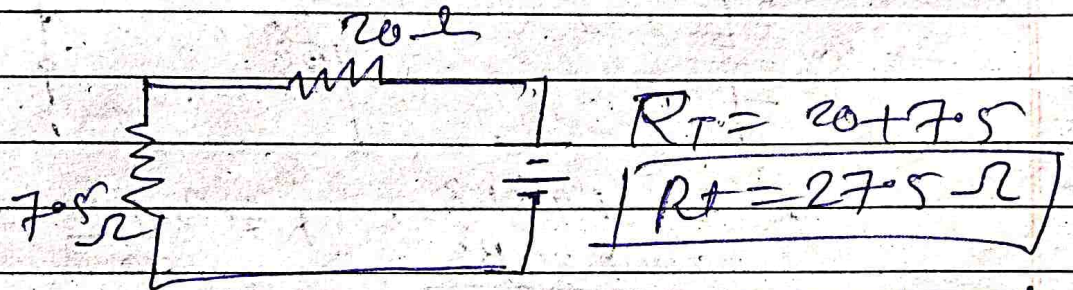


$$R = \frac{R_3 \times R_2}{R_2 + R_3}$$

$$R = \frac{20 \times 10}{40} = \frac{300}{40}$$

$$R = \frac{15}{2}$$

$$R = 7.5 \Omega$$



$$I = \frac{20}{27.5} \Omega = \boxed{I = 0.72 A}$$

$$I = \frac{0.72 \times 10}{10 + 30}$$

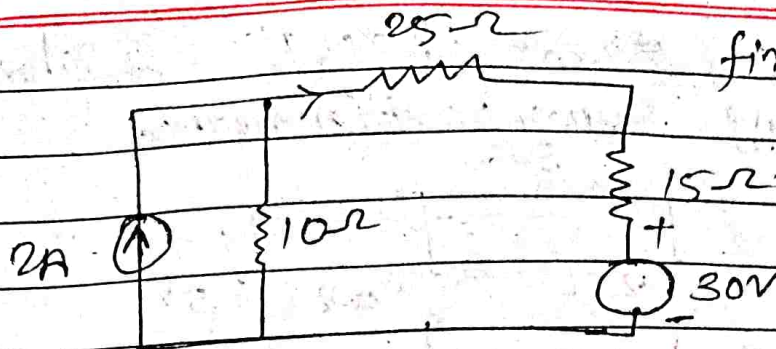
$$I = \frac{7.2}{40}$$

$$\boxed{I_2 = 0.18 A}$$

total current flow from I

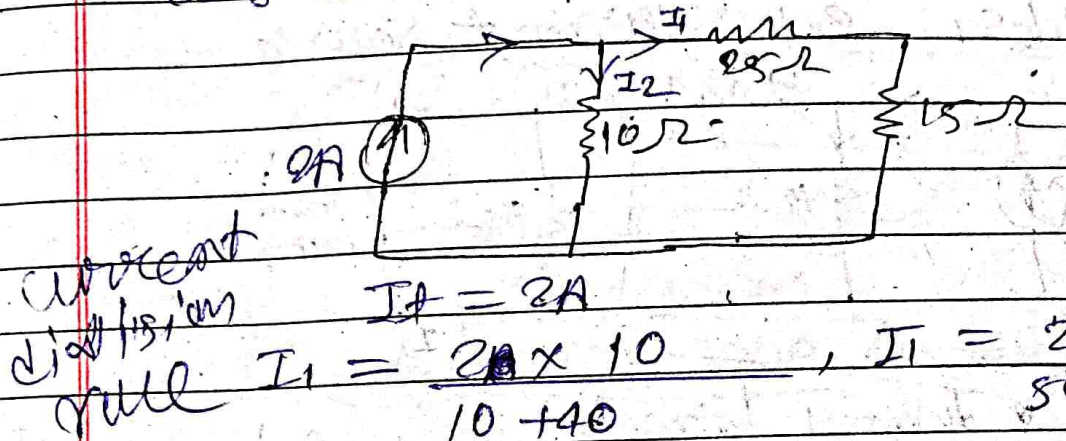
$$I = I_1 + I_2 \Rightarrow I = 0.18 + 0.908$$

$$\boxed{I = 1.088 A}$$

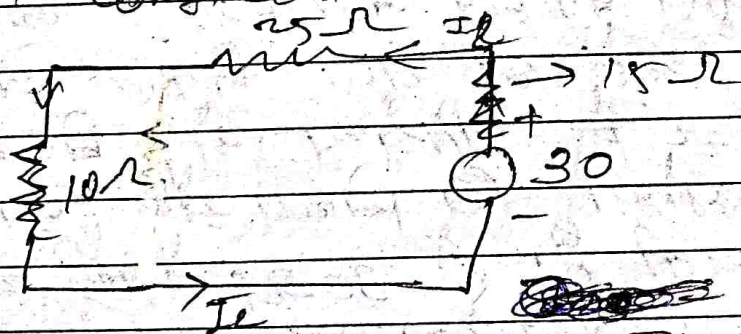


find current from
25 ohm resistor

consider 2A DC source



again consider 30V source



$$R_T = 50 \Omega$$

$$I_2 = \frac{30}{50} \quad \boxed{I_2 = 0.6}$$

$$\boxed{I_{25} = 0.6}$$

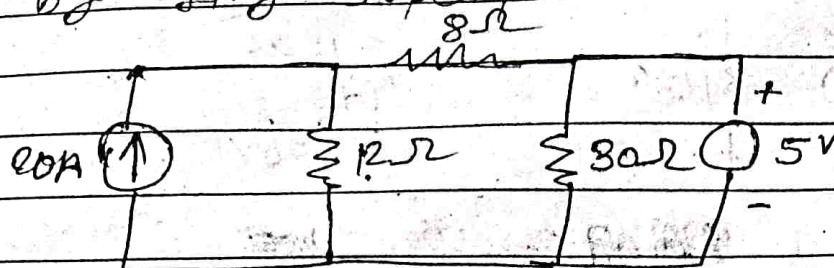
$$I = I_{25} - I_1$$

$$I_{25} = I_2 - I_1$$

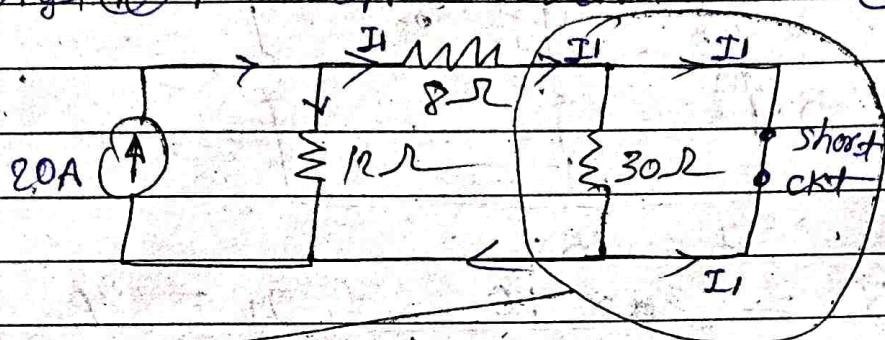
$$I_{25} = 0.6 - 0.4$$

$$\boxed{I_{25} = 0.4 \text{ A} (\leftarrow)}$$

* find the current through $8\ \Omega$ resistor by using superposition method

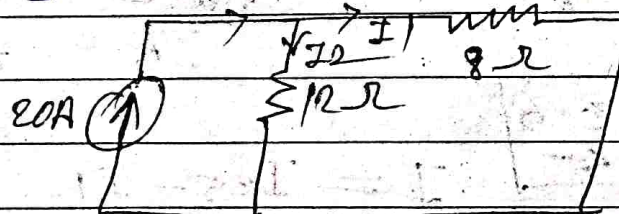


Step-1 $\rightarrow$ Consider $20A$ current source



dimmy branch

को चारा प्रवाहित नहीं होगा क्योंकि जो short पक है उसे ही चारा निकल जाएगा बिना $30\ \Omega$ के प्रतिरोध से निकले बिना कधोका चारा हमेशा सिचा और आसान मार्ग चुंचती है। तो $30\ \Omega$ से कोई चारा नहीं जाएगा

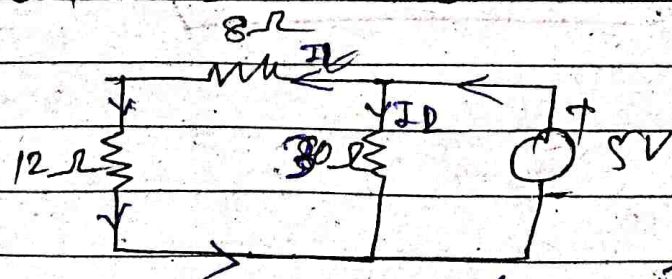


$$I_x = I \times \frac{\text{opp Res}}{\text{opp Res} + \text{Res of current}}$$

$$I_1 = \frac{20 \times 12}{12 + 8}$$

$$I_1 = \frac{240}{20} \quad (I_1 = 12A) \quad (\rightarrow)$$

Step-2 $\rightarrow$ Consider $5V$ voltage source



$$I_2 = \frac{20 \times 80}{20 + 30} \quad I_3 = \frac{600}{80} \quad I_3 = 7.5A$$

$$I_4 = \frac{5}{12} \quad I_4 = 0.416$$

by current divider rule

$$I_2 = I_1 \times \frac{\text{res of oppb}}{\text{res of oppb} + \text{res of currb}}$$

~~$$I_2 = \frac{12 \times 30}{20 + 30} \quad I_2 = \frac{360}{50} \quad I_2 = 6.12$$~~

$$I_2 = \frac{0.916 \times 30}{30 + 20}$$

$$I_2 = \frac{12.48}{50}$$

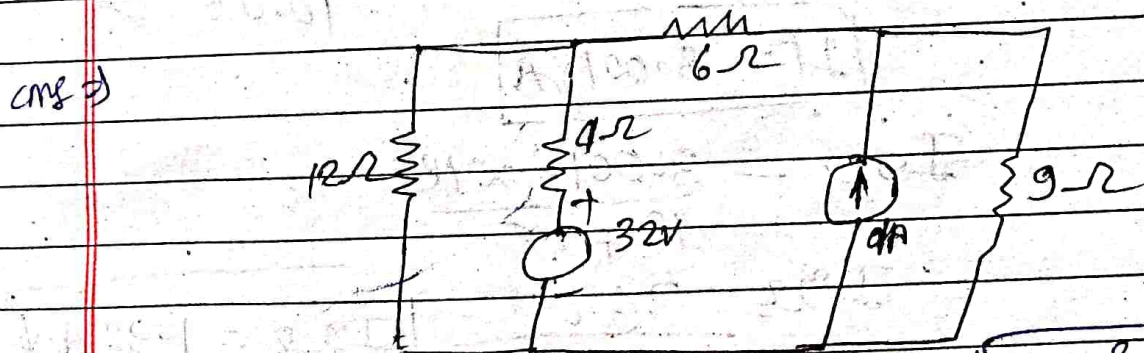
$$I_2 = 0.2496 \text{ A} \quad (\leftarrow)$$

$$I_{8\Omega} = I_1 - I_3$$

$$I_{8\Omega} = 12 - 0.249$$

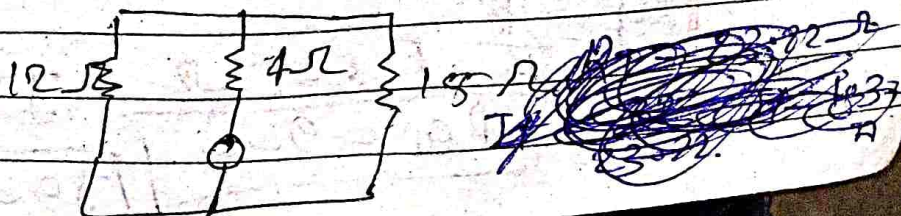
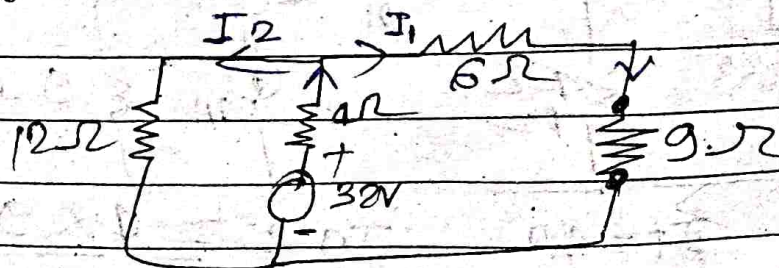
$$I_{8\Omega} = 11.751 \text{ A} \quad (\rightarrow)$$

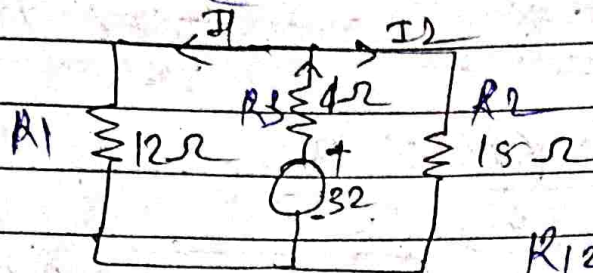
* find the power dissipated across 9Ω resistance by using superposition theorem



$$\therefore P = VI, \quad P = I^2 R$$

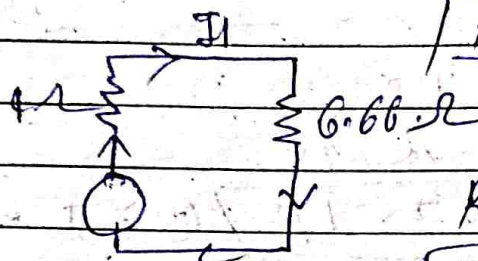
Consider 32V Voltage source.





$$R_{12} = \frac{12 \times 15}{12 + 15}$$

$$R_{12} = 6.66 \Omega$$



$$R_T = 6.66 + 4$$

$$R_T = 10.66 \Omega$$

$$I_1 = \frac{4}{10.66}$$

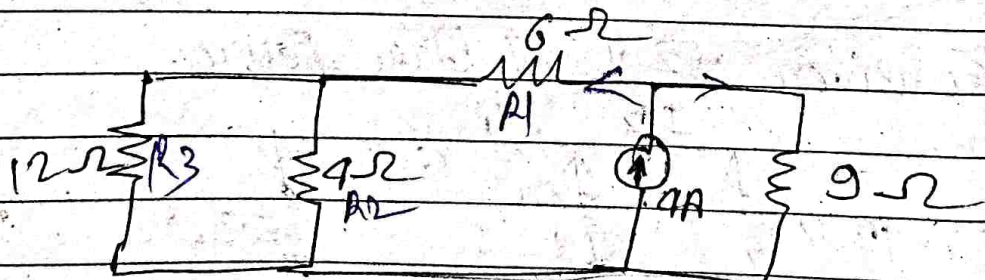
$$I_1 = 3.0018 \text{ A}$$

$$I_{9\Omega} = \frac{3.0018 \times 12}{12 + 15}$$

$$I_{9\Omega} = \frac{36.022}{27}$$

$$I_{9\Omega} = 1.33 \text{ A} \downarrow$$

Consider 4A current source



$$I_1 = 4 \text{ A}$$

$$I_{9\Omega} = \frac{4 \times 9}{9 + 9}$$

$$R_{23} = \frac{12 \times 4}{12 + 4}$$

$$R_{23} = 3 \Omega$$

$$I_{9\Omega} = \frac{36}{18}$$

$$R_{eq} = 9 \Omega$$

$$I_{9\Omega} = 2 \text{ A} \downarrow$$

$$I_{9\Omega} = 2 + 1.33A$$

$$\boxed{I_{9\Omega} = 3.33A} \downarrow$$

So power dissipated across 9Ω

$$P = I^2 R \quad P = (3.33)^2 \times 9$$

$$P = 9.99 \times 9$$

$$\boxed{P = 99.98 \text{ W}}$$

* Obtain the power dissipation in 10Ω resistor using

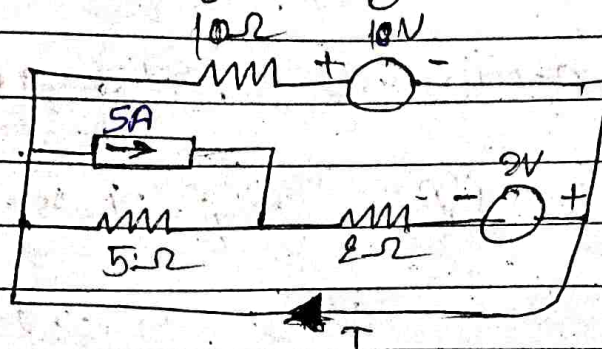
Hard

don't do this ↓

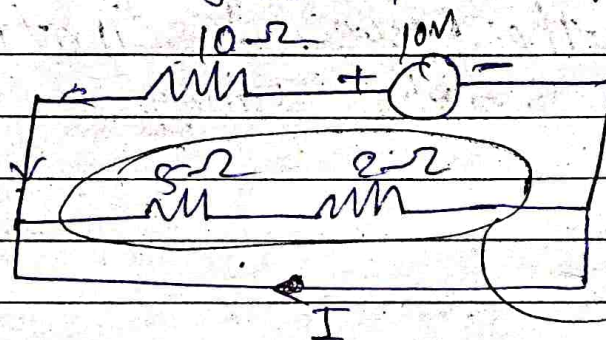
Page No.

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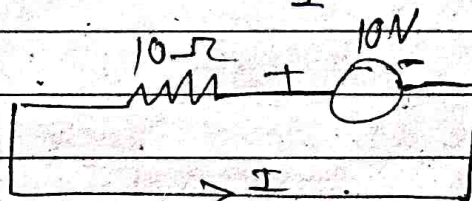
* find the current 'I' for the circuit shown below by using superposition theorem



Step-1 → Consider 10V voltage source



dummy current

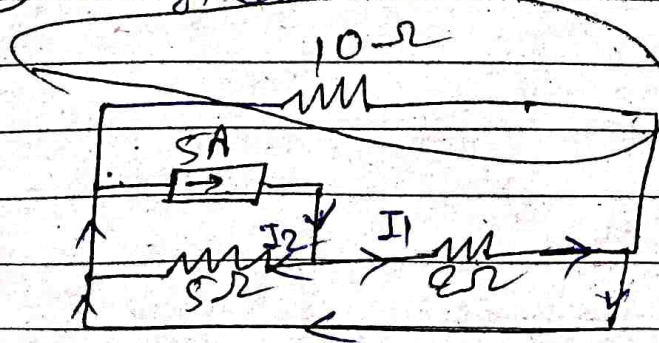


$$R_T = 10 \quad I_t = \frac{10}{10}$$

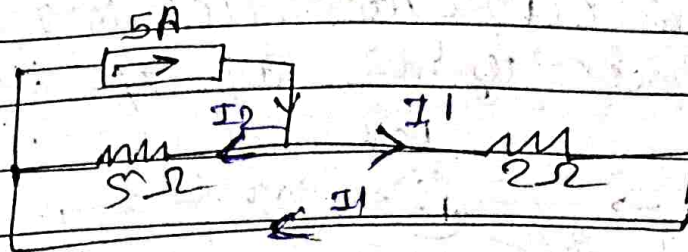
$$I_t = 1$$

$$I_1 = 1$$

Step ② Consider 5A current source



dummy current



$$I = 5A$$

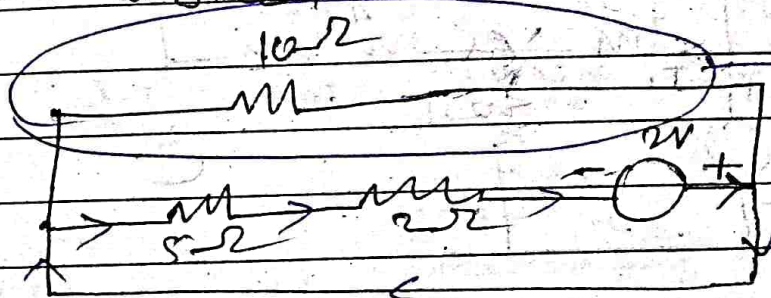
by current division

$$I_1 = \frac{5 \times 5}{5 + 2}$$

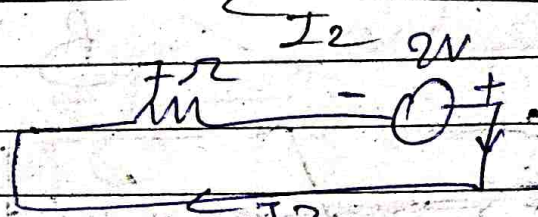
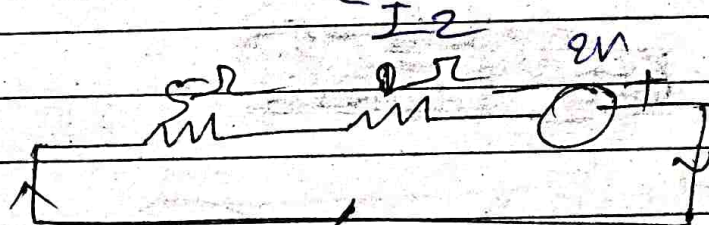
$$I_1 = \frac{25}{7}$$

$$I_1 = 3.5A$$

Step-3 → Consider 2V voltage source



dummy current



$$I = \frac{2}{7}$$

$$I = 0.285A$$

$$I_2 = 0.285A$$

Total current through I

$$I = I_1 + I_2 + I$$

$$I = 3.5 + 0.28 + 0.28$$

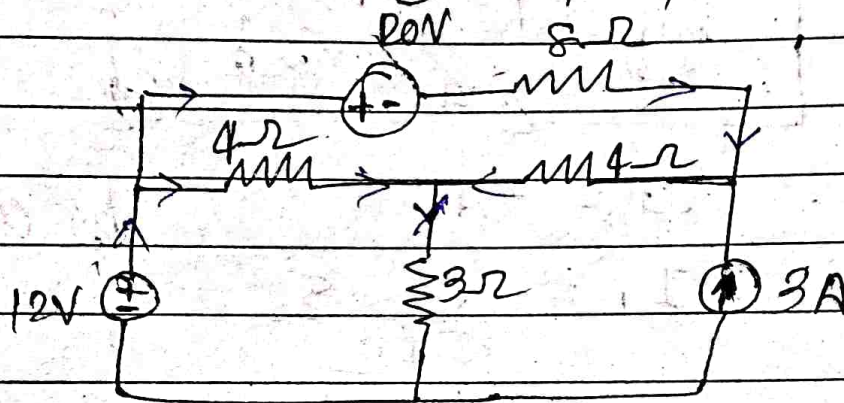
$$I = 4.06A$$

dom1st do this

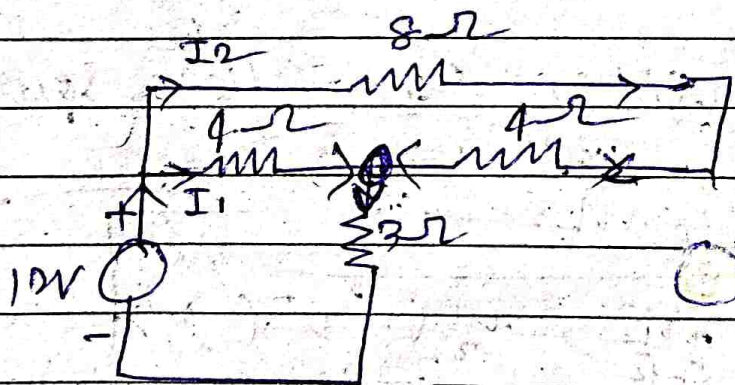
Page No.

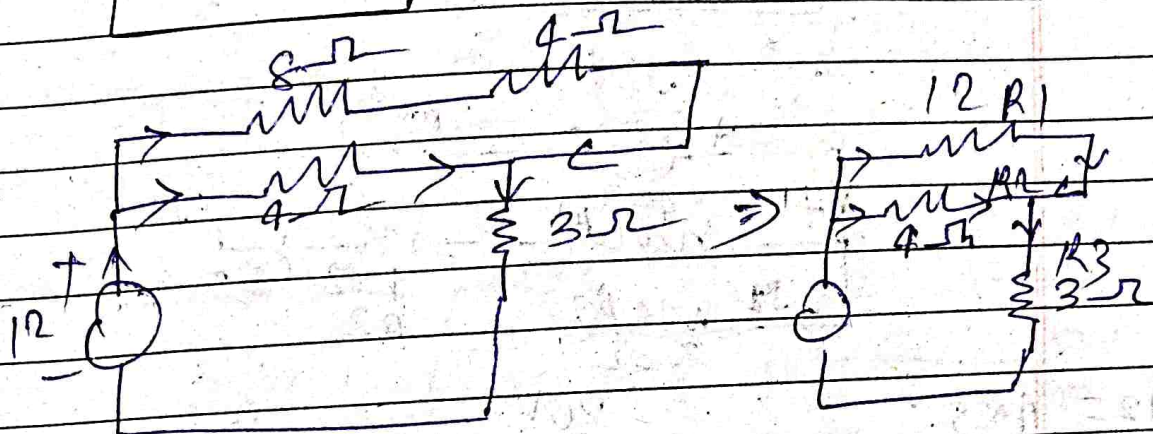
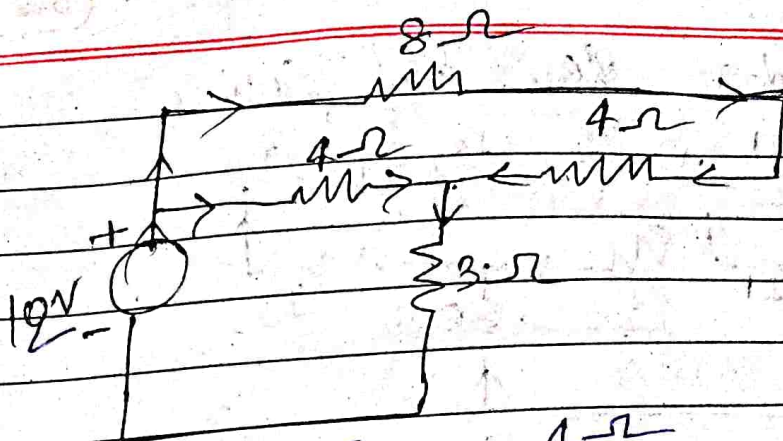
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find the current flowing through 3 ohm resistor using superposition theorem

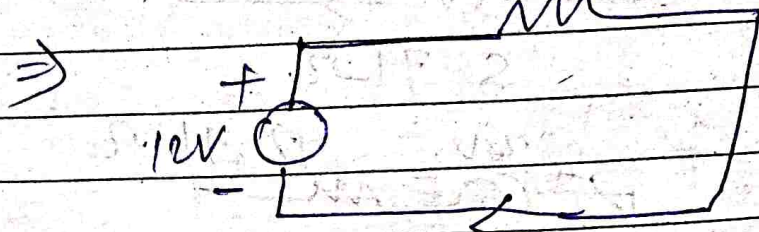
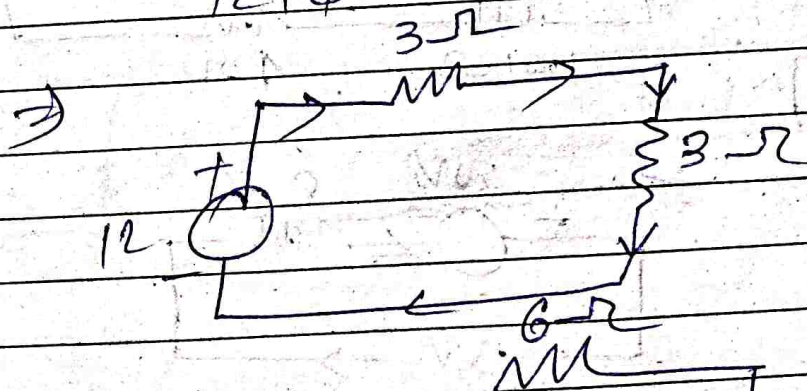


Step-1 $\rightarrow$ Consider 12V voltage source





$$R_{12} \Rightarrow \frac{12 \times 4}{12 + 4} = \frac{48}{16} = 3\Omega$$



$$I_T = \frac{12}{6}$$

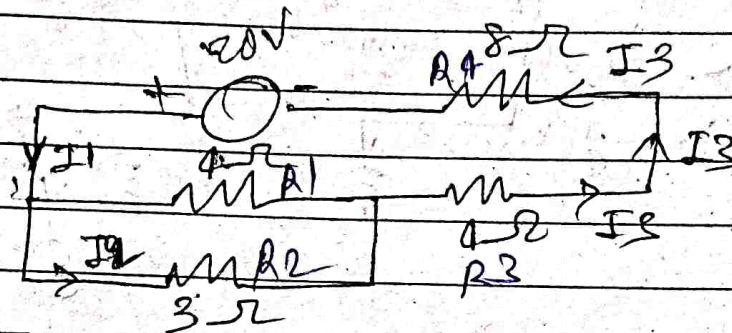
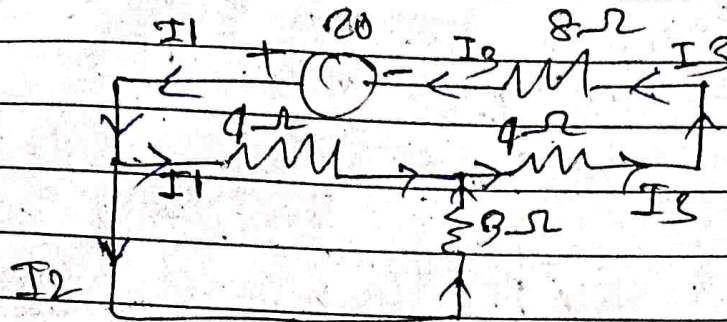
$$I_T = 2A$$

~~$$I_{3\Omega} = 2A$$~~

$$I_{3\Omega} = 2A$$



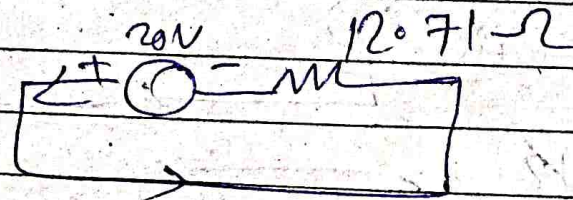
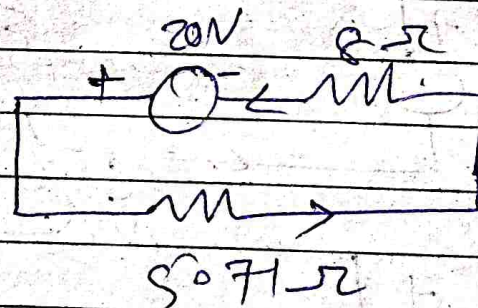
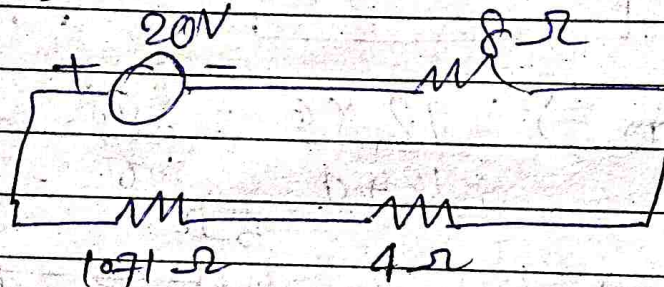
Comfide27 20V Vol Source



$$R_{12} = \frac{4 \times 3}{4 + 3}$$

$$R_{12} = \frac{12}{7}$$

$$R_{12} = 1.71 \Omega$$



$$I = \frac{20}{12.71} \quad I_T = 1.57 A$$

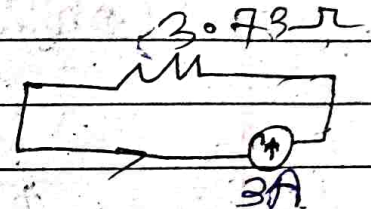
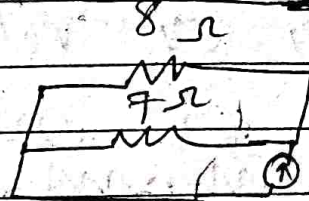
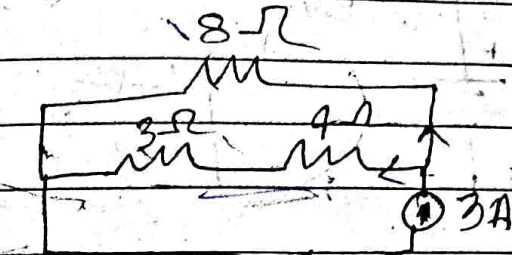
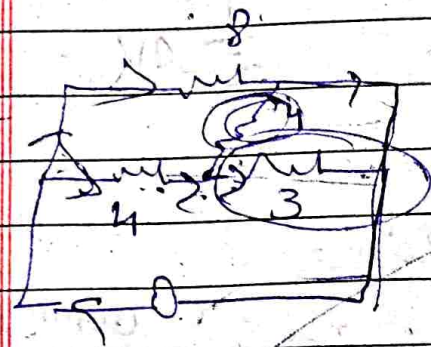
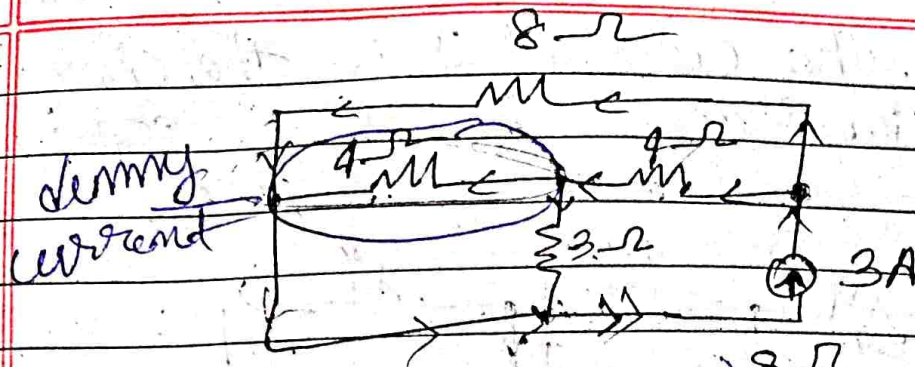
$$I_3 = \frac{20}{3}$$

$$I_{3n} = 6.66 A$$

Consider 3A current source.

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$$\rightarrow \frac{8 \times 7}{15} = \frac{56}{15} = 3.73 \Omega$$

$$V = IR$$

$$V = 3 \times 3.73$$

$$V = 11.19 \text{ V}$$

$$I = \frac{V}{R}$$

$$\frac{8 \times 7}{15} = \frac{56}{15}$$

$$R = 3.73$$

$$I = \frac{11.19}{3.73}$$

$$I_{3\Omega} = \text{A}$$

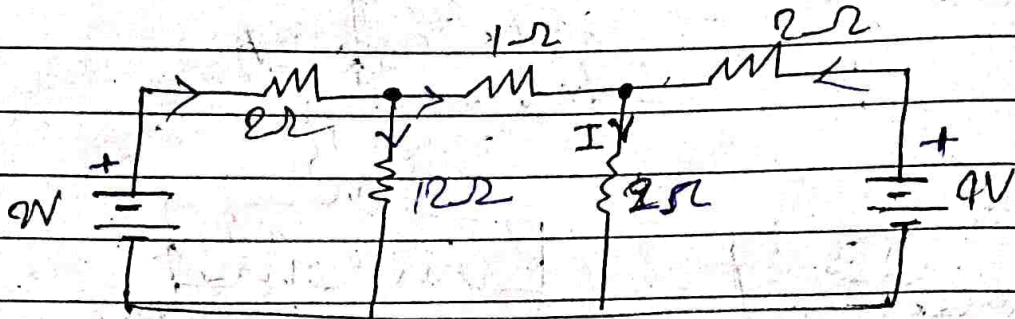
$$I_{3\Omega} = 3A$$

$$I = \cancel{3A} + 2A + (-6.66)$$

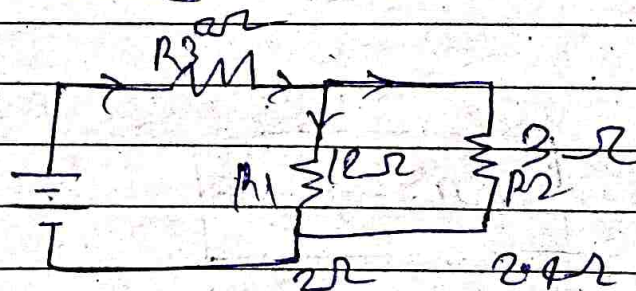
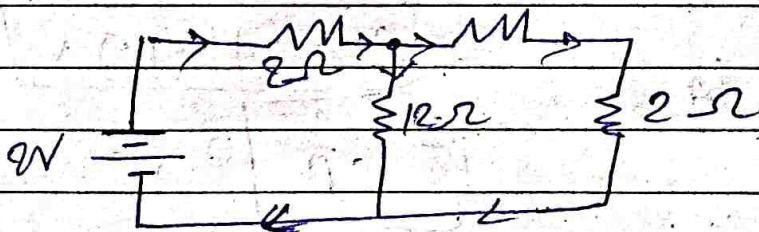
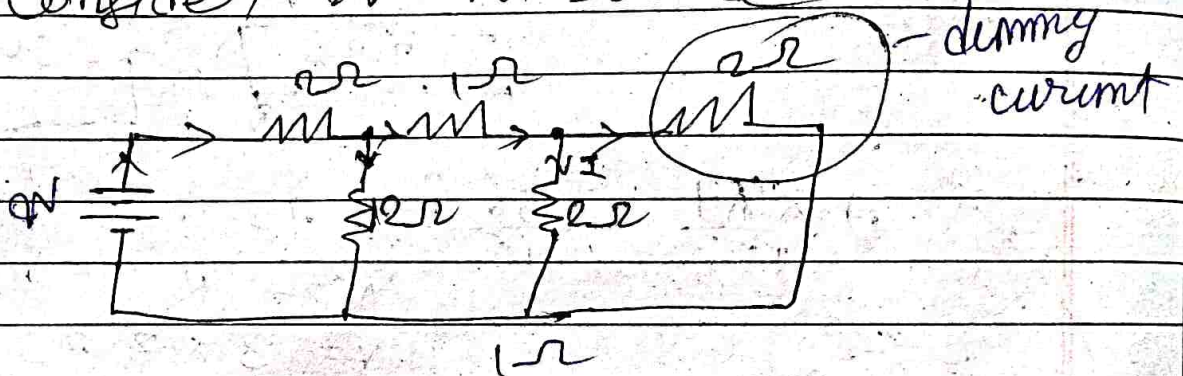
$$I = -1.66A$$

*

Calculate the current I in the circuit show in figure 1 by using superposition theorem.



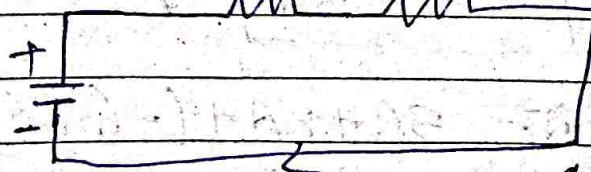
Consider $9V$ source



$$R_{12} = \frac{12 \times 2}{15}$$

$$R_{12} = \frac{36}{15}$$

$$R_{12} = 2.4 \Omega$$



$$I_L = \frac{2}{4.4}$$

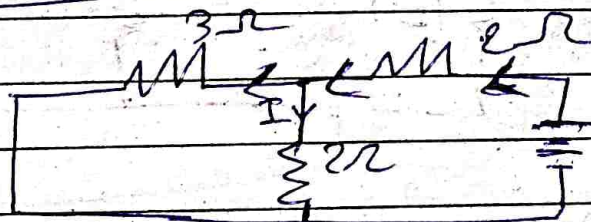
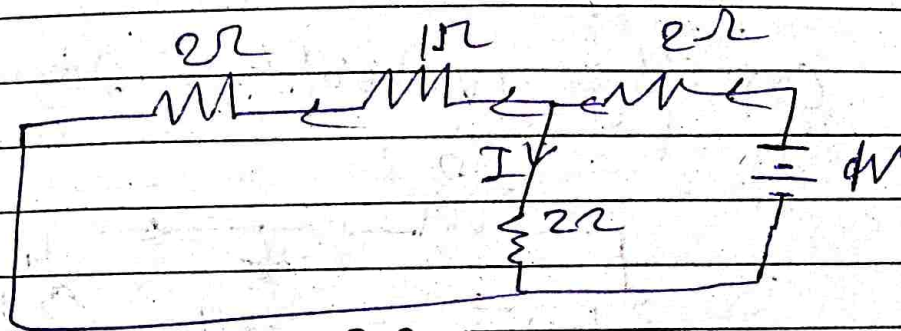
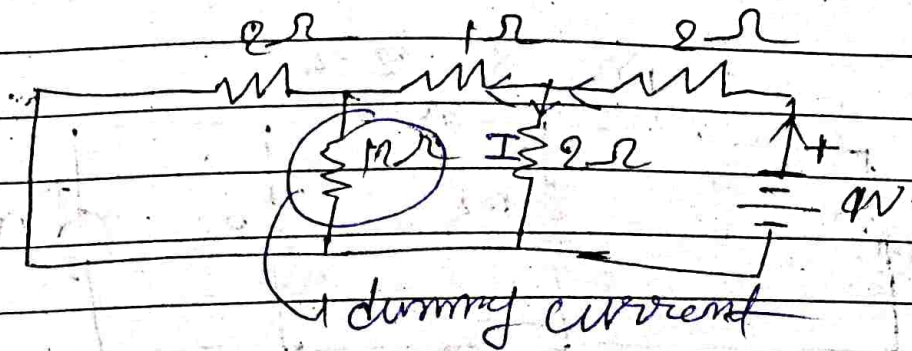
$$I_L = 0.45A$$

$$I_D = \frac{0.45 \times 2}{2 + 2}$$

$$I = \frac{0.9090}{4}$$

$$I = 0.22A$$

Consider 4V Vol source



$$\frac{3R}{3+R}$$

$$= \frac{6}{5}$$

=

$$I_t = \frac{4}{3.2}$$

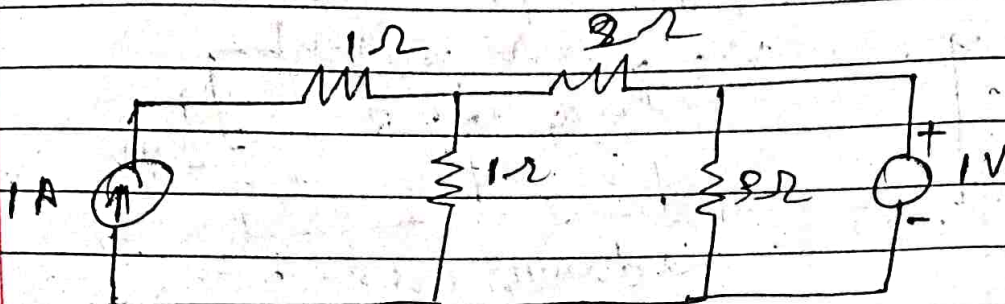
$$I_t = 1.25 \text{ A}$$

$$I_t = \frac{1.25 \times 1}{1+2}$$

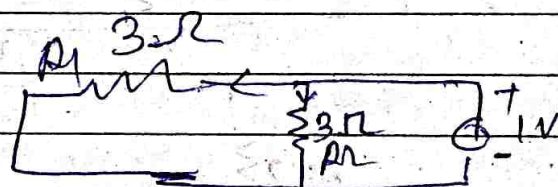
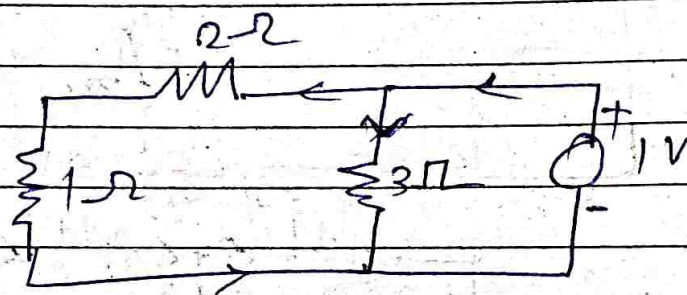
$$I_t = 0.416 \text{ A} \quad (\downarrow)$$

$$\text{Total } I = 0.636 \text{ A} \quad (\downarrow)$$

* find current through 2Ω resistor in the circuit as shown in figure

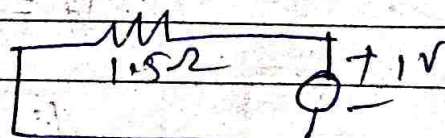


consider 1V voltage current



$$R_{12} = \frac{3 \times 3}{3 + 3} \Rightarrow \frac{9}{6} = \frac{3}{2}$$

$$R_{12} = 1.5\Omega$$



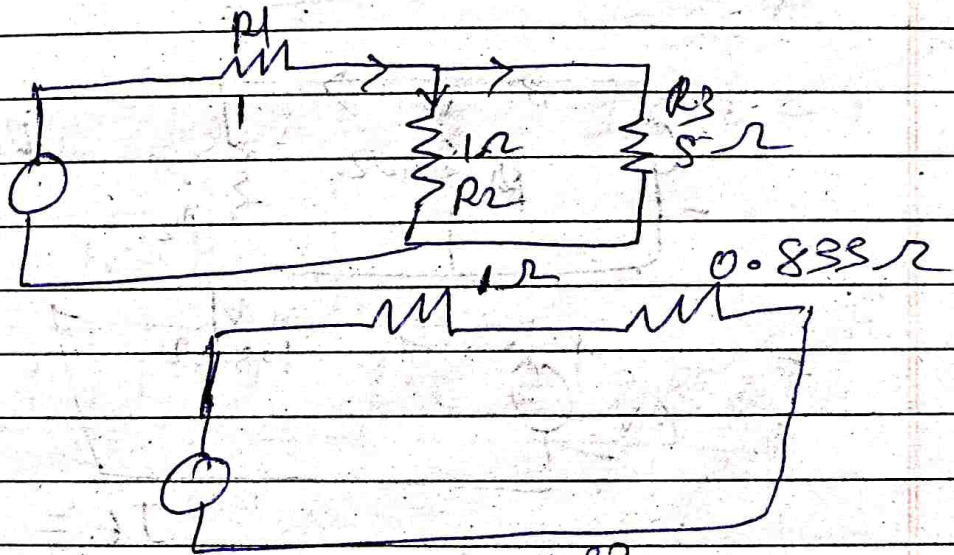
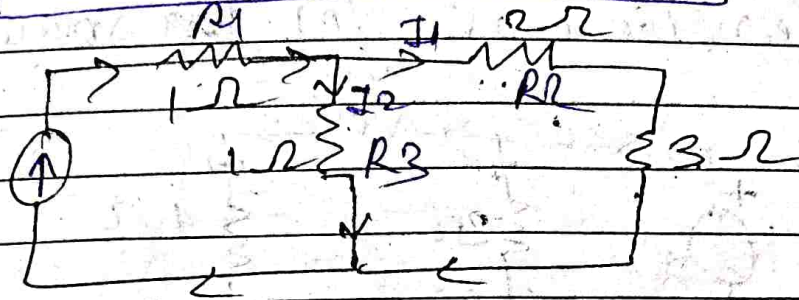
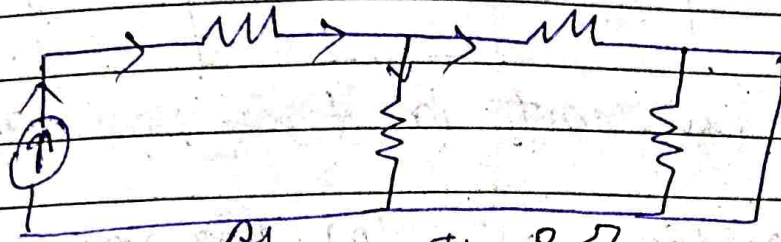
$$I_t = \frac{1}{1.5}$$

$$I_t = 0.66A$$

$$I_{2\Omega} = \frac{0.66 \times 3}{3 + 2}$$

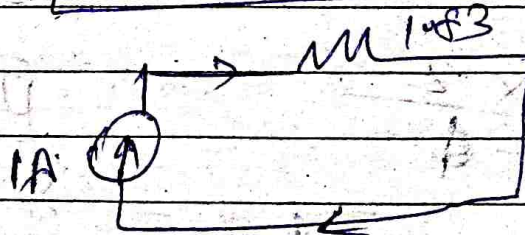
$$I_{2\Omega} = 0.39A$$

Consider 1 A current ~~voltage~~ source



$$R_{eq} = \frac{5}{1+5}$$

$$= \frac{5}{6}$$



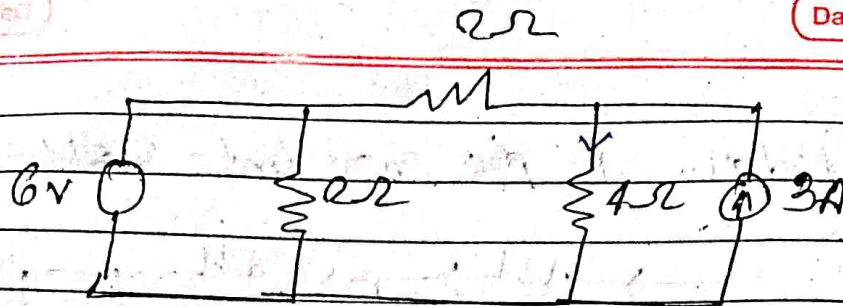
$$I = 1A \quad I_2 R = \frac{1 \times 5}{2+1} \quad I_2 R = \frac{5}{3}$$

~~$$I_2 = 1A$$~~

~~$$I = 0.67A$$~~

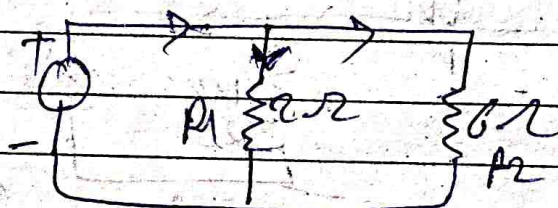
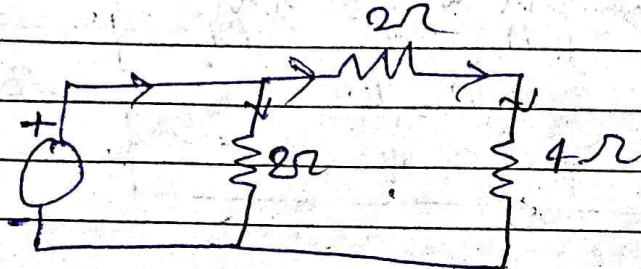
$$I_2 = 0.33A$$

$$I = 0.06A \quad (\oplus)$$



the current in 4Ω resistance using sp

Consider 6V vol source



$$R_{12} = \frac{6 \times 2}{6 + 2}$$

$$R_{12} = \frac{12}{8}$$

$$R_{12} = 1.5\Omega$$

$$I_t = \frac{6}{1.5}$$

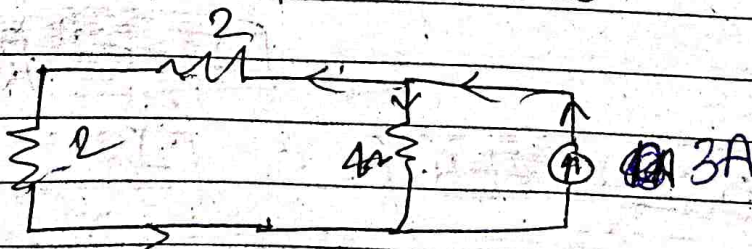
$$I_t = 4A$$

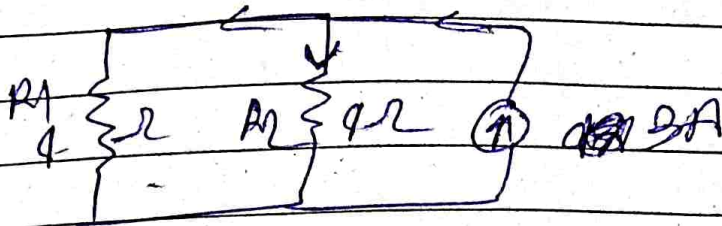
$$I_{4\Omega} = \frac{4 \times 2}{2 + 4}$$

$$I_{4\Omega} = \frac{8}{6}$$

$$I_{4\Omega} = 1.33A$$

Consider 3A current





$$R_{12} = \frac{4 \times 4}{4 + 4}$$

$$R_{12} = \frac{16}{8}$$

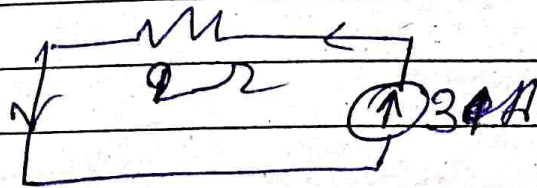
$$R_{12} = 2\Omega$$

$$V = IR$$

$$V = 6$$

$$I = \frac{6}{2}$$

$$I = 3A$$



$$I_t = 4A$$

$$I_{4\Omega} = \frac{3A \times 2}{2 + 4}$$

$$I_{4\Omega} = \frac{6}{6}$$

$$I_{4\Omega} = 1$$

$$I_{4\Omega} = 1.33A \downarrow$$

$$I = 1 + 1.33$$

$$I = 2.33A$$

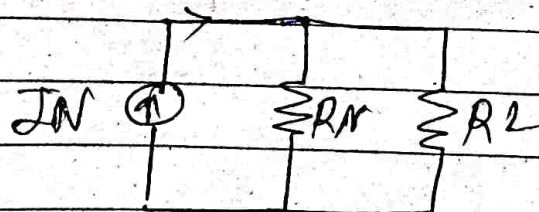
* **Norton Theorem** : Any linear network consisting a number of voltage sources and resistance can be replaced by an equivalent network having a single current source (I_N) and single resistance (R_N) and single load terminal.

Procedure

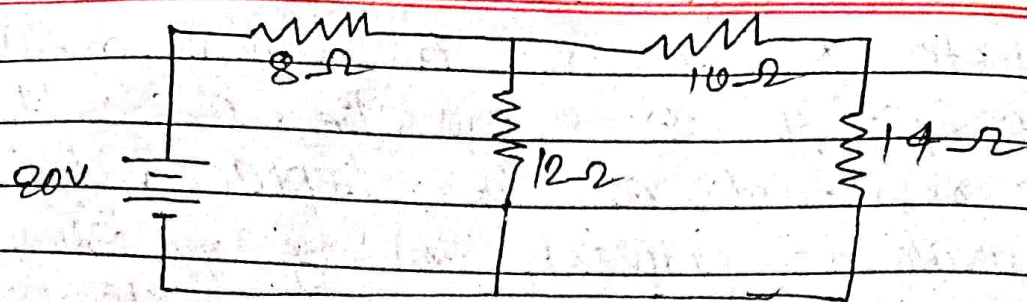
Step (i) ~~short circuit~~ find Norton resistance (R_N) in order to find Norton resistance (R_N) open the load terminal and short circuit the voltage source.

Step (ii) find Norton current in order to find Norton current (I_N) then short the load terminal.

Step (iii) finally make a equivalent network with Norton current I_N and Norton resistance and load terminal.

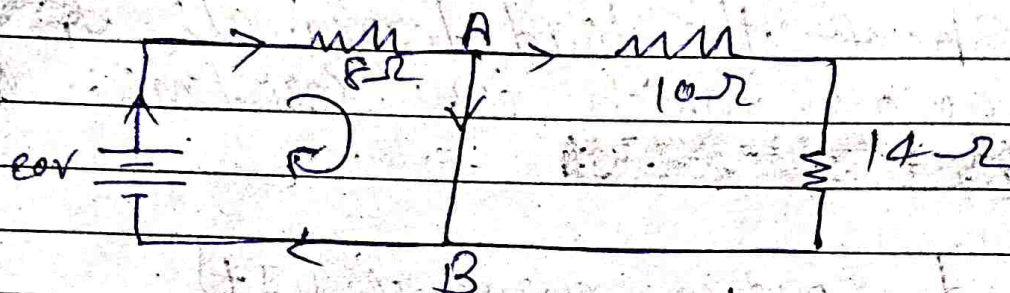


Step (iv) by using current division rule find the Norton current.



find current in 12Ω resistance

Step $\rightarrow$ short the load resistance



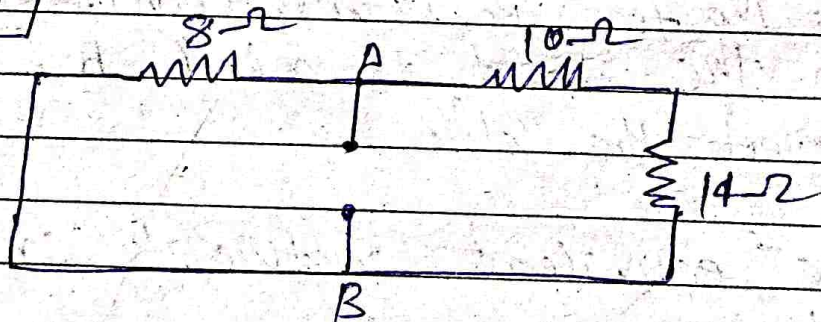
$$I_N = \frac{V}{R}$$

$$I_N = \frac{20}{8}$$

$$I_N = 2.5 \text{ A}$$

To find $I_L = \frac{I_N \times R_N}{R_N + R_L}$

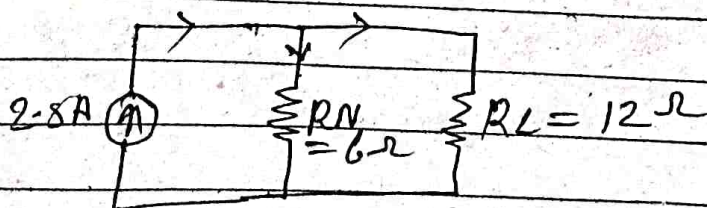
$$R_L = 12\Omega$$



$$R_N = (24 \parallel 8)$$

$$R_N = \frac{24 \times 8}{24 + 8} \quad R_N = \frac{192}{32}$$

$$R_N = 6\Omega$$



$$I_L = \frac{2.5 \times 6}{6 + 12}$$

$$I_L = \frac{15}{18}$$

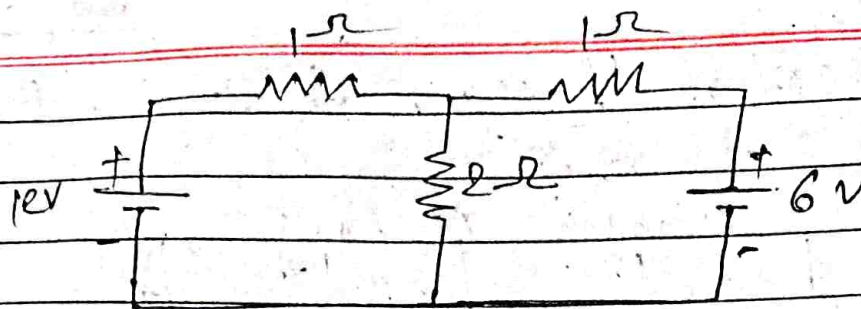
$$I_L = 0.833 \text{ A}$$

find current from 2Ω resistor

Page No.

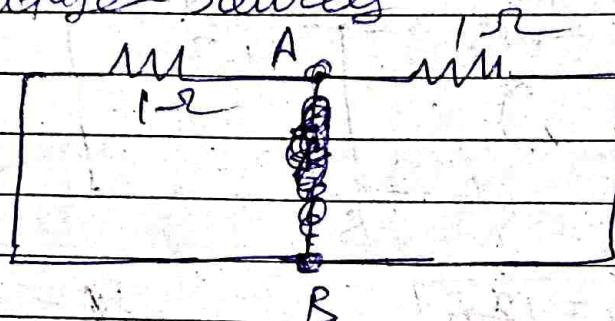
Date / / 20

Q8



Step 1 $\rightarrow$ To find R_N

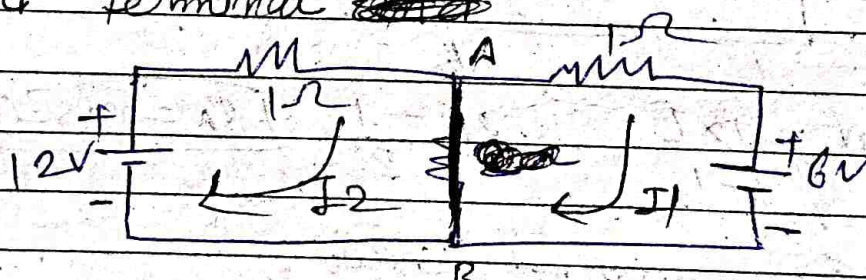
Open the load terminal and short the voltage sources



$$R_N = \frac{1 \times 1}{1+1} \quad R_N = \frac{1}{2}$$

$$R_N = 0.5 \Omega$$

Step - 2 To find I_N short the load terminal



apply KVL

$$I_2 = 12A$$

$$I_1 = -6A / (1)$$

$$I_2 = 12A \quad (\downarrow)$$

$$I_N = 12 + (-6) \quad \downarrow$$

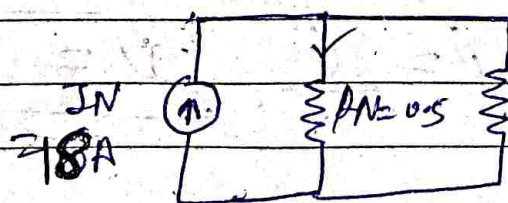
$$I_N = 6A \quad \downarrow$$

$$I_N = \frac{6 \times 0.5}{0.5 + 2}$$

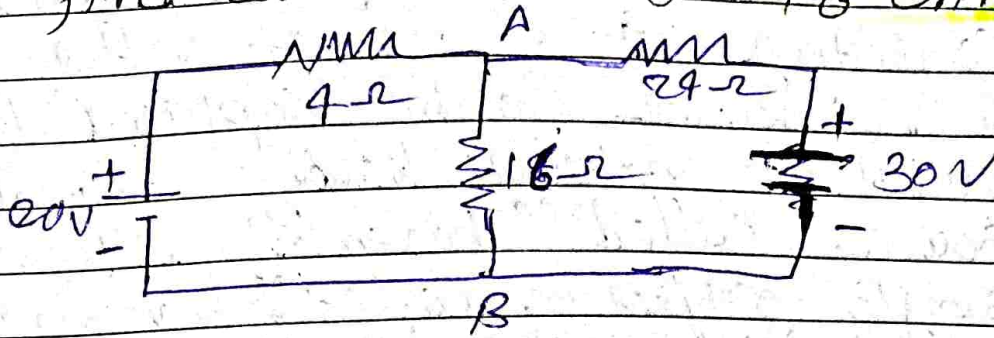
$$I_N = \frac{3}{2.5} \quad \downarrow$$

$$I_N = 1.2A \quad \downarrow$$

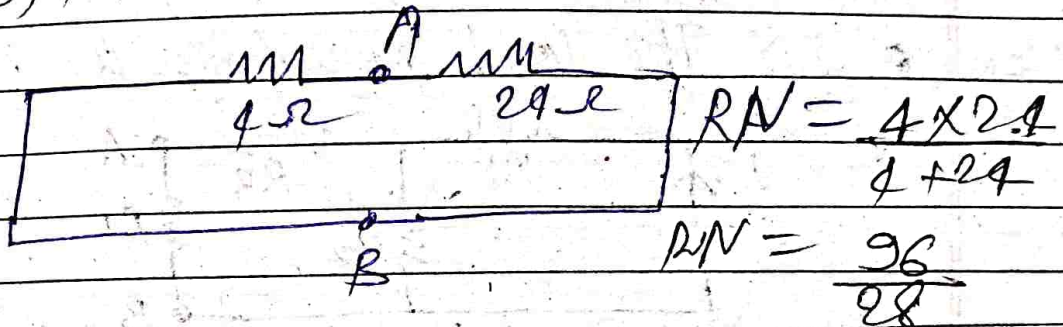
$$I_N = 3.6A \quad \downarrow$$



find current through $16\ \Omega$

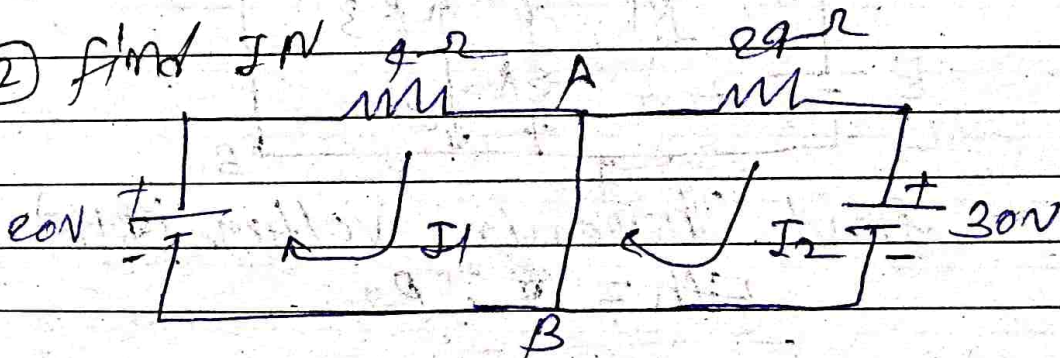


Step 1 find R_N



$$R_N = 3.42\ \Omega$$

Step 2 find I_N



$$4I_1 = 20, \quad 24I_2 = -30$$

$$I_1 = 5\text{ A} \downarrow$$

$$I_2 = -\frac{30}{24}$$

$$I_2 = -1.25\text{ A} \uparrow$$

$$I_N = (5\text{ A}) \downarrow - (-1.25\text{ A}) \uparrow$$

$$I_N = 6.25\text{ A} \downarrow$$

Step 3 equivalent network



Step 4

$$I_N = \frac{6.25 \times 3.42}{3.42 + 16}$$

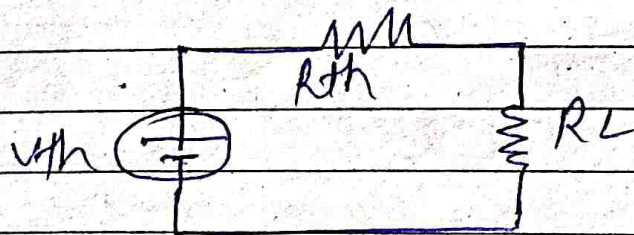
$$I_N = 1.10\text{ A} \downarrow$$

* Thevenin theorem :- Any linear network consisting a number of voltage source and resistance can be replaced by an equivalent network having a single voltage source and a single resistance and a single load terminal.

Step-1 $\Rightarrow$ find R_{th} , To find R_{th} ~~remove~~ open the load resistance and short circuit the voltage source.

Step-2 $\Rightarrow$ find V_{th} , To find V_{th} ~~remove~~ open the load terminal.

Step-3 $\Rightarrow$ Make equivalent network with V_{th} and R_{th} and load terminal



Step-4 $\Rightarrow$ find I_{th} with the help of current division rule.

~~$$R_{th} = R_1 + R_2 // R_3$$~~

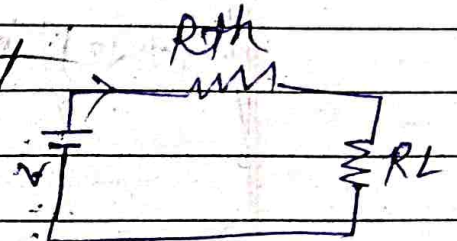
$$R_{th} = R_1 // R_2 + R_3$$

$$R_{th} = \frac{R_1 R_2}{R_1 + R_2} + R_3$$

$$R_{th} = \frac{R_1 R_2 + R_3}{R_1 + R_2} \quad \text{--- (B)}$$

Step - 4 $\rightarrow$ find load current

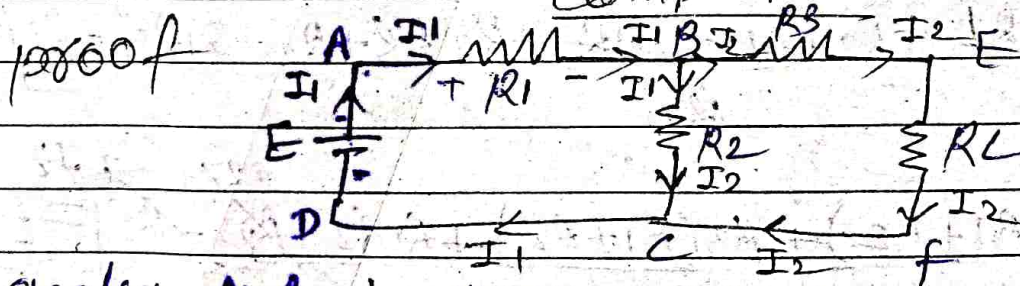
$$I_L = \frac{E_{th}}{R_{th} + R_L}$$



from Eq (A) & (B)

$$I_L = \frac{E R_2}{\left(\frac{R_1 R_2 + R_3}{R_1 + R_2} \right) + R_L}$$

complete



apply KVL in mesh ABCDA

$$I_1 R_1 + I_1 R_2 - I_2 R_2 = E \Rightarrow I_1 (R_1 + R_2) - I_2 R_2 = E$$

again apply KVL in mesh BEFCB

$$I_2 R_3 + I_2 R_L + I_2 R_2 - I_1 R_2 = 0$$

$$I_2 (R_3 + R_L + R_2) - I_1 R_2 = 0 \quad \text{--- (C)}$$

$$I_1 = \frac{I_2 (R_3 + R_L + R_2)}{R_2} \quad \text{--- (C)}$$

$$I_1(R_1 + R_2) - I_2 R_2 = E \quad \text{--- (A)}$$

$$I_2 \frac{(R_1 + R_2 + R_3)R_1 + R_2}{R_2} - I_2 R_2 = E$$

$$\left[\frac{(R_1 + R_2)}{R_2} \frac{(R_1 + R_2 + R_3)R_1 + R_2}{R_2} - I_2 R_2 \right] = E$$

$$\left[\frac{(R_1 + R_2)}{R_2} \frac{R_1 + R_2 + R_3}{R_2} - R_2 \right] I_2 = E$$

$$\frac{R_1 R_1 + R_1 R_2 + R_1 R_3 + R_2 R_1 + R_2 R_2 + R_2 R_3 - R_2^2}{R_2} = E$$

~~$$\frac{R_1 R_2 + R_2(R_1 + R_2) + R_3(R_1 + R_2) + R_2 - R_2^2}{R_2} = E$$~~

~~$$R_1 R_2 + R_3(R_1 + R_2) + R_2$$~~

$$\left[\frac{R_1 + R_2 + R_2 + R_2 + R_1 R_3 + R_2 R_3 + R_2 + R_1 R_2 - R_2^2}{R_2} \right] I_2 = E$$

$$\left[\frac{R_1(R_1 + R_2) + R_3(R_1 + R_2) + R_1 R_2 + R_2 - R_2^2}{R_2} \right] I_2 = E$$

$$\left[R_1 R_2 + R_3(R_1 + R_2) + R_1(R_1 + R_2) \right] I_2 = E R_2$$

~~$$R_1 R_2 + I_2 =$$~~
$$E R_2$$

$$R_1 R_2 + R_3(R_1 + R_2) + R_1(R_1 + R_2)$$

Dividing numerator & denominator by $(R_1 + R_2)$ - we get

$$I_2 = \frac{ER_2}{R_1 + R_2}$$

$$\left(\frac{R_1 R_2}{R_1 + R_2} + R_3 \right) + R_2$$

$$I_2 = I_L$$

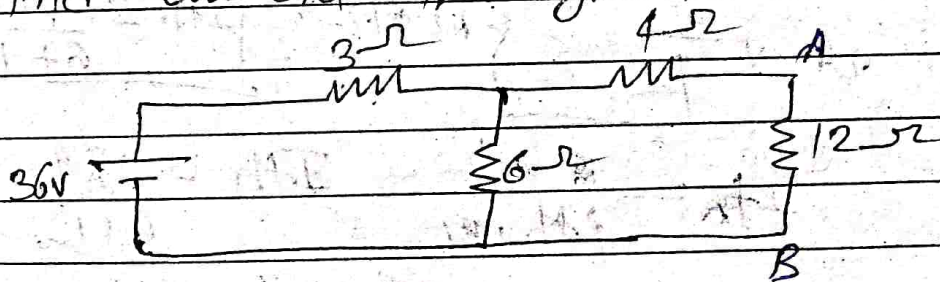
$$I_L = \frac{ER_2}{R_1 + R_2}$$

$$\left(\frac{R_1 R_2}{R_1 + R_2} + R_3 \right) + R_L$$

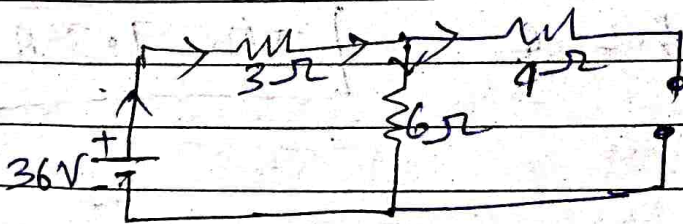
proved

Thevenin theorem

* find current through 12Ω



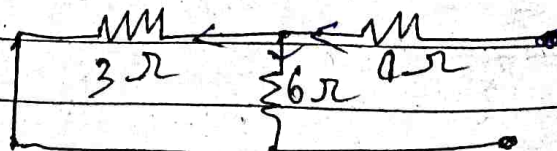
Step 1 $\rightarrow$ Remove the load resistance



Step 2 $\rightarrow$ find eqv R_{th}

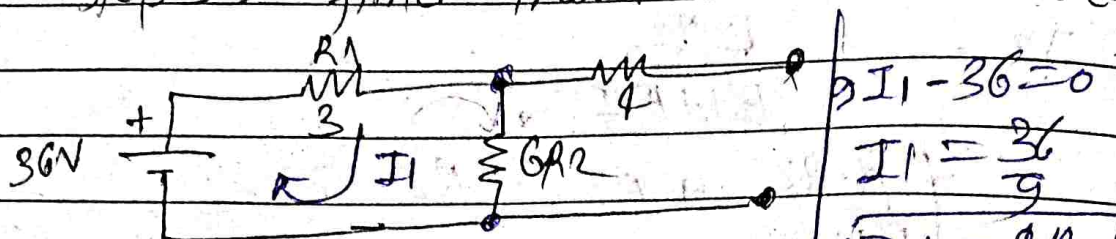
(i) voltage source $\rightarrow$ S.C

(ii) Current source $\rightarrow$ O.C



$$R_{th} = (3 \parallel 6) + 4 \quad \boxed{R_{th} = 6\Omega}$$

Step 3 → find Thevenin eqv voltage



$$I_1 - 36 = 0$$

$$I_1 = \frac{36}{9}$$

$$I_1 = 4A$$

$$V_{th} = 4 \times 6$$

$$V_{th} = 24V$$

$$V = 36, R_{12} = 3 + 6$$

$$R = 9\Omega$$

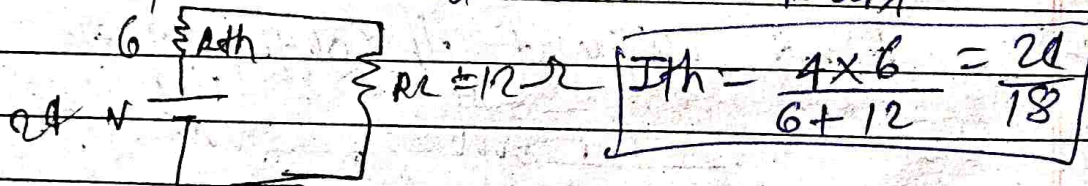
$$I = \frac{36}{9}$$

$$I = 4A$$

$$V_{th} = 4 \times 6$$

$$V_{th} = 24V$$

Step - 4 equivalent circuit



$$I_{th} = \frac{4 \times 6}{6 + 12} = \frac{24}{18}$$

$$I_{th} = \frac{V_{th}}{R_{th} + R_L}$$

$$I_{th} = \frac{24}{6 + 12}$$

$$I_{th} = \frac{24}{18}$$

$$I_{th} = \frac{8}{6}$$

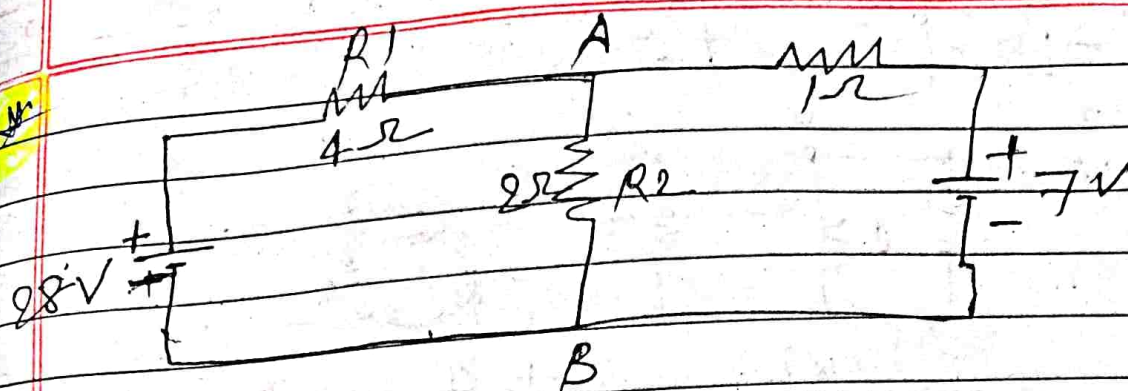
$$I_{th} = \frac{4}{3}$$

$$I_{th} = 1.33A$$

find current across AB

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Step ① find R_{th}

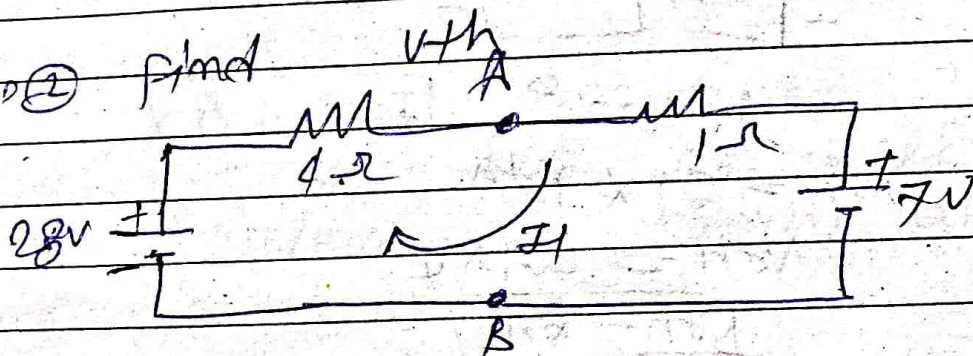


$$R_{th} = \frac{4 \times 1}{4 + 1}$$

$$R_{th} = \frac{4}{5}$$

$$R_{th} = 0.8 \Omega$$

Step ② find V_{th}



KVL

$$5I_1 + 7 - 28 = 0$$

$$5I_1 = 21$$

$$I_1 = \frac{21}{5}$$

$$I_1 = 4.2 \text{ A}$$

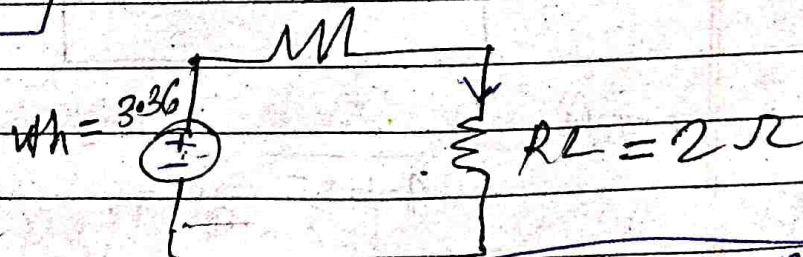
$$V = IR$$

$$V_{th} = 4.2 \times 0.8$$

$$V_{th} = 3.36 \text{ V}$$

$$R_{th} = 0.8 \Omega$$

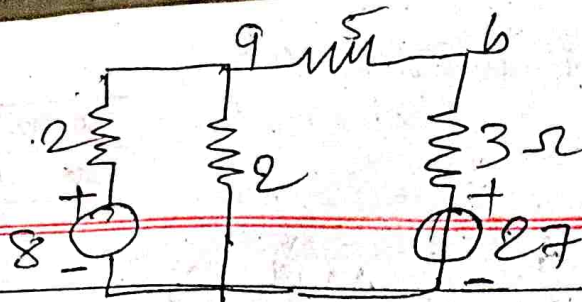
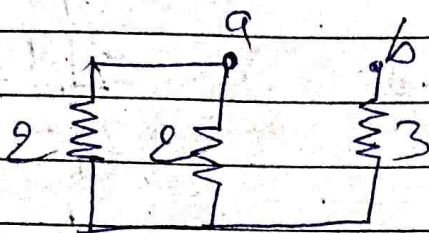
Step ③



$$I_{th} = \frac{3.36}{0.8 + 2}$$

$$I_{th} = \frac{3.36}{2.8}$$

$$I_{th} = 1.2 \text{ A}$$

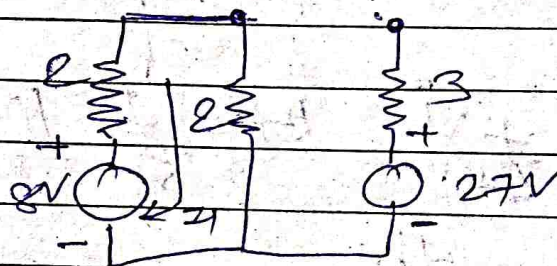
find $R_{th} \rightarrow$ 

$$3 + \frac{2 \times 2}{2 + 2}$$

$$3 + \frac{4}{4} = 4$$

$$R_{th} = 4 \Omega$$

find

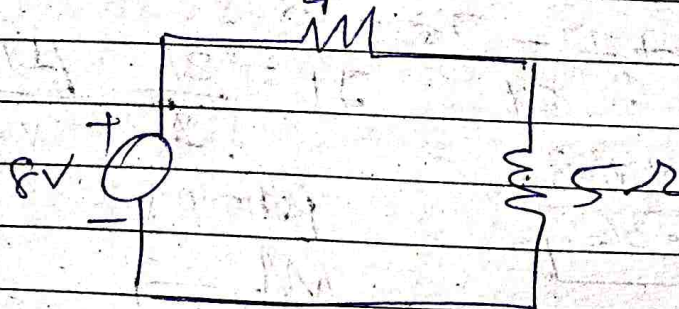
 V_{th} or V_{th} 

$$4I_1 = 8 \quad I_1 = 2A$$

$$V_{th} = I_1 \times R_{th}$$

$$V_{th} = 2A \times 4$$

$$V_{th} = 8V$$

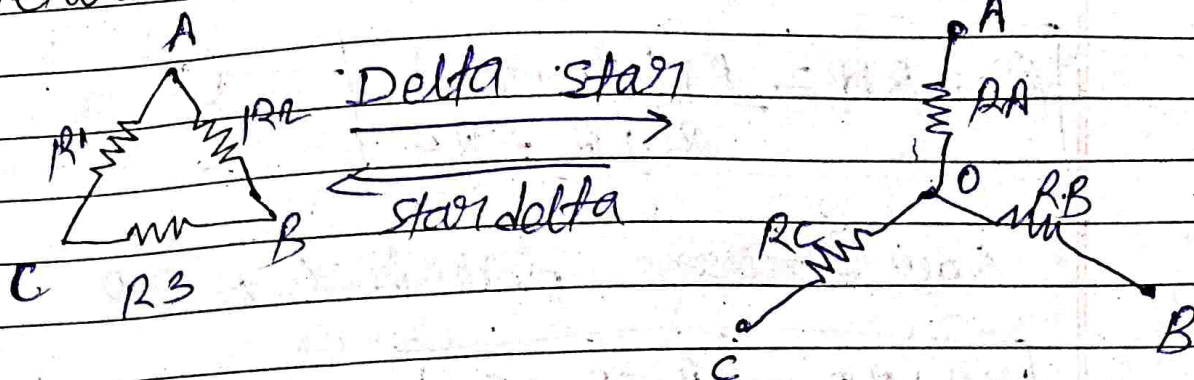


$$I_{th} = \frac{8}{4 + 5}$$

$$I_{th} = \frac{8}{9}$$

$$I_{th} =$$

* Network Reduction by Δ : star transformation



* Delta

3 R connected nose to tail are said to be delta or mesh connected

* 3 R connected together at a common point O are said to be star or delta connected

* Replacement of delta or mesh equivalent star system is known as delta star transformation

The ~~two~~ two systems will be equivalent if the resistance measure between any pair of line is same in both of the system and third line is open

* Resistances between terminals B & C in Δ

$$R_{BC} = R_3 \parallel (R_1 + R_2) = \frac{R_3(R_1 + R_2)}{R_1 + R_2 + R_3}$$

for star $\rightarrow R_{BC} = R_B + R_C$

$$R_B + R_C = \frac{R_3(R_1 + R_2)}{R_1 + R_2 + R_3} \quad \text{--- (1)}$$

between terminal C & A

$$R_C + R_A = \frac{R_1(R_2 + R_3)}{R_1 + R_2 + R_3} \quad \text{--- (2)}$$

Now between terminal A & B

$$R_A + R_B = \frac{R_2(R_1 + R_3)}{R_1 + R_2 + R_3} \quad \text{--- (3)}$$

from eqⁿ (1), (2) & (3) add 1+2+3

we have

$$2(R_A + R_B + R_C) = \frac{2(R_1 R_3 + R_2 R_3 + R_1 R_2)}{R_1 + R_2 + R_3}$$

~~$$R_A + R_B + R_C = \frac{R_1 R_3 + R_2 R_3 + R_1 R_2}{R_1 + R_2 + R_3}$$~~

$$R_A + R_B + R_C = \frac{R_1 R_3 + R_2 R_3 + R_1 R_2}{R_1 + R_2 + R_3} \quad \text{--- (4)}$$

subtract (1), (2), (3) from 4

$$(4) - (1)$$

$$R_A = \frac{R_1 R_2}{R_1 + R_2 + R_3} \quad \text{--- (5)}$$

① - ②

$$R_B = \frac{R_1 R_2 + R_1 R_3 + R_2 R_3 + R_2 R_3 + R_1 R_2}{R_1 + R_2 + R_3}$$

$$R_B = \frac{R_2 R_3}{R_1 + R_2}$$

$$R_B = \frac{R_2 R_3}{R_1 + R_2} \quad \text{--- (6)}$$

③ - ⑥

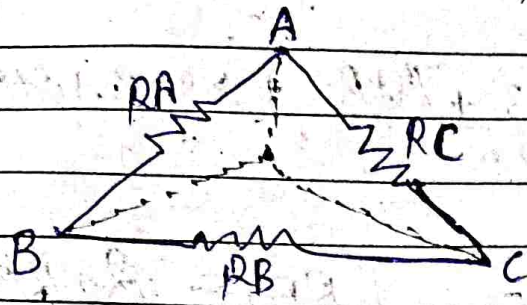
$$R_C = \frac{R_1 R_3 + R_2 R_3 + R_1 R_2}{R_1 + R_2 + R_3} - \frac{R_1 R_2 + R_1 R_3}{R_1 + R_2 + R_3}$$

$$R_C = \frac{R_1 R_3 + R_2 R_3 + R_1 R_2 - R_1 R_2 - R_1 R_3}{R_1 + R_2 + R_3}$$

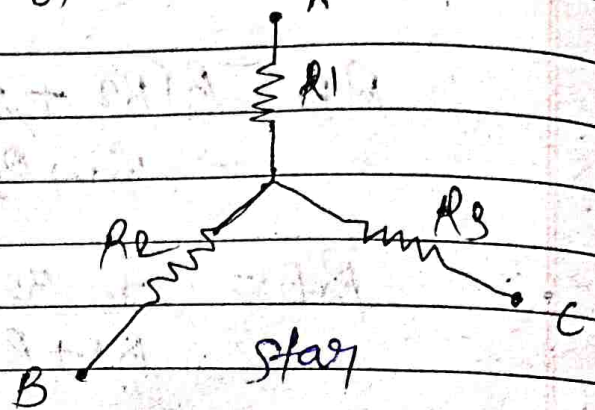
$$R_C = \frac{R_2 R_3}{R_1 + R_2 + R_3} \quad \text{--- (7)}$$

*
Solⁿ ↓

Delta to star transformation



Delta



Star

equivalent resistance between A & B

$$R_A / (R_B + R_C)$$

$$\Rightarrow \frac{R_A (R_B + R_C)}{R_A + R_B + R_C} \quad \text{--- (1)}$$

Similarly eqv resⁿ b/w B & C

$$R_B / (R_A + R_C) \Rightarrow \frac{R_B (R_A + R_C)}{R_A + R_B + R_C} \quad \text{--- (2)}$$

eqv resⁿ b/w C & A

$$R_C / (R_A + R_B) \Rightarrow \frac{R_C (R_A + R_B)}{R_A + R_B + R_C} \quad \text{--- (3)}$$

Eq val resⁿ b/w A & B in star

$$R_1 + R_2 \quad \text{--- (4)}$$

Similarly eq resⁿ b/w B & C

$$R_2 + R_3 \quad \text{--- (5)}$$

eqv resⁿ b/w C & A

$$R_3 + R_1 \quad \text{--- (6)}$$

eqvⁿ (1) & (4) eqvade

$$\frac{RA(RB+RC)}{RA+RB+RC} = R1 + R2 \quad \text{--- (7) ✓}$$

$$RA+RB+RC$$

Similarly equating eqⁿ (2) & (5)

$$\frac{RB(RA+RC)}{RA+RB+RC} = R2 + R3 \quad \text{--- (8) ✓}$$

$$RA+RB+RC$$

Equating equation (3) & (6)

$$\frac{RC(RA+RB)}{RA+RB+RC} = R3 + R1 \quad \text{--- (9) ✓}$$

$$RA+RB+RC$$

$$\text{Eqⁿ (7) - (8)}$$

$$\frac{RA(RB+RC)}{RA+RB+RC} - \frac{RB(RA+RC)}{RA+RB+RC} = R1 - R3 \quad \text{--- (10) ✓}$$

$$RA+RB+RC$$

$$\text{add eqⁿ (9) + (10)}$$

$$\frac{RA \cdot RB + RA \cdot RC - RB \cdot RA - RB \cdot RC + RA \cdot RC + RB \cdot RC}{RA+RB+RC} = 2R1$$

$$RA+RB+RC$$

$$\frac{RA \cdot RC}{RA+RB+RC} = R1 \Rightarrow$$

$$RA+RB+RC$$

$$R1 = \frac{RA \cdot RC}{RA+RB+RC}$$

$$RA+RB+RC$$

Similarly

$$R2 = \frac{RA \cdot RB}{RA+RB+RC}$$

$$RA+RB+RC$$

$$R3 = \frac{RB \cdot RC}{RA+RB+RC}$$

$$RA+RB+RC$$

Suppose in delta $RA = RB = AC = RD$

and in star $\Rightarrow R1 = R2 = R3 = R5$

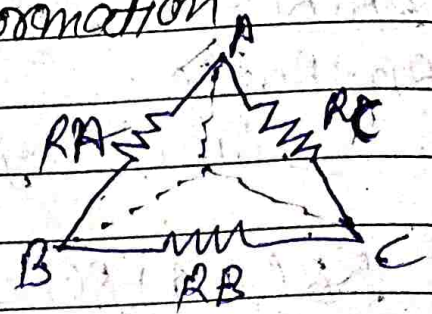
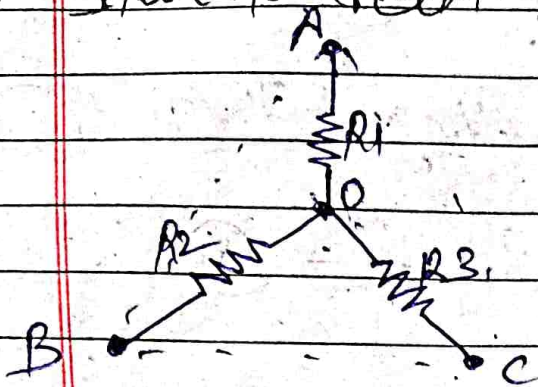
$$R5 = \frac{RD \cdot RD}{RD+RD+RD}$$

$$R5 = \frac{RD}{3RD}$$

$$R5 = \frac{RD}{3}$$

$$RD = 3R5$$

* Star to delta transformation



$$R_1 = \frac{R_A R_C}{R_A + R_B + R_C} \quad R_2 = \frac{R_A R_B}{R_A + R_B + R_C} \quad R_3 = \frac{R_B R_C}{R_A + R_B + R_C}$$

Multiply $R_1 R_2 + R_2 R_3 + R_3 R_1$

$$\frac{R_A^2 R_B R_C}{(R_A + R_B + R_C)^2} + \frac{R_B^2 R_A R_C}{(R_A + R_B + R_C)^2} + \frac{R_C^2 R_A R_B}{(R_A + R_B + R_C)^2}$$

$$\frac{R_A R_B R_C (R_A + R_B + R_C)}{(R_A + R_B + R_C)^2}$$

$$R_1 R_2 + R_2 R_3 + R_3 R_1 = \frac{R_A R_B R_C}{R_A + R_B + R_C} \quad \text{from eq (25)}$$

$$R_1 R_2 + R_2 R_3 + R_3 R_1 = R_A \cdot R_B$$

$$\frac{R_1 R_2}{R_3} + \frac{R_2 R_3}{R_3} + \frac{R_3 R_1}{R_3} = R_A \quad (26)$$

$$\frac{R_1 R_2}{R_3} + R_2 + R_1 = R_A \quad \text{Similarly in (26)}$$

$$\frac{R_2 R_3}{R_1} + R_2 + R_3 = R_B$$

$$\frac{R_1 R_3}{R_2} + R_1 + R_3 = R_C$$

$$\frac{R_S}{R_S} + \frac{R_S}{R_S} + \frac{R_S}{R_S} = R_D$$

$$3R_S = R_D$$

$$R_D = 3R_S$$

$$R_S = \frac{R_D}{3}$$

Suppose $R_1 = R_2 = R_3 = R_S$
 $R_A = R_B = R_C = R_D$

AC circuit

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* Equation of alternative current V & I

max flux $\boxed{\phi = \phi_m \cos \omega t}$

across x axis $\boxed{N\phi = N\phi_m \cos \omega t}$

Emf induced in coil $\propto$ rate of change of flux linkage in the coil.

$$\epsilon \propto -\frac{d\phi}{dt} \Rightarrow \epsilon = -\frac{d(N\phi_m \cos \omega t)}{dt}$$

$$\epsilon = -N\phi_m(-\sin \omega t \cdot \omega)$$

$$\epsilon = +N\phi_m \sin \omega t \cdot \omega$$

$$\boxed{\epsilon = \omega N\phi_m \sin \omega t}$$

$$\because \omega t = 0 \\ 0 = 90$$

$$\because \boxed{\epsilon_m = \omega N\phi_m}$$

$$\because \phi = BA \\ \omega = 2\pi f$$

$$\boxed{\epsilon = \epsilon_m \sin \theta}$$

Similarly ϕ_m

$$\rightarrow \boxed{I = \omega N\phi_m \sin \omega t}$$

$$\because \boxed{I_m = \omega N\phi_m}$$

$$\boxed{I = I_m \sin \omega t}$$

$$\boxed{I = I_m \sin \theta}$$

$$\text{Time period} \Rightarrow T = \frac{1}{f}$$

$$\text{frequency} \Rightarrow f = \frac{1}{T}$$

$$V_{\text{rms}} = \frac{V_m}{\sqrt{2}}$$

$$I_{\text{rms}} = \frac{I_m}{\sqrt{2}}$$

$$[V/c] \rightarrow \text{RMS value} = 0.707 \times \text{Max. Value}$$

$$\text{Average value} = 0.637 \times \text{Maximum value}$$

$$\text{form factor} = \frac{\text{RMS value}}{\text{Avg value}}$$

$$(K_f) \text{ form factor} = \frac{0.707 \text{ Max val}}{0.637 \text{ Max val}}$$

$$\text{form factor} = 1.11$$

$$\text{Amplitude} = 1.414$$

$$\text{Peak factor} = \frac{\text{max val}}{\text{rms val}} \quad K_p = 1.414$$

* The ac supply at a house is 230V, So we find maximum, Average and ~~value~~ value of voltage $\therefore V_{\text{max}} = 230V$

$$V_{\text{rms}} = 0.707 \times \text{Max. value}$$

$$\text{Max value} = \frac{V_{\text{rms}}}{0.707} \quad V_{\text{Max}} = \frac{230}{0.707}$$

$$V_{\text{Max}} = 325.31$$

$$V_{\text{avg}} = 0.637 \times V_{\text{Max}}$$

$$V_{\text{avg}} = 207.82 \text{ V}$$

* Define peak factor and form factor of an alternative current.

* Peak factor $\div$ peak factor is the ratio of maximum value and rms value, is called peak factor

$$K_p = \frac{\text{Max value}}{\text{rms value}}$$

form factor is

* form factor $\div$ the ratio of rms value and average value is, form factor. called

$$K_f = \frac{\text{RMS value}}{\text{average value}}$$

* Average value $\div$ Average value is the multiplication of maximum value and 0.637.

$$\text{Average val} = 0.637 \times \text{max val}$$

* Define magnetic flux and give its unit?

ans $\Rightarrow$ Total magnetic field which is passes through a given area is called magnetic flux. its unit is ~~SI unit~~ SI unit is (Weber).

* Average value of alternative current $\div$ area of first half cycle divide by π is called Average value of A.C

* Define RMS value of ac $\rightarrow I_{rms} = \frac{I_{max}}{\sqrt{2}}$

The ratio of maximum ~~current~~ current and $\sqrt{2}$ is called RMS value of

ac.

$$I_{rms} = \frac{I_{max}}{\sqrt{2}}$$

* The eq of alternative current

$$i = 42.42 \sin 628t$$

- (i) peak or max value (iv) average value
(ii) frequency (v) form factor
(iii) rms value

Sol: $i = 42.42 \sin 628t$

Compare with $i = i_m \sin \omega t$

(1) $i_{max} = 42.42$ $\omega = 628$

$\therefore \omega = 2\pi f$ So $f = \frac{628}{2\pi}$

(ii) $f = 100 \text{ Hz}$ $I_{rms} = 0.707 \times I_{max}$

$I_{rms} = 0.707 \times 42.42$

(iii) $I_{rms} = 30 \text{ A}$

(iv) $I_{avg} = 0.637 \times \text{max value}$

$I_{avg} = 0.637 \times 42.42$

(v) $I_{avg} = 27 \text{ A}$

(v) form factor $\Rightarrow k_f = \frac{I_{rms}}{I_{avg}}$

$k_f = \frac{30}{27}$

$k_f = 1.11$

(1) Peak factor
 $= \frac{\text{max val}}{\text{rms val}}$
 $k_p = \frac{42.42}{30}$

$k_p = 1.414$

* An alternative voltage $V = 100 \sin 100t$ find

(i) amplitude (ii) time period (iii) frequency

(iv) angular velocity (v) form factor

(vi) peak factor

Sol:

$V = 100 \sin 100t$

Compare with $v = v_m \sin \omega t$

$$V_{max} = 100, \quad \omega = 100$$

$$\omega = 2\pi f \quad f = \frac{100}{2\pi}$$

$$(iii) f = 15.92 \text{ Hz}, T = \frac{1}{f} \quad (iv) T = 0.0628$$

$$(iv) \text{ angular velocity } \Rightarrow \omega = 2\pi f$$

$$\boxed{\omega = 100}$$

$$K_f = \frac{RMS \text{ val}}{avg \text{ val}}, \quad K_f = \frac{0.707 \text{ max val}}{0.637 \text{ max val}}$$

$$V_{rms} = 0.707 V_{max}$$

$$V_{rms} = 0.707 \times 100 \quad avg \text{ val} = 0.637 \times V_{max}$$

$$\boxed{V_{rms} = 70.7 \text{ V}} \quad avg \text{ val} = 0.637 \times 100$$

$$\boxed{avg \text{ val} = 63.7 \text{ V}}$$

$$K_f = \frac{70.7}{63.7} \quad (v) \boxed{K_f = 1.11}$$

$$K_p = \frac{100}{70.7} \quad (vi) \boxed{K_p = 1.414}$$

* The equation of alternative voltage
 $v = 42.42 \sin 628t$ Determine.

- (i) average value (ii) rms value
 (iii) form factor (iv) peak factor

$$v = 42.42 \sin 628t$$

Compare with $v = V_m \sin \omega t$

$$\boxed{V_{max} = 42.42}, \quad \boxed{\omega = 628}$$

$$V_{\text{avg}} = 0.707 \times V_{\text{max}} \sqrt{2}$$

$$= 0.707 \times 42.42$$

$$\boxed{V_{\text{avg}} = 30 \quad \checkmark}$$

$$\text{average val} = 0.637 \times V_{\text{max}}$$

$$\text{average val} = 0.637 \times 42.42$$

$$\boxed{\text{average val} = 27 \text{ V} \quad \checkmark}$$

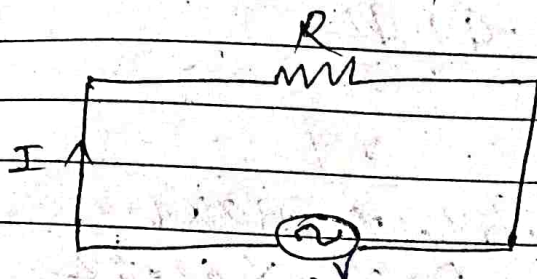
$$K_f = \frac{30}{27} \quad \boxed{K_f = 1.11}$$

$$K_p = \frac{42.42}{30}$$

$$\boxed{K_p = 1.414}$$

* Define power factor

* AC through pure resistance



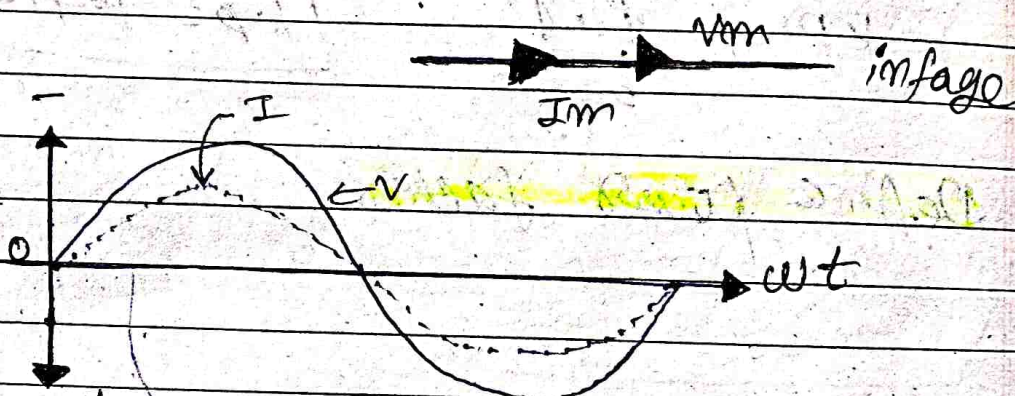
$$V = V_m \sin \omega t$$

$$I = I_m \sin \omega t$$

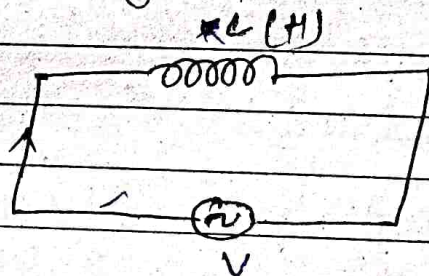
$$I_m = \frac{V_m}{R}$$

$$V = (V_m \angle 0^\circ)$$

$$I = (I_m \angle 0^\circ)$$



* AC through pure inductance



$L \rightarrow$ current voltage
 $\log$ ϕ with 90°
 mean (current $- 90^\circ$)

$$V = V_m \sin \omega t$$

$$I = I_m \sin (\omega t - 90^\circ)$$

$$I_m = \frac{V_m}{X_L}$$

$$V = (V_m \angle 0^\circ)$$

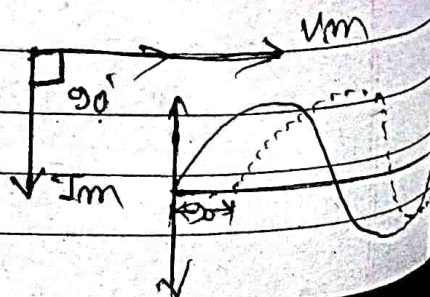
$$I = (I_m \angle -90^\circ)$$

$$X_L = \omega L$$

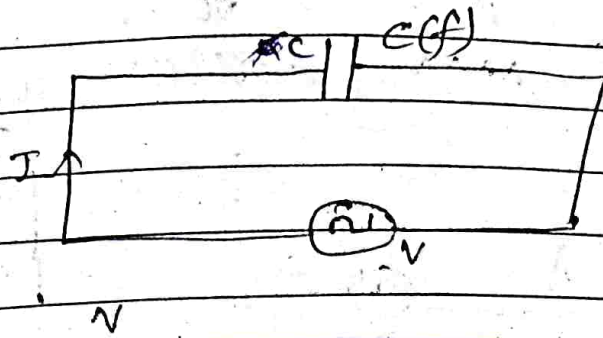
$$\omega = 2\pi f$$

$$X_L = 2\pi f L$$

$$I_m = \frac{V_m}{2\pi f L}$$



* AC through pure capacitance



at current voltage
lead with 90
means (current + 90)

$$V = V_m \sin \omega t$$

$$V = (V_m = 0)$$

$$I = I_m \sin(\omega t + 90)$$

$$I = (I_m = +90)$$

$$I_m = \frac{V_m}{X_c}$$

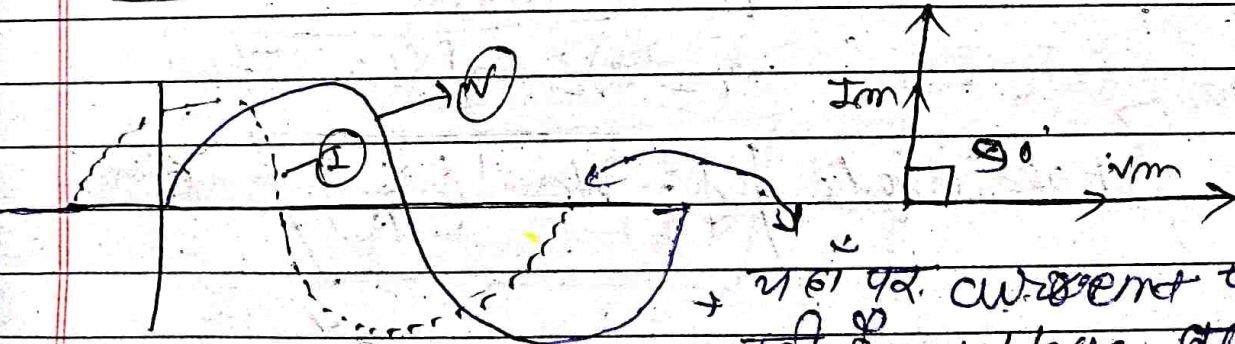
$$I_m = \frac{V_m}{\frac{1}{2\pi f C}}$$

$$I_a = 2\pi f C \cdot V_m$$

$$X_c = \frac{1}{\omega C}$$

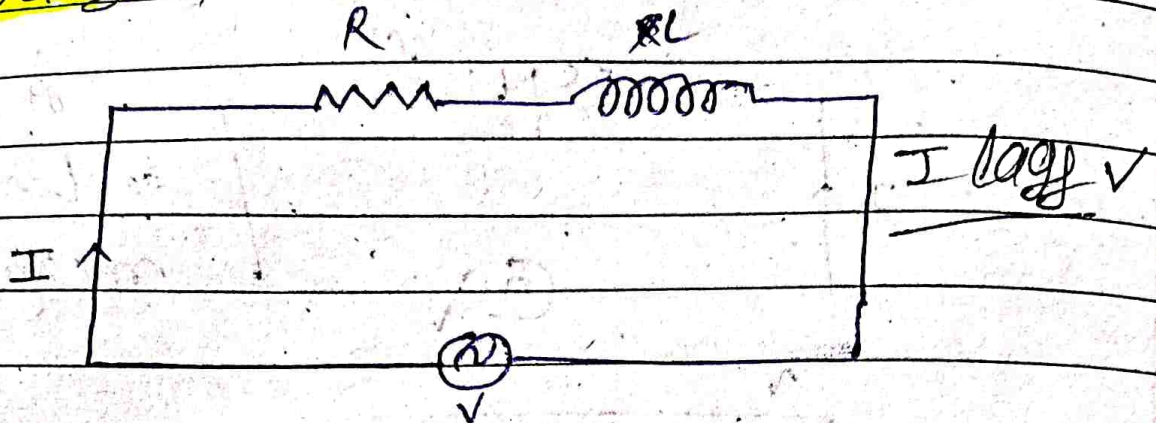
$$X_c = \frac{1}{2\pi f C}$$

$$I_m = \frac{V_m}{\frac{1}{\omega C}}$$



यहाँ पर current पहले बढ़ रहा है, voltage बाद में बढ़ रहा है। यानी I, V को lead कर रही है।

* Series R-L circuit



$$v = v_m \sin \omega t$$

$$I = I_m \sin(\omega t - \phi) \quad \left| \begin{array}{l} v = (v_m = 0) \\ I = (I_m = -\phi) \end{array} \right.$$

$$\therefore I = \frac{V}{Z} \rightarrow Z = \text{impedance } (\Omega)$$

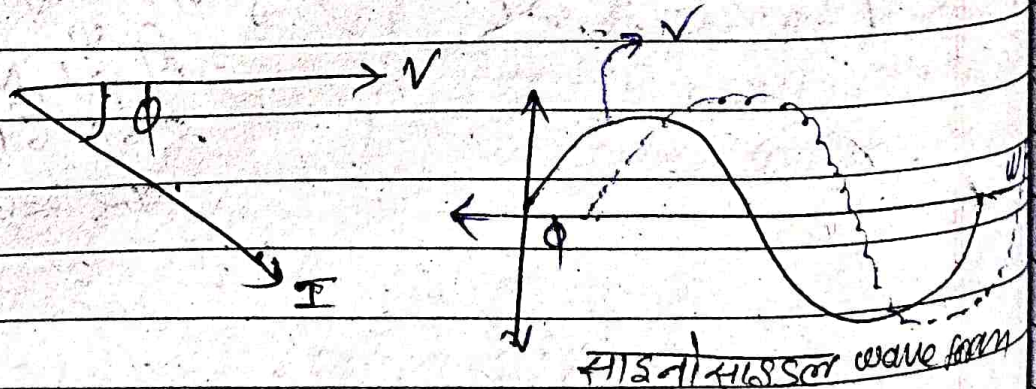
$$Z = R + XL$$

$$Z = \sqrt{R^2 + (XL)^2}$$

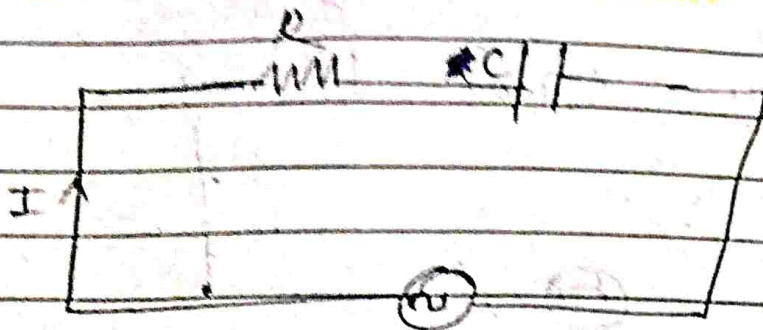
$$Z = \sqrt{R^2 + (\omega L)^2}$$

$$XL = \omega L \Rightarrow [XL = 2\pi fL]$$

phase angle $\phi = \tan^{-1} \left(\frac{XL}{R} \right)$



Series R-C Circuit



$$V = V_m \sin \omega t$$

$$I = I_m \sin(\omega t + \phi) \quad \left| \begin{array}{l} V = 0 \quad (V_m = 0) \\ I = 0 \quad (I_m = 0) \end{array} \right.$$

$$I = \frac{V_m}{Z} \rightarrow \text{Impedance}$$

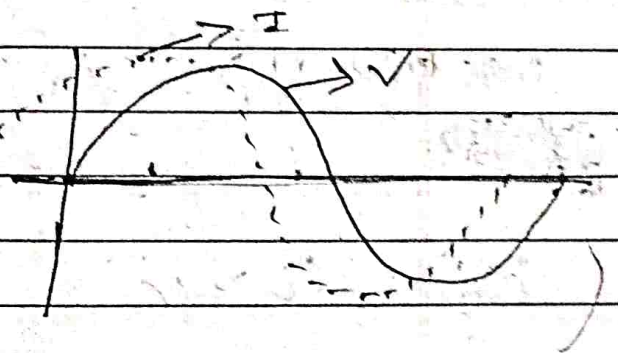
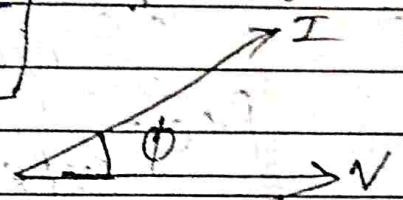
$$Z = R + X_C$$

$$Z = \sqrt{R^2 + (X_C)^2}$$

I leads V

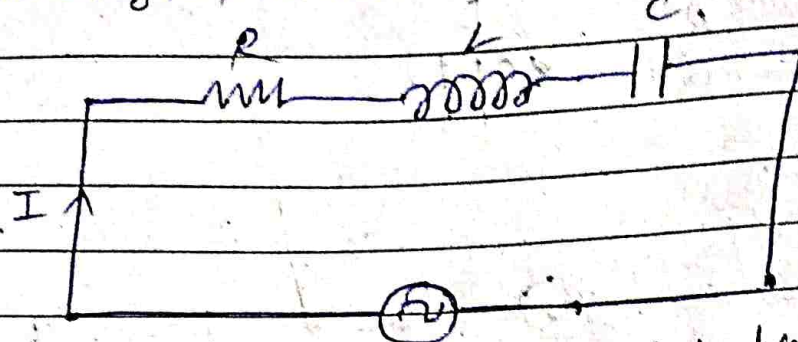
$$X_C = \frac{1}{\omega C} \quad \left| \quad X_C = \frac{1}{2\pi f C} \right.$$

phase angle $\phi = \tan^{-1} \left(\frac{X_C}{R} \right)$



*

Series RLC circuit resonance in RLC



$$V = V_m \sin \omega t$$

$$I = I_m \sin(\omega t \pm \phi)$$

$$V = (V_m = 0)$$

$$I = (I_m \pm \phi)$$

$$I = \frac{V}{Z}$$

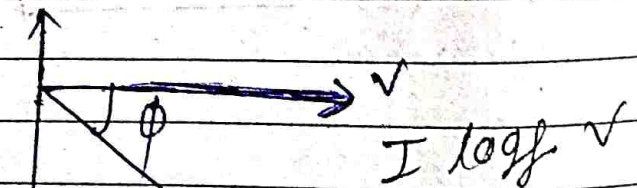
$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$X_C = \frac{1}{\omega C}, \quad X_L = \omega L$$

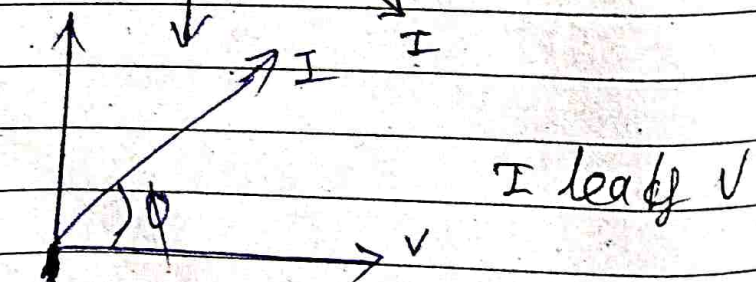
$$X_C = \frac{1}{2\pi f C}, \quad X_L = 2\pi f L$$

phase angle $\Rightarrow \phi = \tan^{-1} \left(\frac{X_L - X_C}{R} \right)$

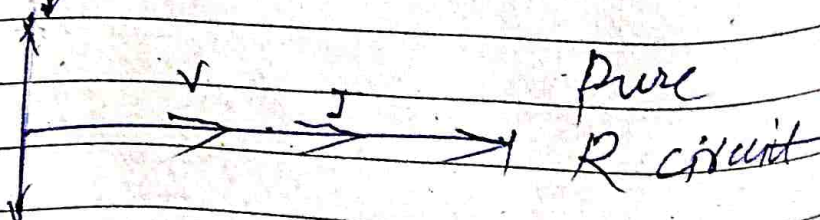
Case (i) $X_L > X_C$



Case (ii) $X_C > X_L$



Case (iii) $X_L = X_C$



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* Define apparent power, active power and reactive power.

* Active power: That power which is consumed or utilized in a circuit is called ^{active} power ~~power~~, it is denoted by P . its unit is (KW)

$$[P = VI \cos \phi]$$

$$P = \frac{S}{\cos \phi}$$
 power

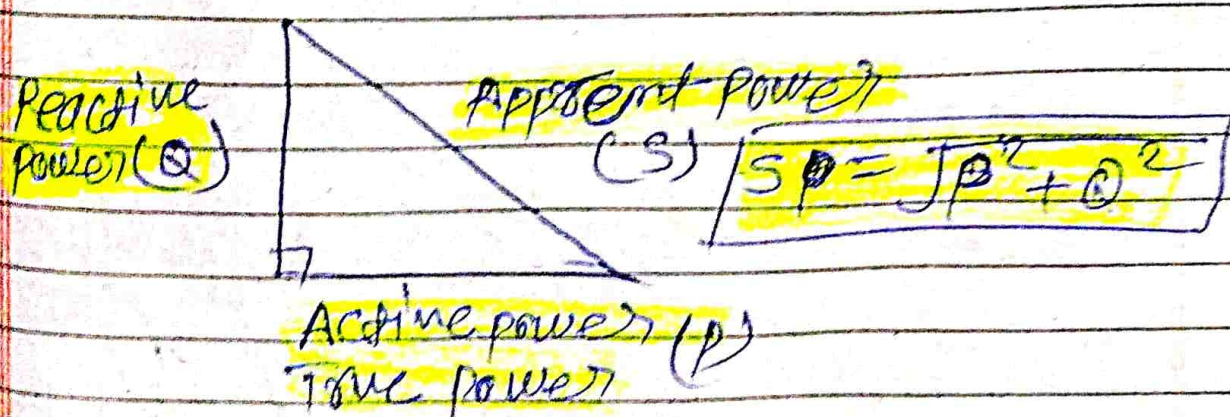
* reactive power: reactive is the useless power which is moves between source and load in the circuit. it is denoted by Q . It is known as imaginary power or wattless power. ~~It is the~~ reactive power is the $\sin \phi$ angle between voltage and current, its unit is (VAR)

$$Q = VI \sin \phi$$

* Apparent power: Apparent power is the ~~combination~~ combination of Active and reactive power is called apparent power. it is denoted by S .

$$[S = \sqrt{P^2 + Q^2}] \quad S = VI \quad (\text{KVA}) \text{ unit}$$

* Draw the power triangle



z = impedance ; x = Reactance

x_L = inductive reactance

x_C = Capacitive reactance

ω = angular velocity

t = time f = frequency

Power factor = $\cos \phi$ (leading or lagging)

Active power $\rightarrow P = I^2 R$

find the true power
Reactive power $\rightarrow$ power, power lost, power absorbed,
power consumed $\rightarrow$ Active power

$$P = I^2 R \quad (\text{W or kW})$$

$$V_{rms} = \frac{V_m}{\sqrt{2}} \quad I_{rms} = \frac{I_m}{\sqrt{2}}$$

$$P = |V| |I| \cos \phi \quad (\text{kW}) \quad \phi = \text{power factor angle}$$

$$\text{Reactive power } Q = |V| |I| \sin \phi \quad (\text{VAR or kVAR})$$

imaginary power
wattless power

$\cos \phi / \sin \phi \rightarrow \cot \phi$ and $\tan \phi$

phase angle

What is active and reactive power?

power factor $\div$ power factor is cosine of angle between voltage and current so it the ratio of resistance to impedance

power factor in never be greater than unity

among $\rightarrow (1)$

$$\text{Apparent power} \rightarrow VI, S = \sqrt{P^2 + Q^2} \quad \text{VA or kVA}$$

$\rightarrow$ rms value

* The sinusoidal voltage applied to a circuit of unknown impedance is $v = 325 \sin \omega t$ and the current $i = 7 \sin \omega t + 63^\circ$. Hence find (i) RMS value of voltage and current (ii) unknown impedance (iii) power factor (iv) comment whether the current is lagging or leading w.r.t. voltage

(i) $v_{rms} = ?$ (ii) $I_{rms} = ?$ $Z = ?$ $\phi = ?$

given $v = 325 \sin \omega t$

$\phi = 63^\circ$ $i = 7 \sin(\omega t + 63^\circ)$

$v_m = 325$, $I_m = 7$

(i) $v_{rms} = \frac{v_m}{\sqrt{2}}$, $v_{rms} = \frac{325}{\sqrt{2}}$

$v_{rms} = 229.80 \text{ V}$

$I_{rms} = \frac{I_m}{\sqrt{2}}$ $I_{rms} = 4.94 \text{ A}$

$I = \frac{v_m}{Z}$ $Z = \frac{v_m}{I}$

$Z = \frac{325}{7}$ $Z = 46.42 \Omega$

$\phi = 63^\circ$ ✓

Current is leading w.r.t. voltage with 63° angle

* $\varepsilon(t) = 150 \sin(2\pi f)t$, $50, 112, 10 \Omega$, 0.0318 Henry. for R-L circuit

- (i) Expression for I ✓
- (ii) Phase angle b/w V & I ✓
- (iii) Power factor ✓

Given $\varepsilon = 150 \sin(2\pi f)t$

$$V_m = 150, \omega = 2\pi f, L = 0.0318, X_L = \omega L$$

$$R = 10 \Omega, \omega = 2\pi \cdot 50, X_L = 100\pi \times 0.0318$$

$$I = \frac{V_m}{Z}, Z = \sqrt{R^2 + (X_L)^2}$$

$$X_L = \omega L, X_L = 2\pi \times 50 \times 0.0318, Z = \sqrt{R^2 + (X_L)^2}$$

$$X_L = 9.99 \Omega, X_L^2 = 99.80$$

$$I = \frac{150}{\sqrt{100 + 99.80}}, I = \frac{150}{14.12}, I = 10.61 A$$

$$\phi = \tan^{-1}\left(\frac{X_L}{R}\right), \phi = \frac{9.99}{10}, \phi = 0.999$$

$$\phi = \tan^{-1}(0.999), \phi = 0.78$$

$$(iii) \text{ Power factor } \cos \phi \Rightarrow \cos(0.78), I$$

$$PF = 0.71, \text{ leading } \Rightarrow V$$

$$I \text{ leading } V$$

- * The current $I = 35.36 \sin 314t$ is flowing through R-series circuit having $R = 15 \Omega$ and $X_L = 12 \Omega$.
 (i) RMS value of current (ii) Average value of current
 (iii) impedance (iv) power factor

and $\Rightarrow$ Given $I = 35.36 \sin 314t$
 $R = 15 \Omega$ $I_{\text{m}} = 35.36$
 $X_L = 12 \Omega$

$I_{\text{rms}} = \frac{35.36}{\sqrt{2}}$ $I_{\text{avg}} = 25.00 \text{ A}$

$I_{\text{avg}} = 0.637 \times I_{\text{max}}$

$I_{\text{avg}} = 0.637 \times 35.36$

$= 0.637 \times 35.36$

$I_{\text{avg}} = 22.52 \text{ A}$ $Z = \sqrt{R^2 + (X_L)^2}$ $\downarrow 15/10$

(iii) $Z = ?$ $I = \frac{V}{Z}$ $Z = \frac{V}{I}$

$I = 35.36$ $V = 35.36 \times 15$
 $R = 15$ $V = 530.4 \text{ V}$

$Z = \frac{530.4}{35.36}$

$Z = 15 \Omega$

(iv) power factor $\cos \phi$

$\phi = \tan^{-1} \left(\frac{X_L}{R} \right)$ $\phi = \tan^{-1} \left(\frac{12}{15} \right)$

$\phi = 0.099$

$\text{pf} = \cos(0.099)$

$\text{PF} = 0.9951$

$$V = 200 \sin 377t \text{ Volts}$$

$$i = 8 \sin(377t - 30^\circ) \text{ A}$$

Determine p.f., true p, apparent p, reactive p also the power Δ

* A voltage $e = 200 \sin(100\pi t)$ is applied to a coil having $R = 200 \Omega$ and $L = 0.38 \text{ H}$. Determine the expression of current and power taken by coil.

mg $\Rightarrow$ given $e = 200 \sin(100\pi t)$

$$R = 200 \Omega, L = 0.38 \text{ H}$$

$$I = ?, P = ?$$

$$V_m = 200$$

$$I = \frac{V_m}{Z}, Z = \sqrt{R^2 + (X_L)^2} \quad \omega = 100\pi$$

$$X_L = 2\pi fL$$

$$f = 100 \text{ Hz}$$

$$f = 50 \text{ Hz}$$

$$X_L = 2\pi \times 50 \times 0.38 \text{ H}$$

$$X_L = 119.38 \text{ H}$$

$$Z = \sqrt{40000 + 14251.58}$$

$$Z = \sqrt{54251.58}$$

$$Z = 232.91$$

$$I = \frac{200}{232.91}$$

$$I = 0.858 \text{ A}$$

$$I = 0.858 \text{ A}$$

$$P = I^2 R$$

$$P = 0.73736 \times 200$$

$$P = 147.47 \text{ watt}$$

~~$$\cos \phi = \frac{R}{Z} = \frac{200}{232.91} = 0.858$$~~

Q. A 230V, 50Hz AC supply is applied to a coil of 0.06 H (inductance) and 2.5Ω (resistance) connected in series with a $6.8 \mu\text{F}$ capacitor. Calculate (a) Impedance (Z) (b) current (I) (c) Phase Angle (ϕ) (d) Power factor (e) power consumed

→ Given $V = 230$, $f = 50\text{Hz}$, $L = 0.06\text{H}$
 $R = 2.5 \Omega$, $C = 6.8 \mu\text{F}$ $C = 6.8 \times 10^{-6}\text{F}$

$$Z = \sqrt{R^2 + (X_L - X_C)^2} \quad X_L = 2\pi fL \quad \boxed{X_L = 18.84}$$

$$X_C = \frac{1}{2\pi fC} \quad \boxed{X_C = 2.13} \quad Z = \sqrt{6.25 + 16.71}$$

$$\boxed{Z = 4.79} \quad I = \frac{V}{Z} \quad I = \frac{230}{4.79}$$

$$\boxed{I = 48\text{A}}$$

$$\phi = \tan^{-1} \left(\frac{X_L - X_C}{R} \right) \quad \phi = \tan^{-1} \left(\frac{16.71}{2.5} \right)$$

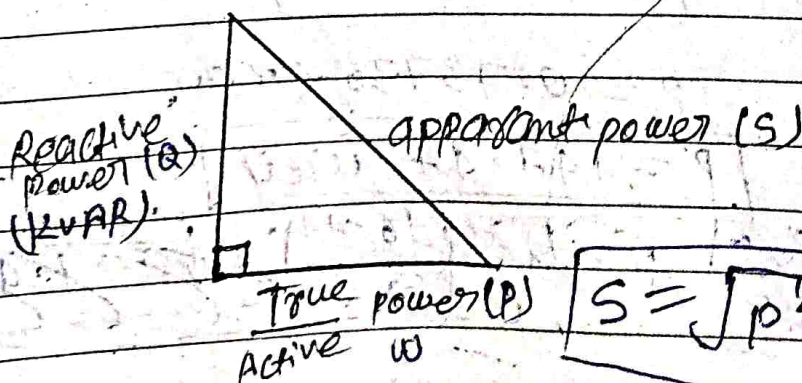
$$\phi = \tan^{-1} (6.684) \quad \boxed{\phi = 81.99}$$

$$\text{PF} = \cos \phi \quad \boxed{\text{PF} = 0.147}$$

$$\text{Power consumed} = I^2 R = 5760 \text{ watt}$$



Draw the power triangle



$$\boxed{S = \sqrt{P^2 + Q^2}}$$

* $V = 200 \sin 377t$ Volts, $i = 8 \sin(377t - 30^\circ)$ A

Determine (i) p.f., (ii) True power (iii) Apparent p
(iv) Reactive p (v) Power

$i_m = 8$

$V_m = 200$

p.f. = $\cos \phi$

$\omega = 377$

$PF = \frac{\sqrt{3}}{2}$

$[PF = 0.866]$

$\phi = 30^\circ$

(ii) True power $\rightarrow VI \cos \phi$ (iv) $AP = VI \sin \phi$

$TP = 200 \times 8 \times 0.866$

$RP = 200 \times 8 \times \frac{1}{2}$

$TP = 240 \text{ Watt}$

$RP = 800$

$[RP = 800 \text{ mVAR}]$

$Q = 800$

(iii) Apparent p $\rightarrow S =$

$S = \sqrt{P^2 + Q^2}$

$S = \sqrt{57600 + 640000} \Rightarrow S = \sqrt{697600}$

$[S = 835.22 \text{ VA}]$

* $V = 100 \sin 314t$, $R = 25 \Omega$, $C = 80 \mu\text{f}$ determine

(i) Peak value of I (ii) p.f. (3) Total power consumed

Peak val = MAX I
of I

given

$V_m = 100$

$\omega = 314$

$R = 25 \Omega$

$C = 80 \times 10^{-6} \text{ f}$

$f = 50 \text{ Hz}$

$\omega C = \frac{1}{2\pi f C}$

$\omega C = 40$

$\phi = \tan^{-1} \left(\frac{-\omega C}{R} \right)$

$\phi = \tan^{-1} \left(\frac{-40}{25} \right)$

$\phi = -1.107$

$I_m = \frac{V_m}{R}$

$I_m = \frac{100}{25}$

$I_m = 4 \text{ A}$

p.v. = $\frac{4 \text{ A}}{0.866}$

$p.v. = 4.61$

$\phi = \tan^{-1} \left(\frac{-40}{25} \right)$

$\phi = -1.107$

$\phi = -1.107$

$\cos \phi$

$\cos \phi = 0.53$

$P = I^2 R$

$P = 16 \times 25 = 400 \text{ Watt}$

$P = 400 \text{ Watt}$

$P = 400 \text{ Watt}$

- Q. $R = 10\Omega$ $L = 50\text{mH}$ $C = 100\mu\text{F}$ $V = 200\text{V}$
 $f = 50\text{Hz}$ (i) Z (ii) pf (iii) I (iv) P
 (v) voltage drop across each element.

$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$X_L = 2\pi fL \quad X_L = 2 \times \pi \times 50 \times 50 \times 10^{-3}$$

$$X_L = 15.70\Omega$$

$$X_C = \frac{1}{2\pi fC} \quad X_C = \frac{1}{2 \times \pi \times 50 \times 100 \times 10^{-6}}$$

$$X_C = 32.25\Omega$$

$$Z = \sqrt{100 + 273.90}$$

$$Z = \sqrt{373.90} \quad Z = 19.33\Omega$$

$$I = \frac{V_m}{Z} \quad I = \frac{200}{19.33} \quad I = 10.34\text{A}$$

$$\phi = \tan^{-1} \left(\frac{X_L - X_C}{R} \right) \quad \phi = \tan^{-1} \left(\frac{-16.55}{10} \right)$$

$$\phi = \tan^{-1}(-1.65)$$

$$\phi = -1.025$$

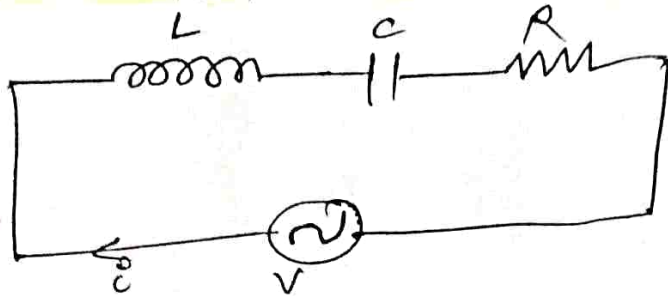
$$\text{pf} = 0.51$$

$$P = I^2 R$$

$$P = 1069.15 \text{ Watt}$$

* What is resonance? When the value of inductive and capacitive reactances have equal magnitude but phase difference is 180° is called resonance.

* Resonance in RLC circuit



∴ Resonance $X_L = X_C$

① $Z = \sqrt{R^2 + (X_L - X_C)^2} \Rightarrow Z = \sqrt{R^2 + (X_L - X_C)^2} \Rightarrow \boxed{Z = R}$

② $Z = R$ impedance minimum

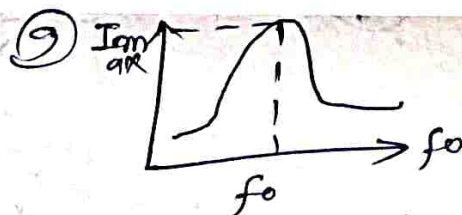
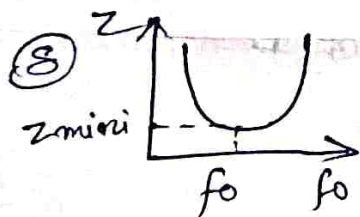
③ $V = \frac{I}{Z}$ $V = \frac{I}{R}$ ④ $I = \text{maximum}$

⑤ $\vec{I} \rightarrow \vec{V}$ pure resistive circuit in phase

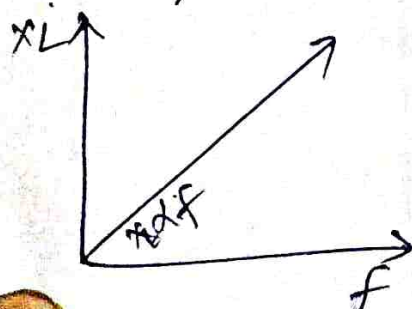
⑥ power factor $\cos 0^\circ = 1$ $X_L = \cancel{X_C}$

⑦ resonance frequency $\Rightarrow \omega L = \frac{1}{\omega C}$
 $\omega_0^2 = \frac{1}{LC}$ $\omega_0 = \frac{1}{\sqrt{LC}}$

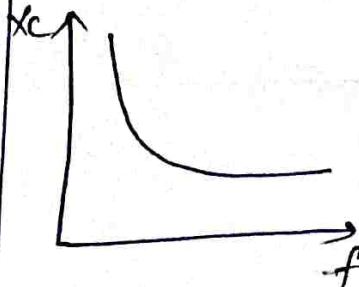
$2\pi f_0 = \frac{1}{\sqrt{LC}}$ $\omega_0 = 2\pi f_0$
 $\boxed{f_0 = \frac{1}{2\pi\sqrt{LC}}}$ resonance frequency



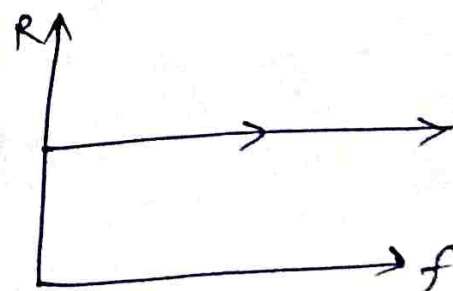
$X_L = \omega L = 2\pi f L$
 $X_L \propto f$



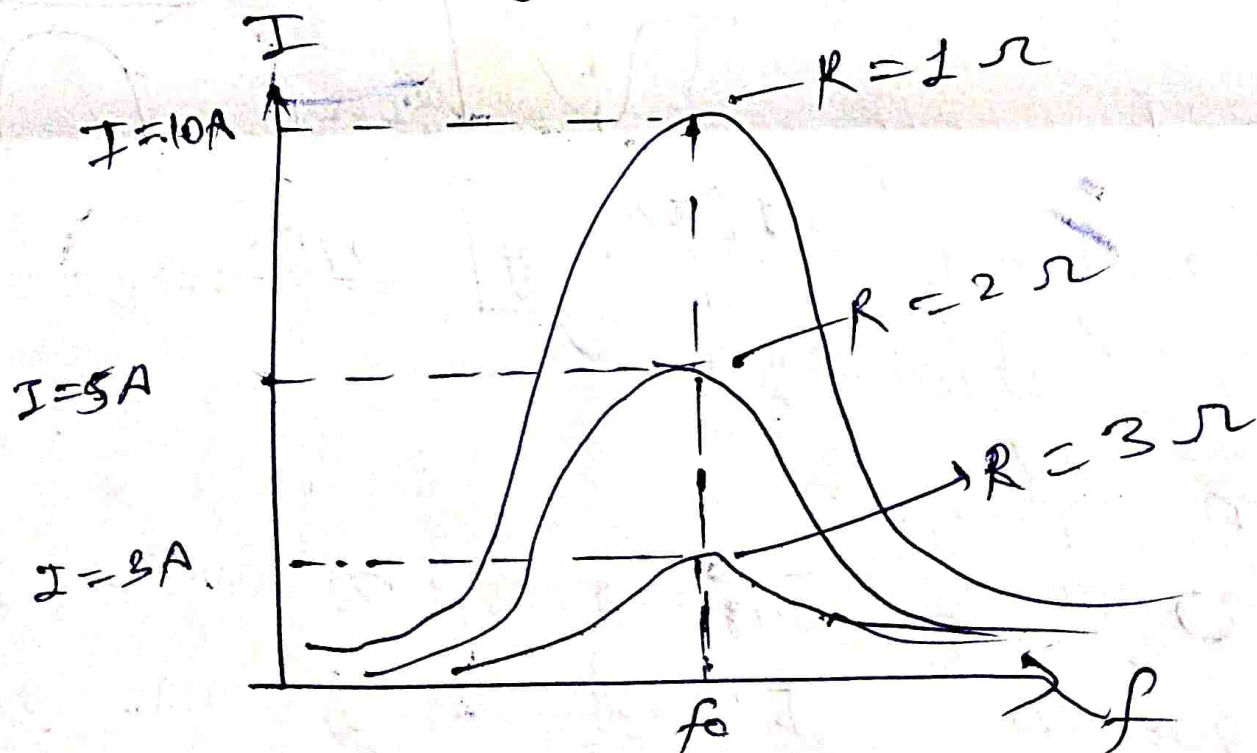
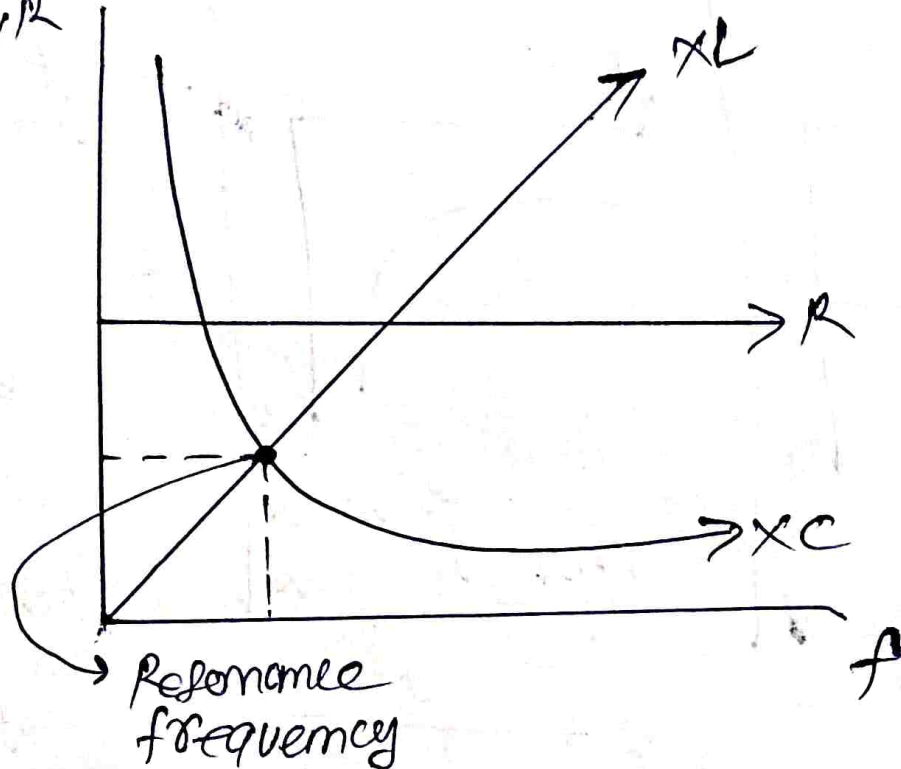
$X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C}$
 $X_C \propto \frac{1}{f}$



$R \rightarrow \text{constant}$



X_L, X_C, R



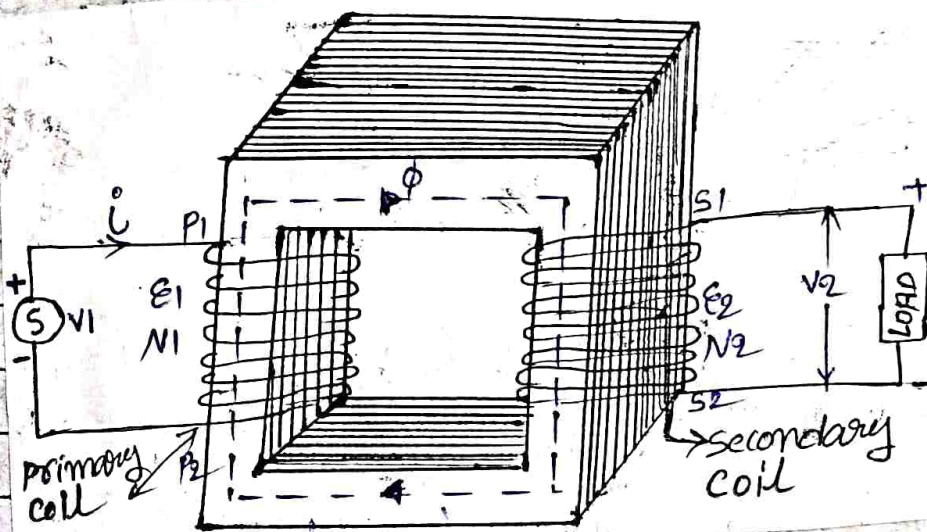
Transformer

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(Q.10) Describe the constructional details of transformer and working principle and E.M.F equation. Efficiency of a transformer & condition for maximum value of efficiency.

Introduction :- Transformer is a device which is used to step-up and step-down the input voltage. It is called transformer.



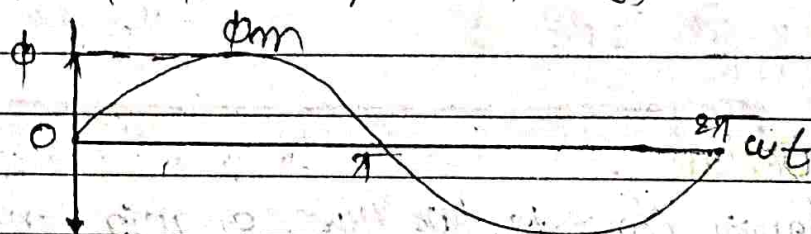
Construction :- $\rightarrow$ Core (magnetic material).

Transformer consists two types of windings and a laminated steel core, two windings are placed on a magnetic core insulated from each other and ~~this~~ steel core is ~~insulate~~ laminated and made of thin sheets of silicon. This arrangement of core diminishes the eddy current loss. There are two types of winding one is called primary winding (P_1 & P_2) and other is called secondary winding (S_1 & S_2) placed on core. N_1 and N_2 be the no of turns in primary & secondary winding. AC input is given to primary winding & AC output taken by secondary winding.

Working principle of transformer

∴ A transformer works on the principle of mutual ~~electromagnetic~~ induction, when an alternative voltage (v_i) is applied to the primary winding then current (i) flows through it and this current produces flux (φ) in the core which links with primary and secondary windings. The flux self-induces emf (E₁) in primary winding and the flux mutually induces emf (E₂) in secondary winding according to the Faraday's laws of electromagnetic induction. After this current will start flowing in the secondary winding.

EMF Equation of A Transformer ∴



$$\phi = \phi_m \sin \omega t \quad \text{--- (1)}$$

by Faraday's law of electromagnetic induction

$$E = N \frac{d\phi}{dt}$$

by Lenz's law

$$E = -N \frac{d\phi}{dt} \quad \text{--- (2)}$$

So, EMF induced in primary winding
Part ① E_1 (in) 2

$$E_1 = -N \frac{d(\phi_m \sin \omega t)}{dt}$$

$$E_1 = -N \cdot \phi_m \cdot \omega \cos \omega t$$

$$\text{at } t = 0$$

$$E_1 = N \phi_m \cdot \omega (\cos \omega t) \quad \text{--- (4)}$$

$$\therefore \cos \theta = \sin\left(\frac{\pi}{2} - \theta\right)$$

mul $(-)$ both side

$$-\cos \theta = -\sin\left(\frac{\pi}{2} - \theta\right)$$

$$\left\{ \begin{array}{l} -\sin \theta = \sin(-\theta) \end{array} \right.$$

$$\boxed{-\cos \omega t = \sin(\omega t - 90^\circ)} \quad \text{--- (3) put in (4)}$$

$$E_1 = N \phi_m \cdot \omega (\sin(\omega t - 90^\circ))$$

$$E_1 = N \cdot \phi_m \cdot 2\pi f \sin(\omega t - 90^\circ)$$

comparing with

$$E_1 = E_{m1} \sin(\omega t + 0) \quad \checkmark$$

$$E_{m1} = N \phi_m \cdot 2\pi f$$

So RMS value of $e_{m \cdot f} = \frac{E_{\max} \text{ value}}{\sqrt{2}}$

$$E_1 = \frac{N \phi_m \cdot 2\pi f}{\sqrt{2}} \Rightarrow E_1 = \frac{2\pi \cdot N \phi_m f}{\sqrt{2}} \therefore \left\{ \frac{2\pi \cdot 4.4}{\sqrt{2}} \right.$$

$$\boxed{E_1 = 4.44 \phi_m f \cdot N_1} \quad \checkmark$$

similarly for secondary winding

$$\boxed{E_2 = 4.44 \phi_m f N_2}$$

$$\text{Transformation ratio } \left[K = \frac{V_2}{V_1} = \frac{E_2}{E_1} = \frac{N_2}{N_1} = \frac{I_1}{I_2} \right]$$

*** Losses in a transformer:**

→ ① Core loss or iron loss

(i) hysteresis loss

(ii) eddy current loss

→ ② Copper loss

(1) Core loss or iron loss $\div$ Core loss or iron loss consists both of the losses hysteresis loss and eddy current loss

(i) Eddy current loss $\div$ Due to apply Alternative current in Core of transformer there are produced eddy currents in core by which energy losses in the form of heat is called eddy current loss in order to diminish the losses we should use ~~thick~~ thin sheets of Silicon for core so we can diminish the energy loss.

$$P_e = K B^2 f^2 t^2 W$$

(ii) Hysteresis loss $\div$ Due to apply Alternative current in core of transformer, core ~~is~~ getting frequently magnetized and de-magnetized so energy gets loss is called hysteresis loss. $P_h = \eta B^2 f V$ $\rightarrow \eta \rightarrow$ constant of the core
 $B \rightarrow$ flux density

(2) Copper loss $\div$ The winding of the transformer is made of copper wire, so it has some resistance due to this resistance electrical energy is converted into heat energy this is called copper loss.

$$P_{cu} = I_1^2 R_1 + I_2^2 R_2$$

EFFICIENCY of a Transformer : efficiency of a transformer is the ratio of input power and output power. It is denoted by η .

$$\eta = \frac{\text{output power}}{\text{input power}} = \frac{\text{output power}}{\text{output power} + \text{losses}}$$

$$\eta = \frac{\text{output power}}{\text{output power} + \text{iron loss} + \text{copper loss}}$$

$$\eta = \frac{V_2 I_2 \cos \phi_2}{V_2 I_2 \cos \phi_2 + I_2^2 R_2 + P_i} \quad \text{--- (A)}$$

Condition for maximum value of efficiency

diff eq. (A) w.r.t. I_2 Note: P_i is constant, and I_2 variable. and all are constant

$$\frac{d\eta}{dI_2} = \frac{(V_2 I_2 \cos \phi_2 + I_2^2 R_2 + P_i)(V_2 \cos \phi_2) - V_2 I_2 \cos \phi_2 (V_2 \cos \phi_2 + 2I_2 R_2 + 0)}{(V_2 I_2 \cos \phi_2 + I_2^2 R_2 + P_i)^2}$$

To get max efficiency put $\frac{d\eta}{dI_2} = 0$

$$(V_2 I_2 \cos \phi_2 + I_2^2 R_2 + P_i) V_2 \cos \phi_2 - V_2 I_2 \cos \phi_2 (V_2 \cos \phi_2 + 2I_2 R_2) = 0$$

$$V_2 \cos \phi_2 (V_2 I_2 \cos \phi_2 + I_2^2 R_2 + P_i) - V_2 I_2 \cos \phi_2 (V_2 \cos \phi_2 + 2I_2 R_2) = 0$$

$$V_2 \cos \phi_2 (V_2 I_2 \cos \phi_2 + I_2^2 R_2 + P_i - I_2 V_2 \cos \phi_2 - 2I_2^2 R_2) = 0$$

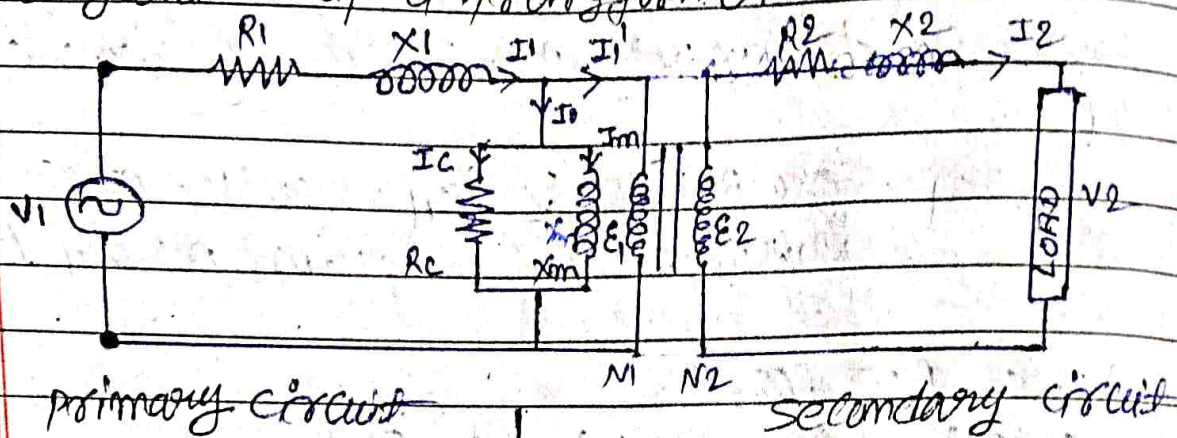
$$P_i - I_2^2 R_2 = 0$$

$$P_i = I_2^2 R_2 \quad \left\{ (P_i = \text{iron losses} \& I_2^2 R_2 \rightarrow \text{copper losses}) \right\}$$

$\therefore$ copper losses & iron losses is equal, so we can say that from the above expression (maximum value of efficiency).

(PQ)

Draw equivalent circuit of a transformer and regulation of a transformer.



$V_1 \rightarrow$ AC V supply

$I_1 \rightarrow$ primary current

$R_1 \rightarrow$ resistance of primary winding

$X_1 \rightarrow$ leakage reactance of primary winding

$I_0 \rightarrow$ No load current

$I_m \rightarrow$ magnetisation current

$X_m \rightarrow$ magnetisation reactance

$I_c \rightarrow$ core loss current

$R_c \rightarrow$ core resistance

$E_1 \rightarrow$ primary induced emf

$R_2 \rightarrow$ resistance of secondary winding

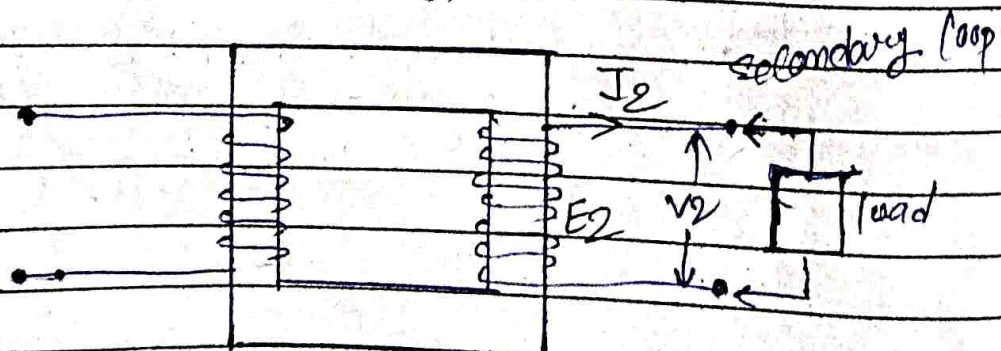
$X_2 \rightarrow$ leakage reactance of secondary winding

$I_2 \rightarrow$ load current

$V_2 \rightarrow$ load voltage

$E_2 \rightarrow$ secondary induced emf

* regulation of a transformer:



No load $\rightarrow E_2$ or V_{2NL}

on load $\rightarrow V_2$

$V_2 \neq V_{NL}$

Regulation of a transformer $\div$ The change in Secondary terminal voltage from No load to full load with respect to No load ~~voltage~~ to full load with respect to No load voltage, when primary voltage is kept constant.

$V_2 \rightarrow$ Secondary terminal voltage at any load

$E_2 \rightarrow$ Secondary terminal voltage at No load

$$\text{Voltage Regulation} = \frac{E_2 - V_2}{E_2} \times 100 \quad \text{--- (B)}$$

Apply KVL in Secondary loop

$$V_2 = E_2 - I_2 Z_2$$

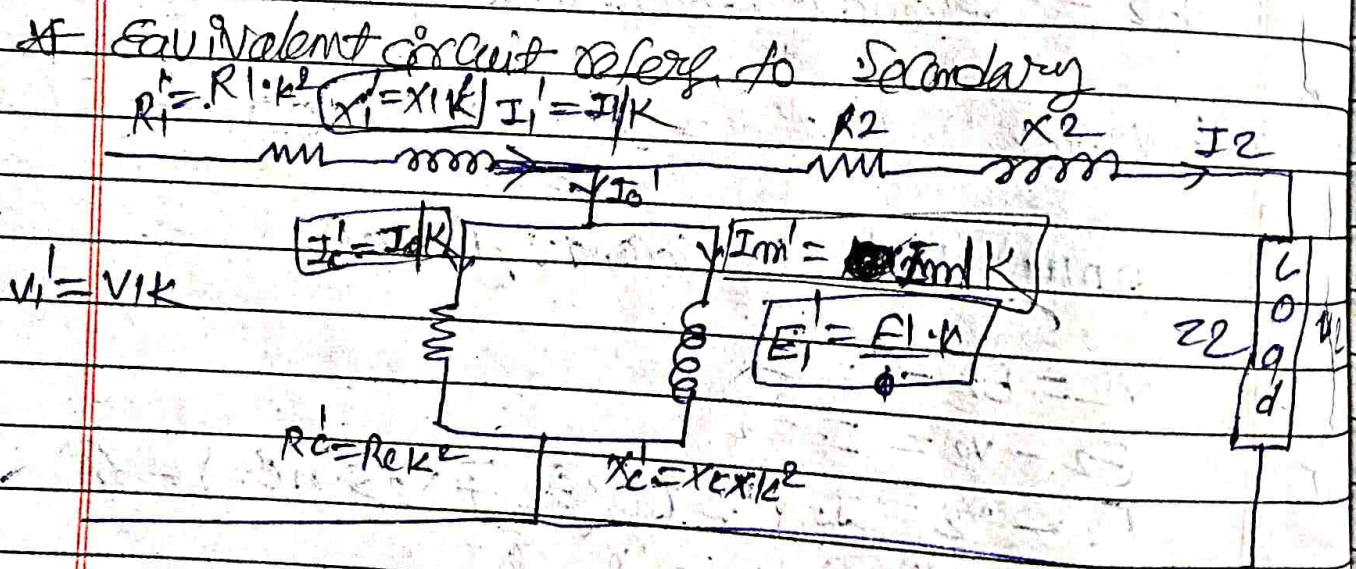
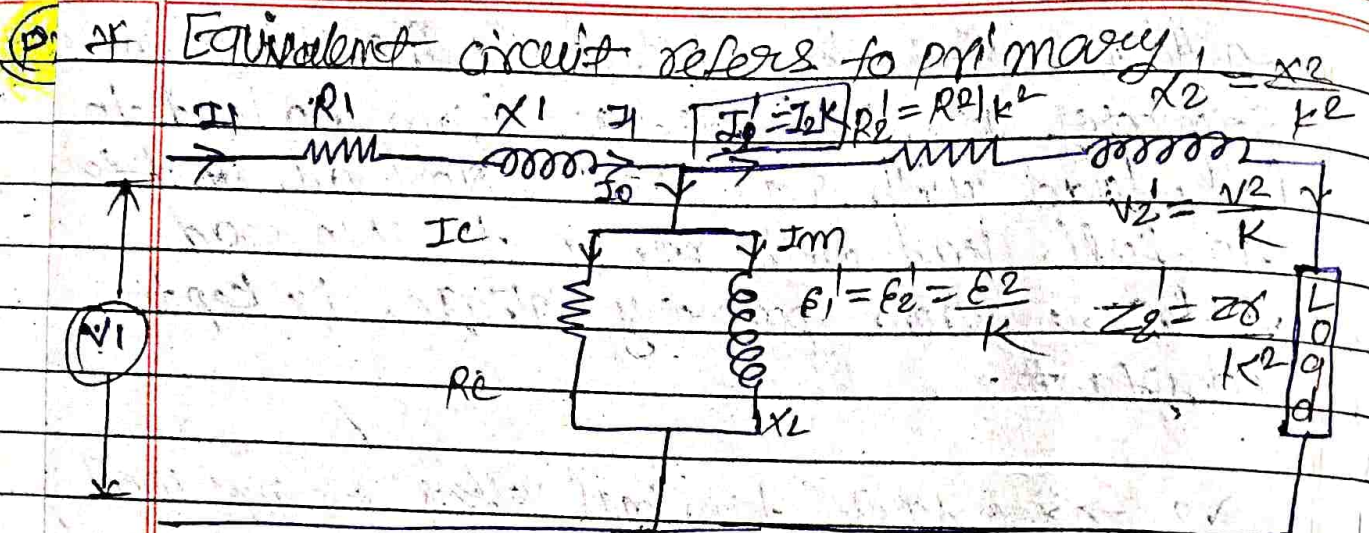
$$E_2 - V_2 = I_2 Z_2$$

$$E_2 - V_2 = I_2 (R_2 \cos \theta_2 \mp X_2 \sin \theta_2) \quad \text{--- (A)}$$

eqⁿ (A) put in (B)

$$VR = \frac{I_2 R_2 \cos \theta_2 \pm I_2 X_2 \sin \theta_2}{E_2} \times 100$$

$$VR = \left[\frac{I_2 R_2 \cos \theta_2 \pm I_2 X_2 \sin \theta_2}{E_2} \right] \times 100$$



$$T_{\phi} \rightarrow \frac{V_1}{V_2} = \frac{E_1}{E_2} = \frac{N_1}{N_2} = \frac{I_2}{I_1} = K$$

~~Capacity KVA rating = $\frac{V_1 I_1}{1000}$~~

Note $\rightarrow$ Connected $\frac{3000}{V_1}$ या E_1 होगा
load voltage $\frac{3000}{V_2}$ या E_2 होगा

$$\text{full load current} = \frac{\text{KVA rating} \times 1000}{E_1 \text{ or } V_1}$$

KVA rating means $\rightarrow$ capacity

* A 25 KVA lossless transformer has 500 turns on primary and 40 turns on secondary the primary is connected to 3000V, 50 Hz mains. determine

- (i) primary and secondary current at full load.
 (ii) The secondary emf
 (iii) The maximum flux in the core
- Given $N_1 = 500$
 $N_2 = 40$
 $V_1 = 3000V$
 $f = 50 \text{ Hz}$

$$\text{load current} = \frac{\text{KVA} \times 1000}{V_1} = \frac{25 \times 1000}{3000} = 8.3 \text{ A}$$

for primary current

primary load current = 8.3 A
 and secondary = 103.75

$$\frac{N_1}{N_2} = \frac{V_1}{V_2}$$

$$\frac{500}{40} = \frac{3000}{V_2} \Rightarrow V_2 = \frac{3000 \times 40}{500} = 240V$$

$$V_2 = 240V$$

load current for

$$\text{secondary current} = \frac{25 \times 1000}{240} = 104.16 \text{ A}$$

$$\frac{V_1}{V_2} = \frac{I_2}{I_1}$$

$$I_2 = \frac{V_1 I_1}{V_2} = \frac{3000 \times 8.3}{240} = 103.75$$

(ii)

$$E_2 = ? \quad \therefore \frac{N_1}{N_2} = \frac{E_1}{E_2}$$

$$\frac{500}{40} = \frac{3000}{E_2}$$

$$\therefore V_1 = E_1 = 3000$$

$$E_2 = \frac{3000 \times 40}{500}$$

$$E_2 = 60 \times 4$$

$$E_2 = 240 \text{ V}$$

(iii)

Maximum flux $\rightarrow$

$$E_1 = 4.44 \phi_m f N_1$$

$$3000 = 4.44 \phi_m \times 50 \times 500$$

$$\phi_m = \frac{3000}{4.44 \times 25000} = 3$$

$$\phi_m = 0.027 \text{ wb / weber}$$

* The emf per turn of a single phase LVN, 2200/220V, 50Hz, transformer is 10V calculate N_1 and N_2 , net cross sectional area of core for a maximum flux density of 1.5 T.

ans $\Rightarrow$

$$\text{Rating} \Rightarrow 10$$

$$N_1 ?$$

$$N_2 ?$$

$$E_1 = 2200 \text{ V}$$

$$E_2 = 220 \text{ V}$$

$$f = 50 \text{ Hz}$$

$$B = 1.5 \text{ T}$$

$$E_1 = 4.44 \phi_m f N_1$$

$$\therefore B = \frac{\phi}{a} \quad \phi = Ba$$

N_1 = emf per turn of a single phase

$$N_1 = \frac{2200}{10} \quad N_1 = 220$$

$$N_2 = \frac{220}{10}$$

$$N_2 = 22$$

$$N_2 = 22$$

$$B = \frac{\Phi}{A}$$

$$A = \frac{\Phi}{B}$$

$$E = 4.44 \Phi_m \cdot f \cdot N$$

$$2200 = 4.44 \times \Phi_m \times 50 \times 820$$

$$\Phi_m = \frac{2200}{4.44 \times 50 \times 820}$$

$$\Phi_m = \frac{22}{488.4} \quad \Phi_m =$$

$$\Phi_m = 0.0450 \text{ wb}$$

$$A = \frac{0.0450}{1.5}$$

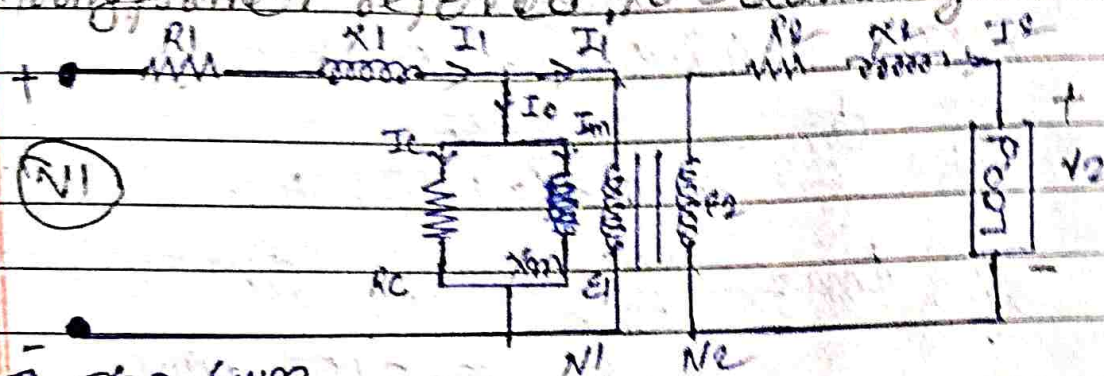
$$A = 0.03 \text{ m}^2$$

आप चाहे तो ये डाई भी देख सकते हैं
चाहे तो जरूर की समझें वें सर्य ही हैं

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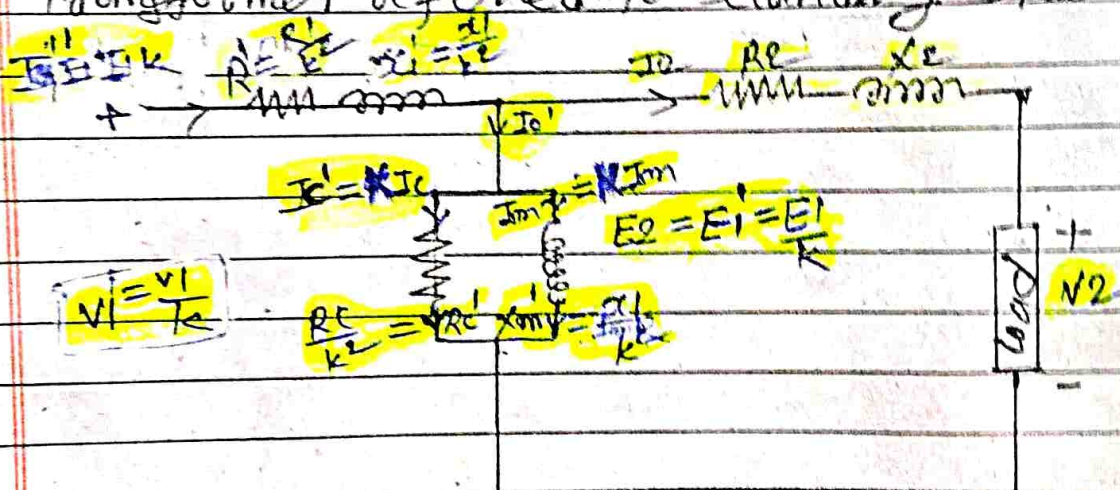
QYQ Draw an equivalent circuit and derive circuit parameters of conventional two winding transformer referred to secondary side.



Step down

$N1:N2$

Transformer referred to secondary side



in primary
 $\therefore \frac{V1}{V2} = \frac{N1}{N2} = k$

in secondary side
 $\frac{V1}{V2} = \frac{N1}{N2} \therefore k = \frac{N1}{N2}$

$V1' = \frac{V1}{k}$

in P.S $R1$ in S.S $\rightarrow R1' = \frac{1}{k^2} R1$

$X1$ $X1'$ $X1' = \frac{1}{k^2} X1$ P.S $I1$ S.S $I1''$

Xm Xm' $Xm' = \frac{1}{k} Xm$ $\frac{I1''}{I1} = \frac{N1}{N2} = k$

Rc Rc' $Rc' = \frac{1}{k^2} Rc$ $I1'' = I1 k$

p.s

E_1

$$\frac{E_1}{E_1'} = \frac{N_1}{N_2} = K$$

I_{m1}

$$I_{m1}' = I_{m1} K$$

I_c

$$I_c' = I_c K$$

s.s

E_1'

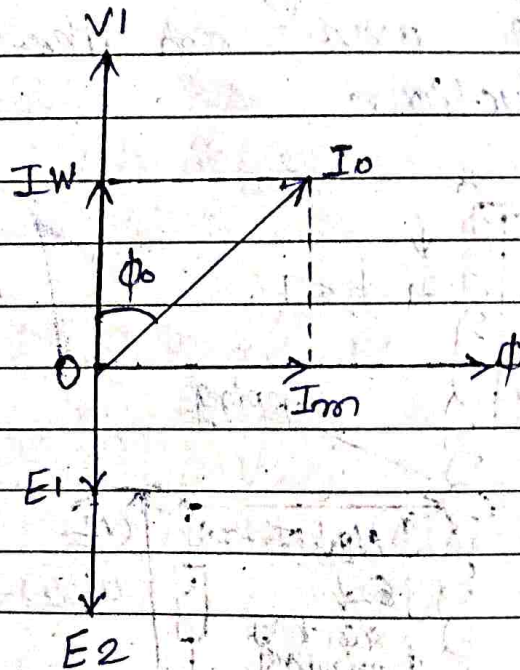
$$E_1' = E_1$$

I_{m1}'

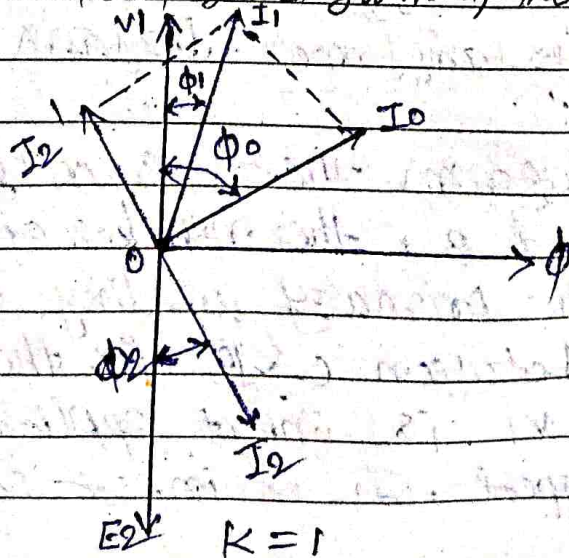
I_c'

Q.10 Draw the complete phasor diagram of the transformer under no load conditions.

Sol:



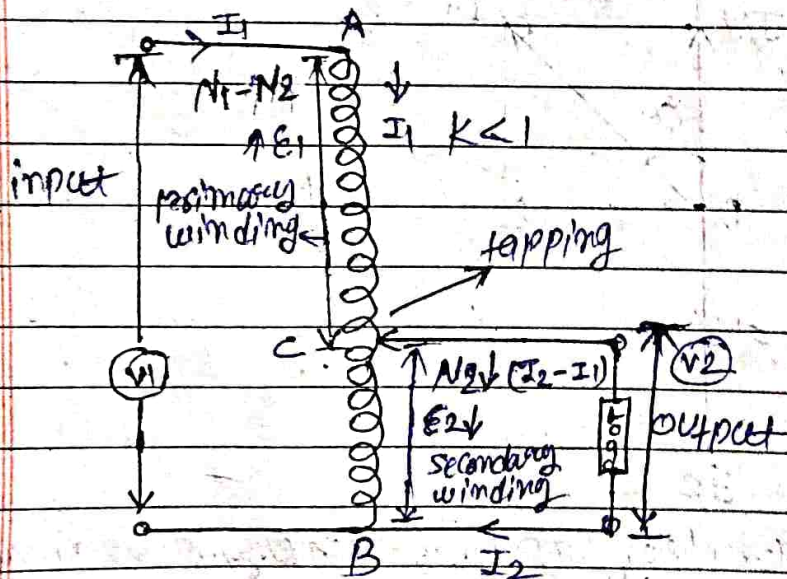
Q.11 Draw the complete phasor diagram of the transformer under on load



Q.10

what do you understand by autotransformer? Explain construction and working principle of an auto transformer. How it's different from conventional two winding transformer.

Ans. An auto transformer is a transformer with only one winding placed on a laminated core. And auto transformer is similar to a two winding transformer but differ in the way the primary and secondary winding are interrelated. Auto transformer works on the principle of self-induction.



Auto transformer - diagram

Construction :-

In the diagram there is only one winding between A and B, the number of turns between A & C is the primary winding and the number of turns between C & B is the secondary winding. V_1 is input applied voltage and V_2 is output, I_1 is input current and I_2

is output current, emf is induced in primary side E_1 and secondary side E_2 and a tapping is done over c point.

Principle $\div$ Auto transformer works on the principle of self-induction.

Working $\div$ The working of autotransformer is similar to the conventional transformer, in ~~that~~ the autotransformer when current is applied to the input side primary winding of autotransformer it creates magnetic field that induces a ^{emf} ~~voltage~~ in the secondary winding and current flows through secondary winding.

Advantage $\div$

- ① Small in size
- ② lower weight
- ③ higher efficiency
- ④ voltage control as per requirement

Ques Difference between auto transformer and conventional two winding transformer.

Auto transformer	conventional transformer
------------------	--------------------------

(i) It has only one winding	It have two winding.
-----------------------------	----------------------

(ii) Voltage is induced due to self induction	voltage is induced due to mutual induction.
---	---

(iii) Voltage can be changed as our requirement	voltage cannot change as our requirement.
---	---

(iv) losses are very low	losses are very high.
--------------------------	-----------------------

(v) output voltage is variable.	output voltage is constant.
---------------------------------	-----------------------------

(vi) cos is very less	cost is very high
-----------------------	-------------------

*** Transformer efficiency**

$$\eta = \frac{n \times VA \text{ rating} \times \cos \phi}{n \times VA \text{ rating} \times \cos \phi + P_i + n^2 \times P_{cu}} \times 100$$

(1) 1KVA, single phase transformer has core loss of ~~15~~ 15 watt and full load cu losses 20 watt calculate the efficiency

(i) full load 0.9 pf (lag)

(ii) Half full load unity power factor

(iii) 3/4 full load 0.707 pf (lag or lead)

① Given Varying = 1000
 $P_i = 15 \text{ watt}$
 $P_{CV} = 20 \text{ watt}$
 $P_f = 0.9 \text{ (lag)}$
 $\eta = ?$

$$\eta = \frac{1 \times 1000 \times 0.9 \times 100}{1000 \times 0.9 + 15 + 20}$$

~~$$\eta = \frac{90000}{9000 + 300} \quad \eta = \frac{90000}{9300}$$

$$\eta = \frac{90000}{10000}$$~~

$$\eta = \frac{900 \times 100}{900 + 300 + 20} \quad \eta = \frac{900 \times 100}{935}$$

$$\eta = \frac{900}{935} \times 100 = 0.9625 \times 100$$

$$\boxed{\eta\% = 96.25\%}$$

② $\eta = \frac{0.5 \times 1000 \times 1}{0.5 \times 1000 \times 1 + 15 + 20 \times (0.5)^2} \times 100$

$$\eta = \frac{500 \times 100}{560} \quad \eta = 0.8928 \times 100$$

$$\boxed{\eta\% = 89.28\%}$$

③ $\eta = \frac{0.75 \times 1000 \times 0.707}{0.75 \times 1000 \times 0.707 + 15 + 20 \times 0.5625} \times 100$

$$\eta = \frac{530.25}{530.25 + 26.25} \times 100 \quad \eta = \frac{530.25}{556.5} \times 100$$

$$\eta = 0.9360 \times 100$$

$$\boxed{\eta = 93.60\%} \quad \text{lead}$$

Q2) 3300/110V, 50Hz, 60kVA single phase transformer has iron losses of 600 watts. Primary and secondary winding resistances are 3.3 ohm and 0.011 ohm respectively. Determine the efficiency of the transformer on full load at 0.8 lag pf load.

Sol: Given: $V_1 = 3300V$, $KVA = 60$, $f = 50Hz$, $R_1 = 3.3\Omega$,
 $V_2 = 110V$, $R_2 = 0.011\Omega$
 $P_i = 600W$, $\cos\phi (pf) = 0.8$ lag

$$\therefore \% \eta = \frac{\eta \times V_A \times \text{rating} \times pf}{\eta \times V_A \times \text{rating} \times pf + P_i + P_{cu} \times \eta^2}$$

$P_{cu} = \text{primary copper loss} + \text{secondary copper loss}$

$$P_{cu} = I_1^2 R_1 + I_2^2 R_2$$

$\therefore$ full load current = $\frac{KVA \text{ rating} \times 1000}{V_1}$

$$I_1 = \frac{60 \times 1000}{3300} \Rightarrow I_1 = 18.18A$$

$$I_2 = \frac{60 \times 1000}{110} \Rightarrow I_2 = 545.45A$$

$$P_{cu} = (18.18)^2 \times 3.3 + (545.45)^2 \times 0.011$$

$$P_{cu} = 3272.72 + 330.51 \times 3.3$$

$$P_{cu} = 3272.72 + 1090.62092$$

$$P_{cu} = 4363.41 \text{ Watt on full load}$$

$$\therefore \% \eta = \frac{1 \times 60 \times 1000 \times 0.8}{60 \times 1000 \times 0.8 + 600 + 4363.41} \times 100$$

$$\therefore \% \eta = 90.62\%$$

Q. In a 50 kVA transformer, the iron loss is 500 W and full load copper loss is 800 W. Find the efficiency at full load and half load at 0.8 pf lag.

Given $V_{A \text{ rating}} = 50 \times 1000$

$$P_i = 500 \text{ W}$$

$$n_1 = 1$$

$$P_{cu} = 800 \text{ W}$$

$$n_2 = \frac{1}{2} = 0.5$$

$$PF = 0.8$$

$$\eta = \frac{9.1 \times 50000 \times 0.8}{50000 \times 0.8 + 800 + 800 \times 1^2} \times 100$$

$$\% \eta = \frac{4000}{4000 + 1600} \times 100 \Rightarrow \frac{4000}{5600} \times 100$$

$$\% \eta = 0.7547 \times 100$$

$$\boxed{\% \eta = 75.47\%}$$

(ii) at half load

$$\% \eta = \frac{0.5 \times 50000 \times 0.8}{0.5 \times 50000 \times 0.8 + 500 + 800 \times (0.5)^2} \times 100$$

$$\% \eta = \frac{20000}{20000 + 500 + 200} \times 100$$

$$\% \eta = \frac{20000}{20700} \times 100 \Rightarrow \% \eta = 0.9661 \times 100$$

$$\boxed{\% \eta = 96.61\%}$$

Nomericale on refers to primary & secondary.

for primary $\rightarrow$

equivalent resistance $\rightarrow R_{eq}$

equivalent reactance $\rightarrow X_{eq}$

$$R_{eq} = R_1 + R_2'$$

$$R_{eq} = R_1 + R_2/k^2$$

$$R_{01} = R_2/k^2$$

where

$$k = \frac{V_2}{V_1}$$

$$X_{eq} = X_1 + X_2'$$

$$X_{01} = X_2/k^2$$

k transformer ratio

total equivalent

for secondary $\rightarrow$

equivalent resistance

$$R_{eq} = R_2 + R_1'$$

$$R_{02} = R_1/k^2$$

$$k = \frac{V_2}{V_1}$$

$$X_{02} = X_1/k^2$$

total equivalent

pyq

A 400/200, 50 Hz, 10 kVA transformer has primary and secondary winding resistance of 2.5Ω and 0.5Ω and winding leakage reactance of 5Ω and 1Ω respectively. find the equivalent resistance and reactance referred to secondary side.

Given $\Rightarrow V_1 = 400V, R_1 = 0.5 \Omega$
 $V_2 = 200V, R_2 = 0.5 \Omega$
 $X_1 = 5 \Omega$
 $X_2 = 1 \Omega$

$$R_{eq} = R_1 + R_2'$$

$$R_{02} = R_1 / k^2$$

$$k = \frac{V_2}{V_1}$$

$$k = \frac{200}{400}$$

$$k = \frac{1}{2} \quad [k = 0.5]$$

$$R_{02} = 2.5 / 0.25$$

$$R_{02} = 10 \Omega$$

$$R_{02} = 10 \Omega$$

$$R_{eq} = 10 \Omega$$

$$X_{2eq} = X_2 + X_1'$$

$$X_{02} = X_2 + X_1 / k^2$$

$$[k = 0.5]$$

$$X_{02} = 1 + 5 / 0.25$$

$$X_{02} = 21 \Omega$$

$$X_{02} = 21 \Omega$$

Q70) A 100 kVA, 1100/200 volt single phase transformer has the following parameters $R_1 = 0.1 \Omega$, $X_1 = 0.3 \Omega$, $R_2 = 0.004 \Omega$, $X_2 = 0.012 \Omega$ find equivalent resistance and leakage reactance referred to primary side.

Ans) Give $\Rightarrow R_1 = 0.1 \Omega, X_1 = 0.3 \Omega, V_1 = 1100V$
 $R_2 = 0.004 \Omega, X_2 = 0.012 \Omega, V_2 = 200V$

$$R_{01} = R_2 / k^2, X_{01} = X_2 / k^2$$

$$k = \frac{V_2}{V_1} \quad k = \frac{200}{1100} \quad [k = 0.1818] \quad k^2 = 0.033$$

$$R_{01} = 0.004 / 0.033, X_{01} = 0.012 / 0.033$$

$$R_{01} = 0.121 \Omega$$

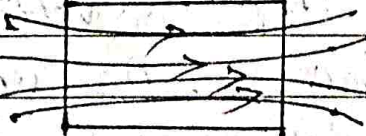
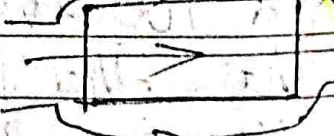
$$X_{01} = 0.366 \Omega$$

* What is magnetic material?

ans $\Rightarrow$ It is a substance that can be magnetized & produce a magnetic field, they are used in many applications like $\rightarrow$ electric motors, generators. For ex $\rightarrow$ iron, nickel.

Types of magnetic material

ferromagnetic paramagnetic diamagnetic

(i)	They are solid.	They can be solid, liquid or gas.	They can be solid, liquid or gas.
(ii)	They strongly attracted by a magnet.	They weakly attracted by a magnet.	They weakly repelled by a magnet.
(iii)	They tend to move from low to high field region.	They tend to move from low to high field region.	They tend to move from high to low field region.
(iv)	Ex $\Rightarrow$ Iron	Ex $\Rightarrow$ Lithium	Ex $\Rightarrow$ Copper
(v)			
(vi)	after remove external magnetic field it retains its magnetic property.	after remove external magnetic field it does not retain its magnetic property.	after remove external magnetic field it does not retain its magnetic property.

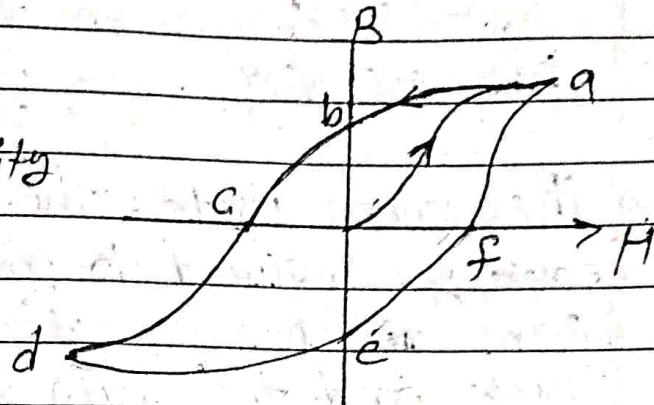
Q. Explain the B-H characteristics of magnetic material.

a $\rightarrow$ Saturation

b $\rightarrow H=0, B \neq 0$ Retentivity

c $\rightarrow H = -H_c, B=0$
coercivity

Hysteresis loop



BH characteristic describe the relationship between magnetic flux density (B) and applied external magnetic field.

- (i) Saturation $\div$ At high value of external magnetic field, the magnetic flux density of a material reaches a maximum value known as saturation.
- (ii) Retentivity $\div$ When external magnetic field reduced to zero but magnetic flux density does not return to zero known as retentivity.
- (iii) Hysteresis $\div$ When external magnetic field increased and decreased than magnetic flux density does not follow the same path.
- (iv) Coercivity $\div$ It is the amount of external magnetic field required to demagnetise a material.
- (v) Permeability $\div$ It is the ratio of magnetic flux density and external magnetic field

$$\mu = \frac{B}{H}$$

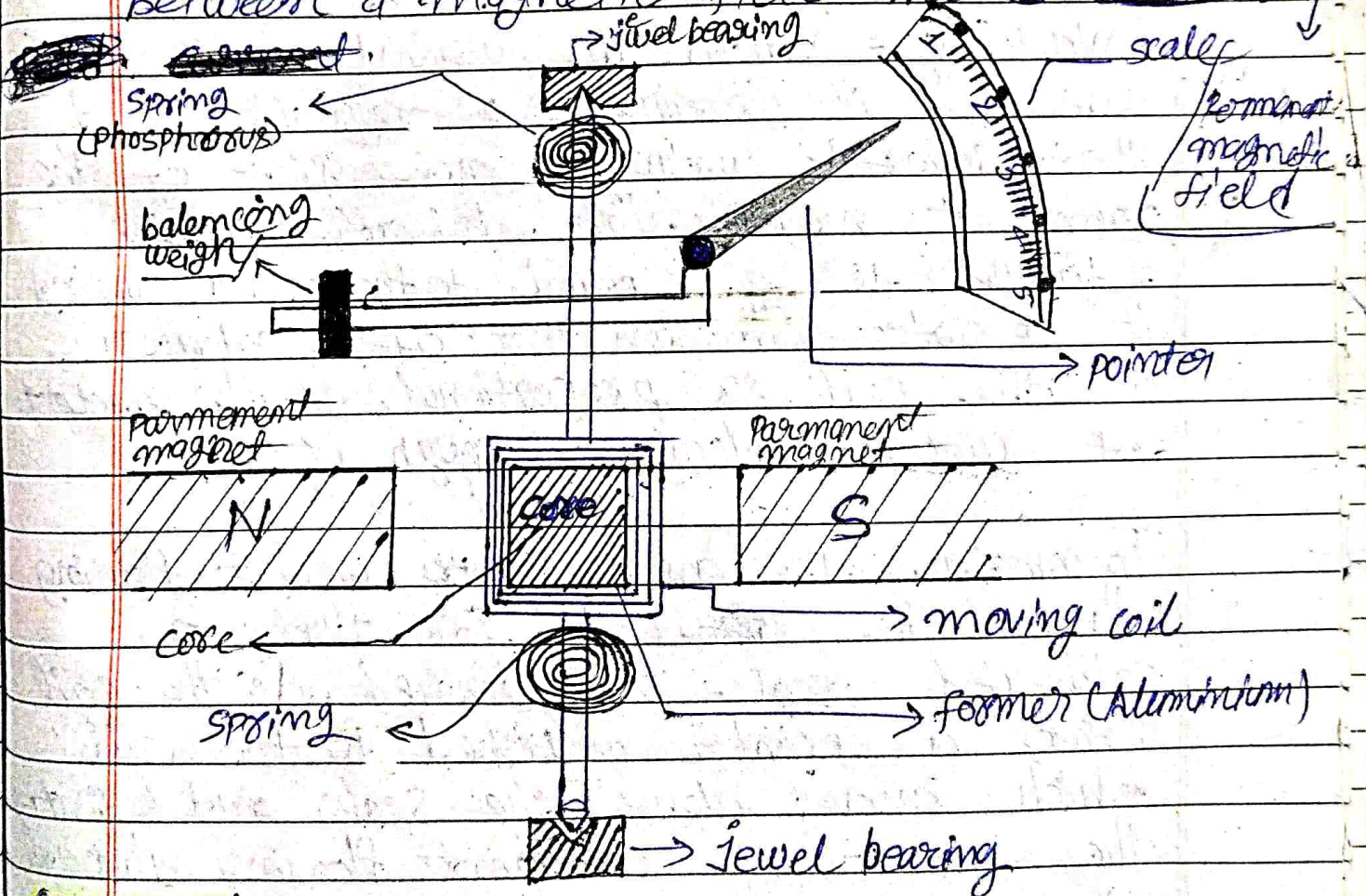
(pyq) What can you infer regarding magnetic properties of a material from area under BH curve?

ans $\Rightarrow$ The area under the BH curve represents the energy required to magnetize the material from ~~an~~ unmagnetized to a fully magnetized state and the demagnetize it back to its original state.

Electrical instrument

Ques Explain construction and working of permanent magnet moving coil instrument. Give its merits and demerits and operating principle of a PMMC.

PMMC - stands for permanent magnet moving coil. PMMC is a type of instrument which is used as voltmeter or ammeter to measure the voltage & current it is based on the principle of interaction between a magnetic field and ~~current~~ ~~current~~.



Construction:

Permanent magnet moving coil consists two permanent magnet N & S, and a core on which moving coils are placed and core is made of former which is made of Aluminium and core is connected to spring and jewel bearing, spring is made of Phosphorous.

A pointer is connected to core with the help of balancing weight and there is a calibrated scale placed over pointer to point magnitude of measurement.

Operating principle :- The operating principle of a permanent magnet moving coil is based on the interaction between a magnetic field and ~~an electrical field~~ permanent magnetic field.

Working :- When dc current flows through ~~and this~~ wire coil it produces a magnetic field ~~torque~~ that interacts with magnetic field of the permanent magnet. This interaction causes a torque to be applied to the coil causing it to rotate. The amount of rotation of the coil is proportional to the amount of current flowing through it.

To measure the amount of current flowing through the ~~coil~~ coil for that a calibrated scale is attached. As the coil rotates a pointer attached to the coil which moves along the scale and indicating the amount of current flowing through the coil.

Applications :-

- (i) Ammeter
- (ii) Voltmeter
- (iii) Galvanometer
- (iv) Ohm meter

Merits or advantages :

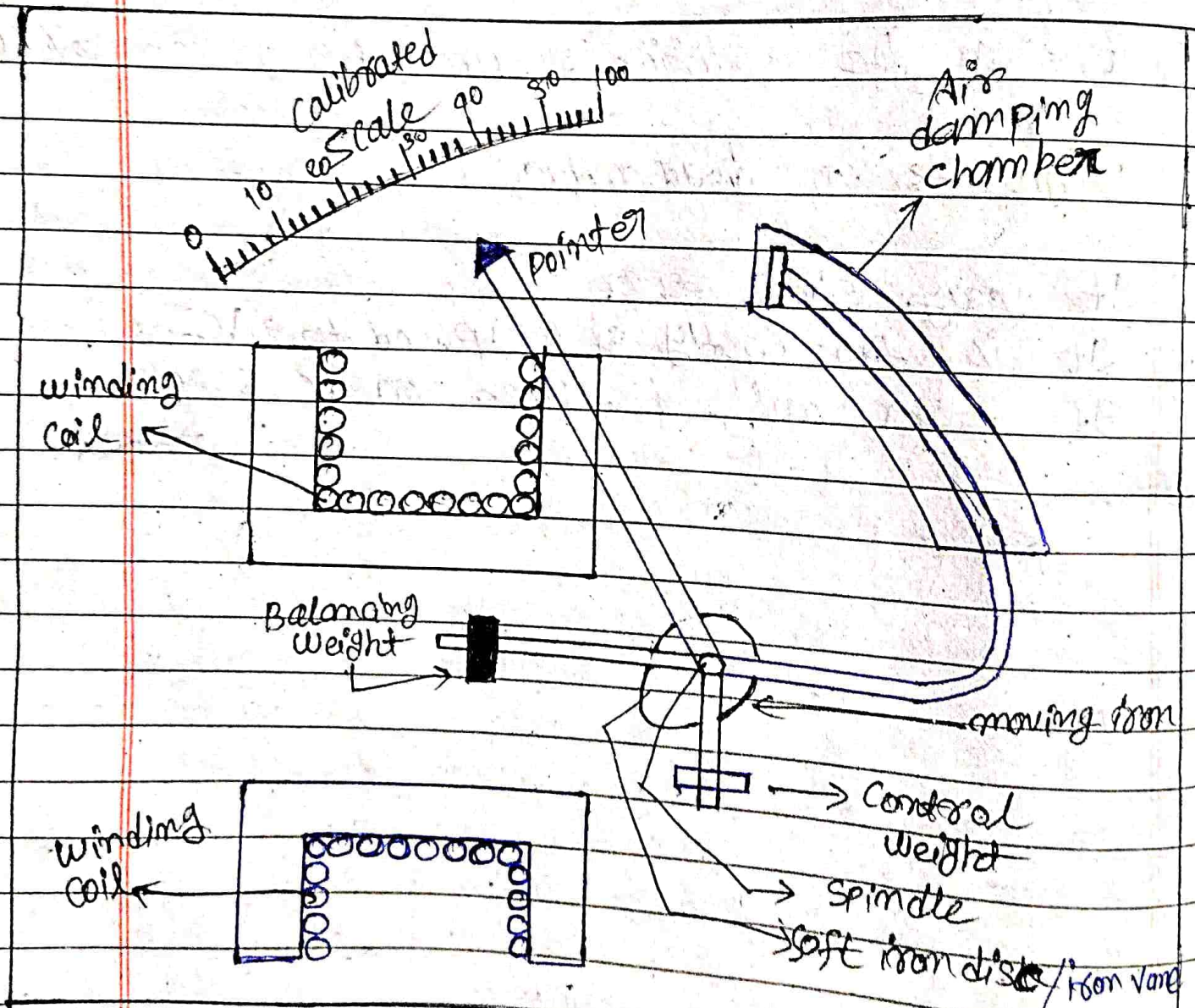
- (i) PMMC consumes less power and has great accuracy.
- (ii) It's scale can cover arc of 270° .
- (iii) It produces no losses due to hysteresis.
- (iv) It can be modified as ammeter or voltmeter.

Demerits or disadvantages :

- (i) It may show error.
- (ii) It is too costly as compared to MCI.
- (iii) It can only be used on dc supply.

(Q70) Explain the construction and working principle of Moving iron instrument. Give applications, merits & demerits.

Ans → Moving iron instrument is a type of analog electrical measuring instrument used to measure AC or DC electrical quantities such as voltage, current, power.



Construction: MII - Stands for Moving iron instrument. Iron instrument consists two winding coil and a spindle on which calibrated scale, Air damping chamber and Soft iron disc and pointer ^{attached} with the help of control weight & Blanding weight, here in moving iron winding coil is the temporary magnet whose magnetic field strength increases or decreases with current passing through it.

Working: When a current flows through coil, it creates a magnetic field around it which interacts with the electromagnet. The interaction of the magnetic fields causes the iron vane to move, which is connected to a pointer that moves along the calibrated scale and indicating the amount of current or voltage ~~flowing~~ flowing through coil.

The amount of deflection of the iron vane depends on the strength of the magnetic field produced by current flowing through the coil, deflection of iron vane is proportional to current flowing in the coil.

Applications: (i) Power measurement

① Voltmeter

(ii) Energy metering

(iv) electrical system testing

② Ammeter

(iii) Load monitoring

③ Speed meter

Advantage: It does not show any error.

① It is too cheaper than PMMC.

② It can be used DC along with AC supply.

disadvantage: it does not have great accuracy.

① It can't modified as ammeter or voltmeter

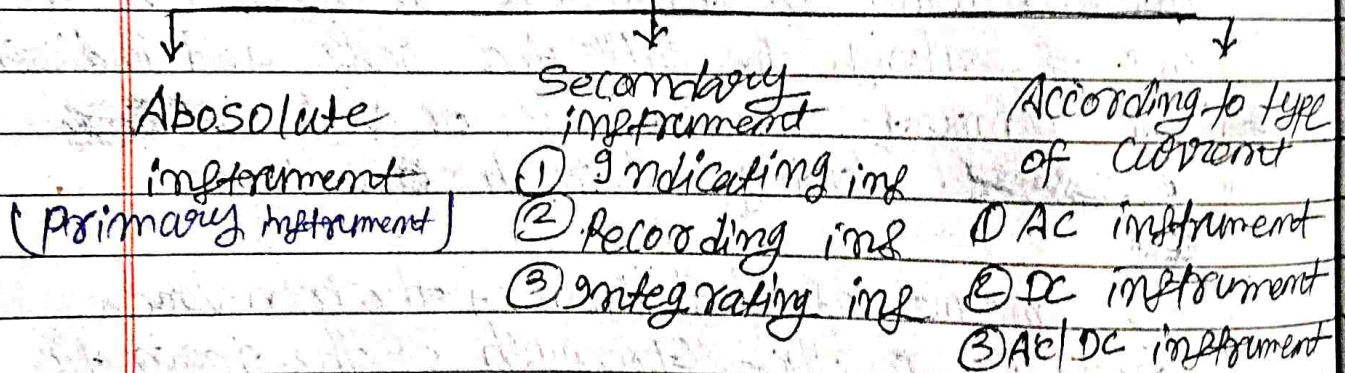
*** Deflection torque** $\div$ Deflection torque used for ~~deflecting~~ deflecting the pointer by measuring quantity.

~~stop~~ **stop torque**

*** Controlling torque** $\div$ Controlling ~~stop~~ stops the pointer at its final position and it brings back the pointer at initial position.

*** Damping torque** $\div$ Damping torque eliminates the oscillation of pointer near its ~~final~~ final position.

electrical Classification of instrument



*** Absolute instrument** $\div$ Absolute instrument also known as primary instrument, it measures a physical quantity and provides reading. It does not require calibration against any other instrument.
Ex $\rightarrow$ thermocouples.

*** ~~Indicating instrument~~** $\div$

*** Secondary instrument** $\div$ Secondary instrument is an instrument that requires to calibration against a primary or standard instrument to ensure the accuracy. Ex $\rightarrow$ multimeter.

i) Indicating instrument ÷ Indicating instrument indicates the magnitude of quantity being measured.

Ex $\Rightarrow$ Ammeter, voltmeter etc.

ii) Recording instrument ÷ Recording instrument records the magnitude of quantity being measured.

Ex $\Rightarrow$ ECG, EEG etc.

iii) Integrating instruments ÷ Integrating instrument add up the total physical quantities that have been measured ~~etc~~ such as volume, mass, temperature, pressure etc.

i) Dc instrument ÷ The instrument whose deflections are proportional to current or voltage, which is used for dc measurement only. Ex $\Rightarrow$ PMMC.

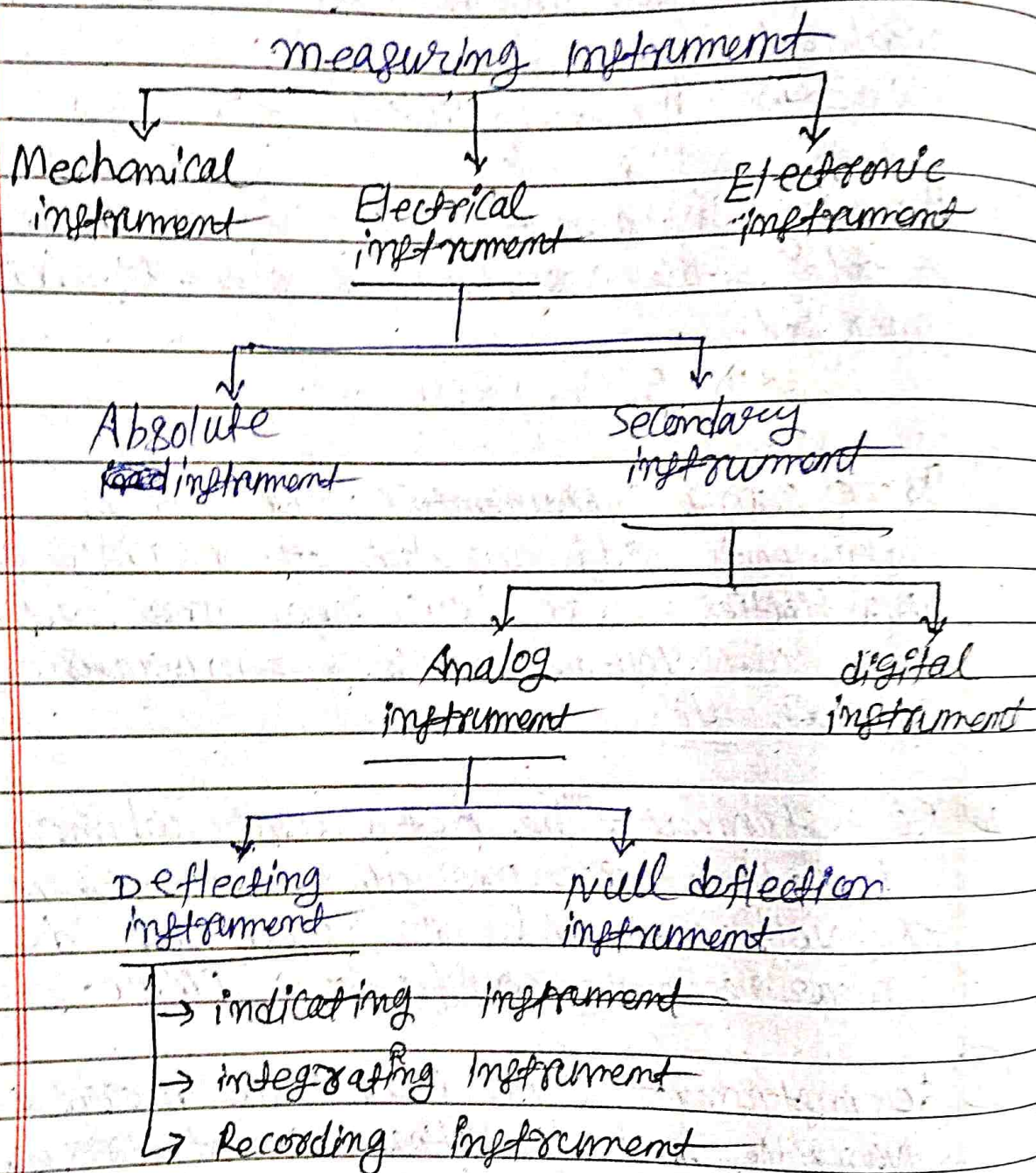
ii) Ac instrument ÷ Ac instrument measures quantities such as voltage current, frequency and power in Ac circuit only.

Ex $\Rightarrow$ Induction motor

iii) Ac/dc instrument ÷ The instrument having deflections proportional to the square of current or voltage, it can be used for 'dc' as well as 'ac' measurement.

Ex $\Rightarrow$ Moving iron instrument.

(Ques) Classify various measuring instruments

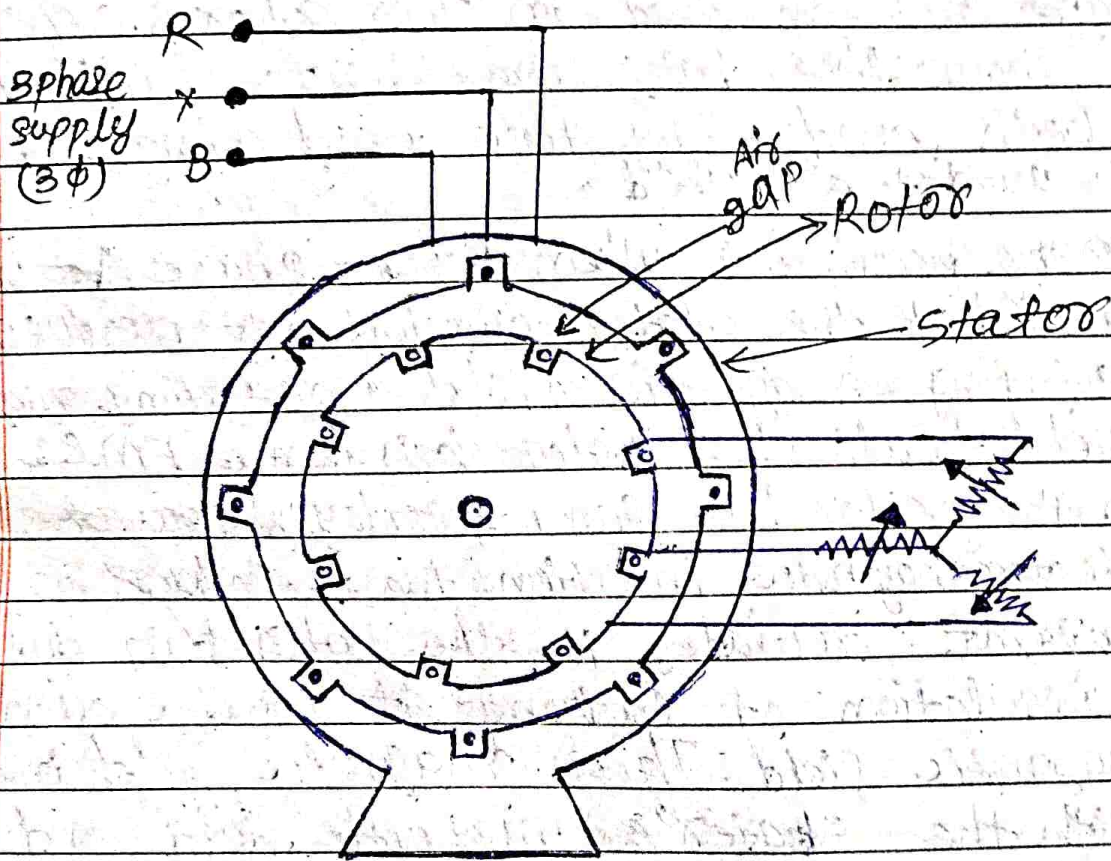


(Ques) which type of instruments are used for measuring DC quantities only?

- Ans →
- ① DC Ammeter
 - ② DC voltmeter
 - ③ DC ohmmeter
 - ④ DC watt meter

Q. Explain the construction and working principle of 3 ϕ induction motor. Why induction motor need stator?

A three phase induction motor is a type of AC motor that converts electrical energy into mechanical energy through electromagnetic induction.



Construction: A three phase induction motor has two parts: first stator and second rotor.

Stator: Stator is the stationary part of the motor and it is made up of a cylinder frame made of steel laminations. There are three windings inside the cylinder apart from 120° degree.

These windings are connected to three-phase AC supply and produce a rotating magnetic field, in the stator, field winding are used.

Rotor ÷ The rotor is the rotating part of the motor and consists of a cylindrical core made of steel laminations. It has a series of conductive bars, made of copper or aluminium that are arranged in a cylindrical shape and embedded in the rotor's core.

The conductive bars are short-circuited at both ends by two end rings. These armature windings are used.

Working principle ÷ When three-phase AC voltage is applied to the stator winding, it produces a rotating magnetic field. This rotating magnetic field cuts the rotor bars hence EMF is induced in the rotor bar from Faraday's law of electromagnetic induction. Due to induced EMF, current circulates in the rotor bar. Due to circulation of current, it creates its own magnetic field. This magnetic field interacts with the stator's magnetic field and produces a torque that rotates the rotor.

pro

induction motor needs a ~~star~~ starter to limit the starting current drawn by the motor during its starting period and provide ~~the motor with a power supply system from~~ protection to the motor against overloading and low voltage condition.

Q. Discuss the various speed control method of three phase induction motor.

∴ running speed of induction motor is

$$N = \frac{120f}{P}$$

from this equation speed of IM can be controlled.

- ① changing the number of poles method :-
Changing the number of poles in the motor by rewinding the stator. This method is not used generally.
- ② frequency method :- The speed of induction motor is directly proportional to the frequency of the power supply, therefore by changing the frequency the speed of IM can be controlled.
- ③ Slip control method :- In this method, the slip of the motor is controlled by varying the rotor resistance. This method is commonly used.
- ④ voltage control method :- The speed of induction motor is directly proportional to the voltage applied to the stator winding. therefore by changing the voltage of stator winding the speed of IM can be controlled.
- ⑤ external resistance method :- In this method By adding external resistance to rotor the speed of the IM can be controlled.

(PYQ) What are the various types of starters?
Explain any two starters in detail.

ans → Here are various types of starters

- (i) D.O.L ~~starter~~ starter
- (ii) Star-Delta ~~starter~~ starter
- (iii) Auto-transformer ~~starter~~ starter

① (D.O.L) Direct-On-line starter ÷ This is the simplest and most common type of starter used with small and medium-sized motors. It connects the motor directly to the supply.

② Star-Delta starter ÷ This starter is used for ~~with~~ larger motors. It connects the motor in a star configuration for starting, and then switches the motor in ~~star~~ delta configuration for normal operation.

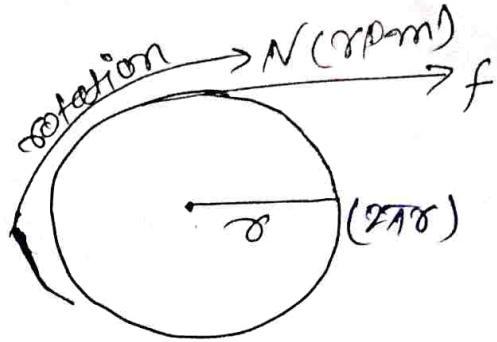
③ Auto-transformer starter ÷ This starter is used for larger motors and it provides a variable voltage to the motor by using an auto-transformer. It provides at starting ~~step down~~ voltage to the motor.

④ Variable frequency drive (VFD) starter ÷ This starter is used for larger motors. It provides a variable frequency and voltage to the motor.

* Torque equation of dc machine

Power develop

$$P = \frac{\text{work done}}{\text{time}}$$



$$P = \frac{f \times \text{distance moved}}{\text{time req for one revolution}}$$

$$P = \frac{f \times 2\pi r}{\left(\frac{60}{N}\right)}$$

time required for one revolution
 $\left(\frac{60}{N}\right)$

$$P = \frac{2\pi r f N}{60} \text{ watt}$$

$\therefore \text{Torque} = f \times r (\text{distance moved})$

$$T = f \times r$$

$$P = \frac{2\pi T \cdot N}{60}$$

Power developed in armature = power at output

$$E_b \cdot I_a = \frac{2\pi T N}{60}$$

$$\therefore E_b = \frac{\phi P N Z}{60 A}$$

$$\frac{\phi P N Z}{60 A} \times I_a = \frac{2\pi T N}{60}$$

$$\frac{\phi P Z}{A} \times I_a = 2\pi T$$

$$T = \frac{\phi P Z \cdot I_a}{2\pi A} \quad \left\{ \because \frac{1}{2\pi} = 0.159 \right\}$$

$$T = \frac{0.159 \cdot I_a \cdot \phi P \cdot Z}{A} \text{ (N-m)} \quad (\text{Torque equation})$$

* Derive Emf & Torque equation of DC machine.

$$\text{Sol}^n \div \left. \begin{array}{l} p = \text{No of poles} \\ \phi = \text{flux} \\ N = \text{speed of armature} \end{array} \right\} \begin{array}{l} Z = \text{no of conductors in armature} \\ A = \text{No of parallel paths} \end{array}$$

Now, Emf induced in armature conductor is from Faraday's law of electromagnetic induction

$$\boxed{\varepsilon = \frac{d\phi}{dt}} \quad \text{--- (1)}$$

total flux ($d\phi$) = flux produced $\times$ no of poles by each pole.

$$\boxed{d\phi = \phi \times p} \quad \text{--- (2)}$$

Time required for to complete one revolution

$$\boxed{dt = \frac{60}{N}} \quad \text{--- (3)}$$

put eqⁿ (2) & (3) in eqⁿ (1)

$$\varepsilon = \frac{\phi \times p}{\frac{60}{N}} \Rightarrow \boxed{\varepsilon = \frac{\phi p N}{60}} \quad \left\{ \begin{array}{l} \text{This is only} \\ \text{for one conductor} \end{array} \right\}$$

Now, Z conductors are distributed in A parallel paths ($\frac{Z}{A}$).

$$\varepsilon = \frac{\phi p N}{60} \times \frac{Z}{A}$$

$$\boxed{\varepsilon = \frac{\phi p N Z}{60 A}} \quad \text{Emf equation of DC motor}$$

$$\text{or } \boxed{\varepsilon = \frac{\phi N P Z}{60 A}}$$

MST

Cage

Ques Explain squirrel induction motor and wound rotor induction motor or compare types of 3 phase induction motors and give applications of each type.

→ Squirrel cage induction motor: A squirrel cage induction motor is a type of motor that uses a squirrel cage rotor which is made up of a cylindrical laminated core with conductive bars with short-circuited. Application: pumps and fans, compressors

→ Wound rotor induction motor: A wound rotor induction motor is a type of motor that uses a wound rotor which is made up of a cylindrical laminated core with three phase winding, which are connected to slip rings that allow external resistors to be connected to the rotor circuit.

Application: cranes, hoists, conveyor system

~~* Types of 3 phase induction motor~~
~~(i) squirrel cage induction motor~~
~~(ii) wound rotor induction motor~~

* Enlist different types of single-phase induction motor. give application.

- (1) squirrel cage induction motor
- (2) wound rotor induction motor

Ques what do you mean by slip?

ans → The difference between the synchronous speed and rotor speed is known as slip.

Note: The speed of the rotating magnetic field is known as synchronous speed.

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Date

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* (1) Synchronous speed = $N_s = \frac{120f}{P}$ rpm

(2) Slip speed = $N_s - N_r$

(3) Slip = $\frac{N_s - N}{N_s} \times 100$ % $S = \frac{N_s - N}{N_s} \times 100$

rotor frequency / slip frequency

(4) $f_r = \frac{P \times (N_s - N)}{120}$

(1) No load speed of motor $\Rightarrow N_0 = N_s(1 - S)$ rpm

(2) full load speed of motor $\Rightarrow N_{f1} = N_s(1 - S)$ rpm

(3) frequency of rotor at full load

~~...~~ $f_r = f_s \times S$
Slip $\rightarrow$ full load

Q. If a 4 pole induction motor running at 50 Hz frequency and frequency of rotor current f_r is 2 Hz find

(1) Synchronous speed

(2) Slip

ans $\Rightarrow$ $N_s = \frac{120f}{P}$ $S = \frac{N_s - N}{N_s} \times 100$

given $\div$ $P = 4$ $f = 50$ Hz

$f_r = 2$ Hz $N_s = \frac{120 \times 50}{4}$ $N_s = 1500$ rpm

Slip = $\frac{N_s - N}{N_s} \times 100$

Q A 30 ; 4 pole, 50Hz induction motor is running at 1455 rpm find slip speed & slip.

$$p = 4$$

$$f = 50 \text{ Hz}$$

ans $\Rightarrow$
$$\text{Slip} = \frac{N - N_s}{N_s} \times 100$$

$$N_s = \frac{120f}{p} \quad N_s = \frac{120 \times 50}{4}$$

$$N_s = 1500$$

$$\text{Slip} = \frac{N_s - N}{N_s} \times 100$$

$$\text{Slip} = \frac{1500 - 1455}{1500} \times 100$$

$$\text{Slip} = \frac{45}{1500} \times 100$$

$$\text{Slip} = 3\%$$

$$\text{Slip speed} = \frac{(N_s - N)}{N_s} \times 1500$$

$$\text{Slip speed} = 4(1500 - 1455)$$

$$\text{Slip speed} = 45 \text{ rpm}$$

* An 8 pole alternator runs at 750 rpm and supply power to a 4 pole induction motor, frequency of rotor current is 1.5 Hz determine the speed of motor/rotor.

$$f_r = \frac{p \times (N_s - N)}{120}$$

$$2 = \frac{4 \times (150 - N)}{120} \Rightarrow 240 = 4 \times (150 - N)$$

$$240 = 150 - N \Rightarrow 60 = 150 - N$$

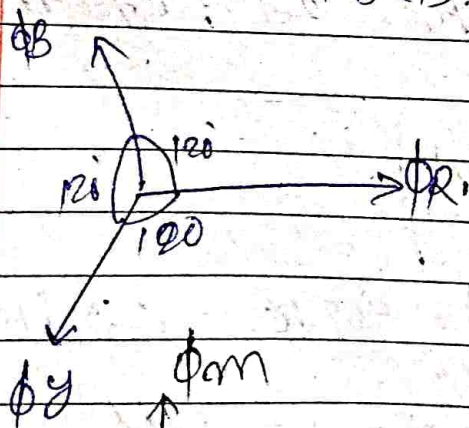
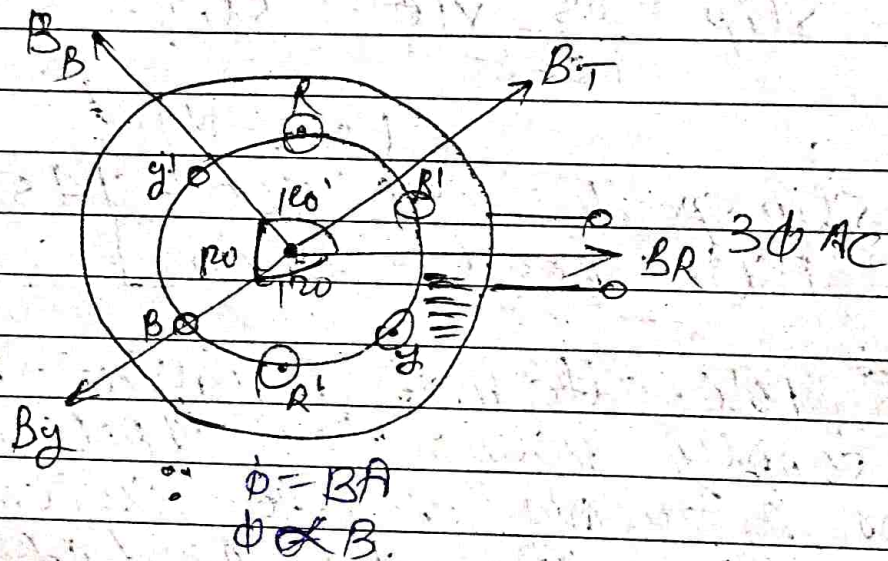
$$N = 150 - 60$$

$$N = 90 \text{ rpm}$$

$$\text{Slip} = \frac{150 - 90}{150} \times 100 = \frac{60}{150} \times 100 = 40\%$$

Q. How rotating magnetic field is produced give mathematical expression.

Ans: When 3- ϕ supply applied to the stator winding of 3 ϕ induction motor, a rotating magnetic field is produced. This magnetic field is such that its poles do not remain in a fixed position on the stator but go on shifting their position around the stator. For this reason, it is known as rotating magnetic field.



$$e = E_m \sin \omega t$$

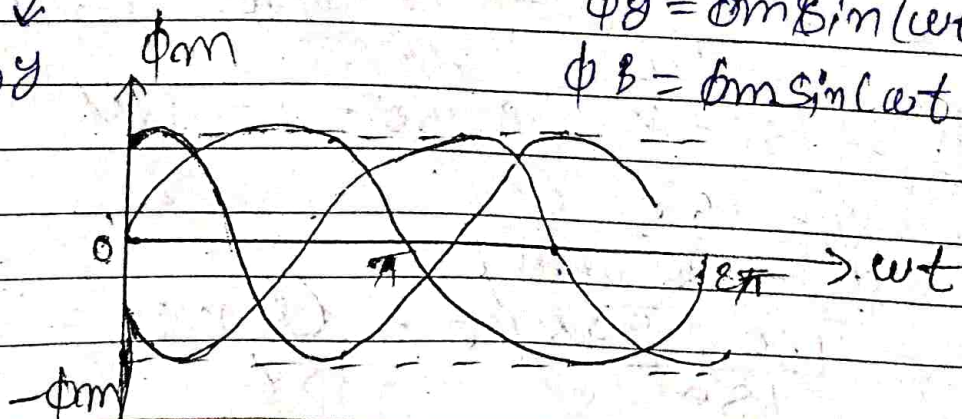
$$\phi = \phi_m \sin \omega t$$

$$\phi_R = \phi_m \sin \omega t$$

$$\phi_Y = \phi_m \sin(\omega t - 120^\circ)$$

$$\phi_B = \phi_m \sin(\omega t - 240^\circ)$$

graph
of eqs



$$\theta = 0^\circ$$

$$\theta = 60^\circ$$

$$\theta = 180^\circ$$

Case I $\rightarrow (\theta = 0^\circ)$

$$\phi_R = \phi_m \sin(0^\circ)$$

$$\boxed{\phi_R = 0}$$

$$\phi_y = \phi_m \sin(0 - 120^\circ)$$

$$\phi_y = \phi_m \sin(-120^\circ)$$

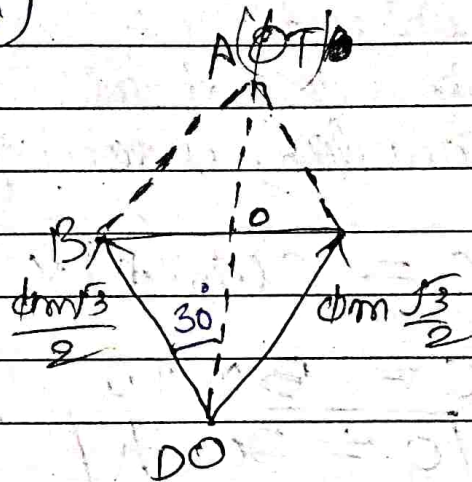
$$\phi_y = -\phi_m \frac{\sqrt{3}}{2}$$

$$\phi_B = \phi_m \sin(\theta - 240^\circ)$$

$$\phi_B = -\phi_m \sin(240^\circ)$$

$$\phi_B = -\phi_m \left(-\frac{\sqrt{3}}{2}\right)$$

$$\boxed{\phi_B = \frac{\phi_m \sqrt{3}}{2}}$$



$$\phi_T = 2OP$$

$$\phi_T = 2OP$$

$$\phi_T = 2 \times OB \cos 30^\circ$$

$$\phi_T = 2 \times \phi_m \frac{\sqrt{3}}{2} \times \cos 30^\circ$$

$$\phi_T = 2 \times \phi_m \frac{\sqrt{3}}{2} \times \frac{\sqrt{3}}{2}$$

$$\phi_T = 2 \times \phi_m \times \frac{3}{4}$$

$$\phi_T = \frac{3}{2} \phi_m$$

$$\boxed{\phi_T = 1.5 \phi_m}$$

* Capacity of the cell =

- ① current (in A) $\times$ time (in hours) Ah
- ② ~~charge (Q) during charging =~~

~~Ques~~ A lead acid cell, maintaining a constant current of 3A for 10 hours before its terminal voltage falls to 1.8V. Calculate the capacity of the cell.

ans $C = C(\text{in A}) \times t(\text{in H})$

$$C = 3 \times 10$$

$$C = 30 \text{ Ah}$$

② Charge (Q) during charging

$$Q = \text{charging current} \times \text{charging time}$$

$$Q = I \times t$$

③ Energy during charging :-

$$E = \text{charging voltage} \times Q$$

$$E = V \times Q$$

④ Charge during discharging

$Q = \text{discharging current} \times \text{Discharging time}$

$$Q = I t$$

⑤ Energy during discharging

$E = \text{Average discharging voltage} \times Q$

$$E = V \times Q$$

⑥ Quantity efficiency = Q during discharging

$$QE = \frac{Q \text{ during discharging}}{Q \text{ during charging}} \times 100$$

⑦ Energy efficiency

$$Ef = \frac{E \text{ during discharging}}{E \text{ during charging}} \times 100$$

(Pye) A battery has taken a charging current of 5.2 A for 24 hours at a voltage of 2.25 V, while discharging it gave a current of 4.5 A for 24 hours at an average voltage of 1.85 V. Calculate the quantity efficiency and energy efficiency of the battery.

Sol: $\text{Q.E} = \frac{\text{Q during dis.c}}{\text{Q during char}} \times 100$

$$\text{Q.d.dis} = I \cdot d \cdot \text{dis} \times t \cdot d \cdot \text{dis}$$

~~$$= 4.5 \times 24$$~~

$$\boxed{\text{Q} = 108 \text{ Ah}}$$

$$\text{Q d.ch} = I \cdot d \cdot \text{ch} \times t \cdot d \cdot \text{char}$$

$$\text{Q} = 5.2 \times 24$$

$$\boxed{\text{Q} = 124.8 \text{ Ah}}$$

$$\text{Q.E} = \frac{108}{124.8} \times 100$$

$$\boxed{\text{Q.E} = 86.53\%}$$

$$\boxed{\text{E.E} = \frac{\text{E dur dis}}{\text{E dur char}} \times 100}$$

$$\text{E dur dis} = \text{Q dur dis} \times V \text{ dur dis}$$

$$E = 108 \times 1.85$$

$$E = 199.8 \text{ Wh}$$

$$E_{\text{dur char}} = \emptyset \text{ dur char} \times V \text{ dur char}$$

$$E = 124.8 \times 2.25$$

$$E = 280.8 \text{ Wh}$$

$$\text{energy efficiency} = \frac{199.8}{280.8} \times 100$$

$$EE = 71.15\%$$

(p40) A 3ϕ , 4 pole, 50 Hz induction motor has a fractional slip = 0.02 at no load and 0.04 at full load. Calculate synchronous speed, No load speed of motor, full load speed of motor, frequency of rotor at full load.

Sol: $P = 4$ no load slip = 0.02
full load slip = 0.04

$$N_s = ? \quad N_o = ? \quad N_f = ? \quad f_r = ?$$

$$N_s = \frac{120f}{P} \quad N_s = \frac{120 \times 50}{4} \quad N_s = 1500 \text{ rpm}$$

$$N_o = N_s(1 - s)$$

$$N_o = 1500(1 - 0.02)$$

$$N_o = 1500 \times 0.98$$

$$N_o = 1470 \text{ rpm}$$

$$N_f = N_s(1 - s)$$

$$N_f = 1500(1 - 0.04)$$

$$N_f = 1500(0.96)$$

$$N_f = 1440 \text{ rpm}$$

$$f_r = f \times s$$

$$f_r = 50 \times 0.04$$

$$f_r = 2 \text{ Hz}$$